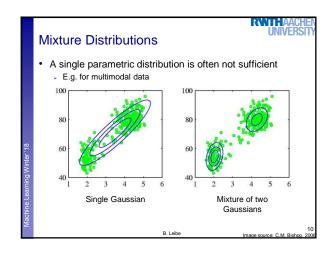
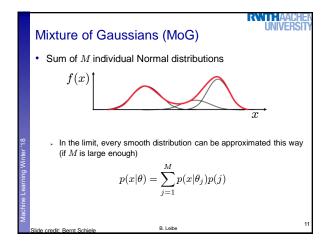
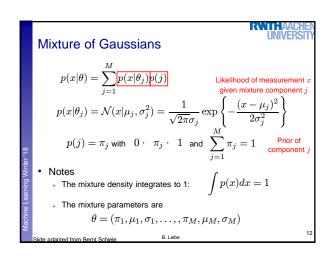
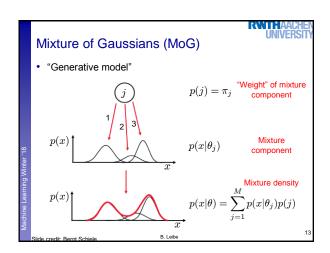


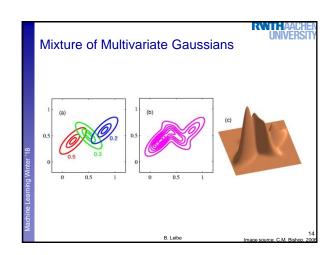
Topics of This Lecture • Mixture distributions • Mixture of Gaussians (MoG) • Maximum Likelihood estimation attempt • K-Means Clustering • Algorithm • Applications • EM Algorithm • Credit assignment problem • MoG estimation • EM Algorithm • Interpretation of K-Means • Technical advice • Applications



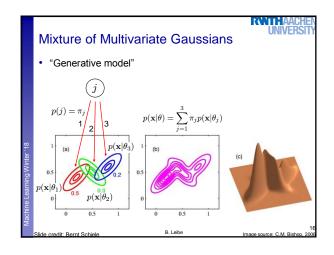


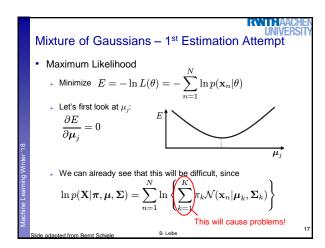


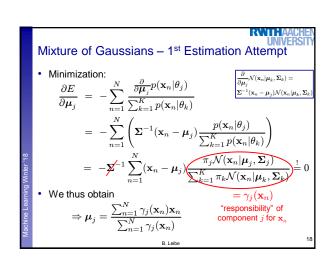


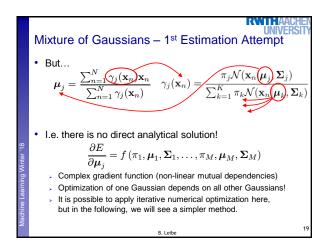


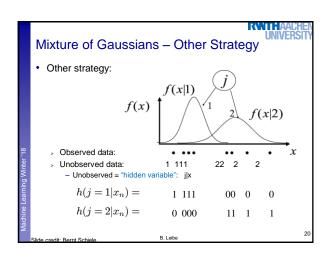
Mixture of Multivariate Gaussians $p(\mathbf{x}|\theta) = \sum_{j=1}^{M} p(\mathbf{x}|\theta_j) p(j)$ $p(\mathbf{x}|\theta_j) = \frac{1}{(2\pi)^{D/2} |\mathbf{\Sigma}_j|^{1/2}} \exp\left\{-\frac{1}{2}(\mathbf{x} - \boldsymbol{\mu}_j)^{\mathrm{T}} \mathbf{\Sigma}_j^{-1} (\mathbf{x} - \boldsymbol{\mu}_j)\right\}$ > Mixture weights / mixture coefficients: $p(j) = \pi_j \text{ with } \quad 0 \cdot \quad \pi_j \cdot \quad 1 \text{ and } \sum_{j=1}^{M} \pi_j = 1$ > Parameters: $\theta = (\pi_1, \boldsymbol{\mu}_1, \mathbf{\Sigma}_1, \dots, \pi_M, \boldsymbol{\mu}_M, \mathbf{\Sigma}_M)$ Slide credit: Bernt Schiele

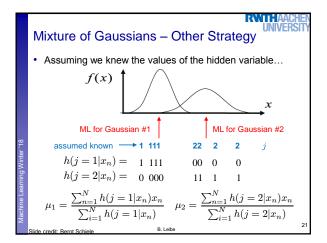


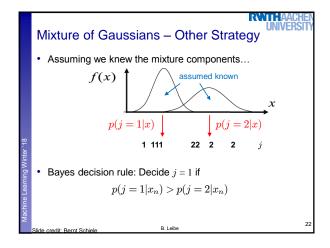


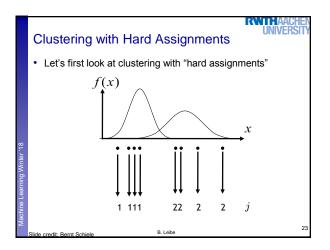


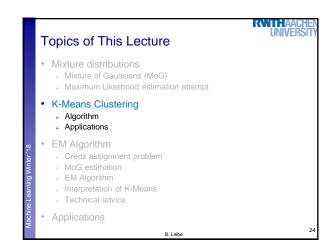


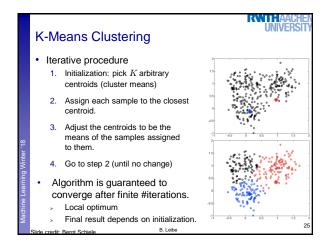


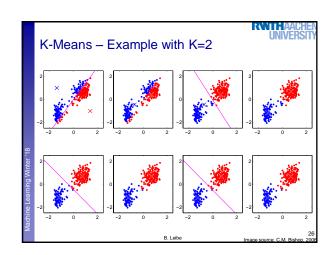


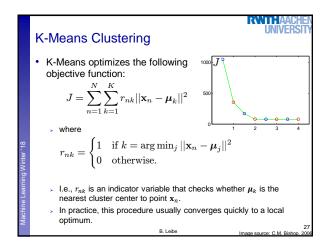


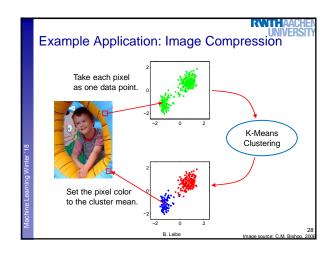


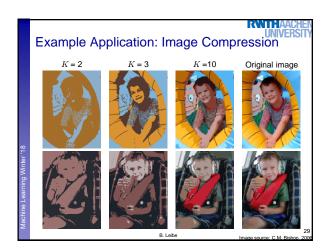


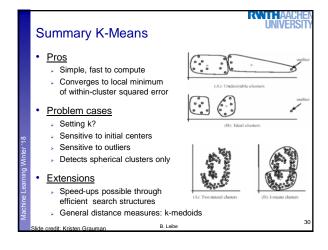


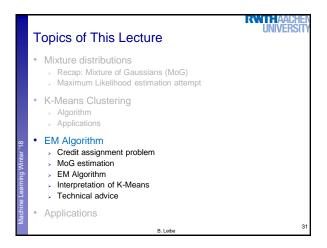


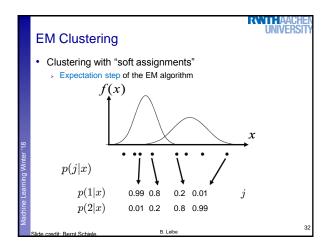


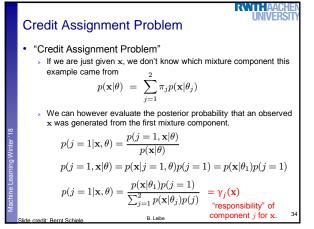


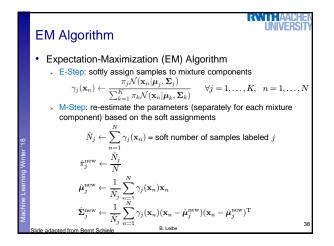


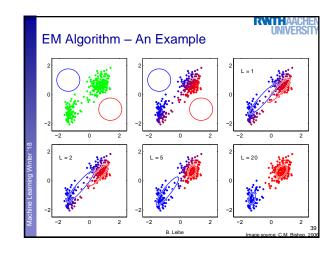


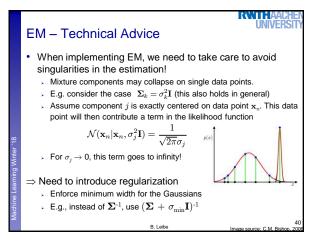


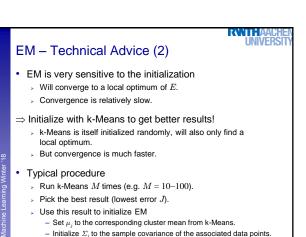


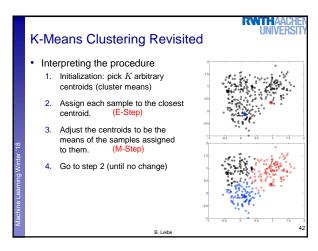


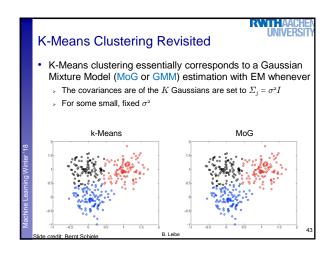


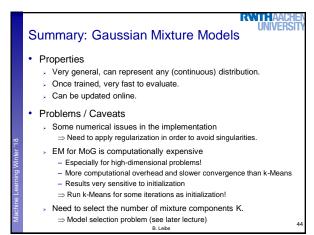


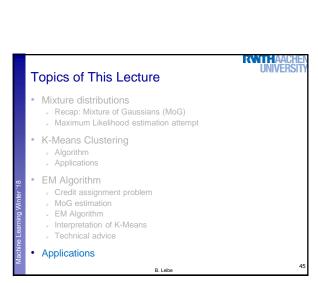


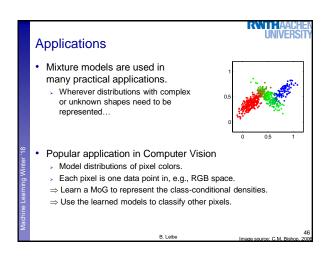


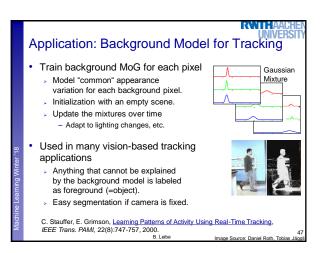


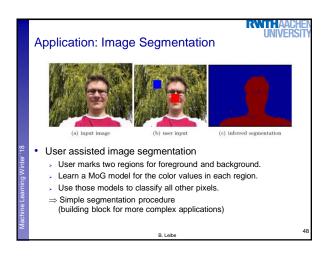












References and Further Reading

More information about EM and MoG estimation is available in Chapter 2.3.9 and the entire Chapter 9 of Bishop's book (recommendable to read).

Christopher M. Bishop Pattern Recognition and Machine Learning Springer, 2006

· Additional information

Original EM paper:

 A.P. Dempster, N.M. Laird, D.B. Rubin, "Maximum-Likelihood from incomplete data via EM algorithm", In Journal Royal Statistical Society, Series B. Vol 39, 1977

EM tutorial:

 J.A. Bilmes, "A Gentle Tutorial of the EM Algorithm and its Application to <u>Parameter Estimation for Gaussian Mixture and Hidden Markov Models</u>", TR-97-021, ICSI, U.C. Berkeley, CA,USA

B. Leibe

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