

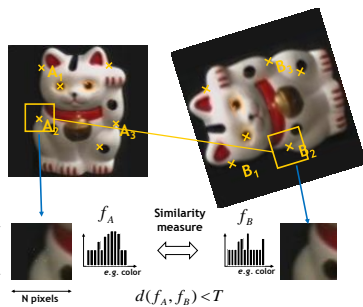
Computer Vision - Lecture 12

Recognition with Local Features

05.12.2016

Bastian Leibe
 RWTH Aachen
<http://www.vision.rwth-aachen.de/>
 leibe@vision.rwth-aachen.de

Recap: Local Feature Matching Outline

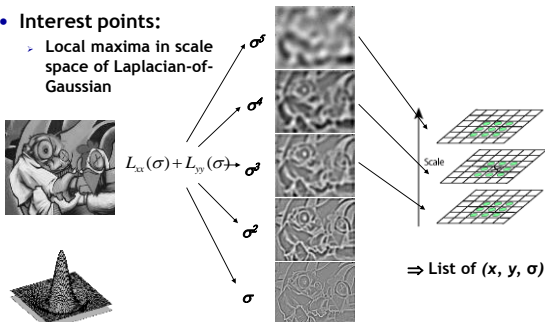


1. Find a set of distinctive key-points
2. Define a region around each keypoint
3. Extract and normalize the region content
4. Compute a local descriptor from the normalized region
5. Match local descriptors

B. Leibe

Recap: Laplacian-of-Gaussian (LoG)

- Interest points:
 - > Local maxima in scale space of Laplacian-of-Gaussian



B. Leibe

Slide adapted from Krystian Mikolajczyk

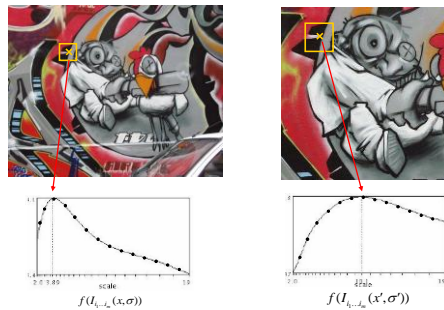
Course Outline

- Image Processing Basics
- Segmentation & Grouping
- Object Recognition
 - Object Categorization I
 - > Sliding Window based Object Detection
 - Local Features & Matching
 - > Local Features - Detection and Description
 - > Recognition with Local Features
 - > Indexing & Visual Vocabularies
 - Object Categorization II
- 3D Reconstruction
- Motion and Tracking

3

Recap: Automatic Scale Selection

- Function responses for increasing scale (scale signature)

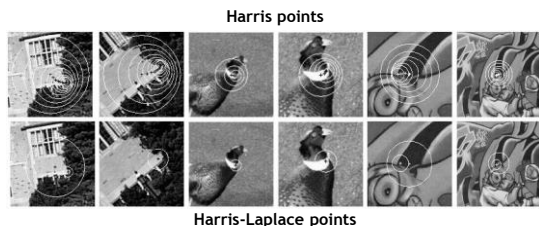


Slide credit: Krystian Mikolajczyk

B. Leibe

Recap: Harris-Laplace [Mikolajczyk '01]

1. Initialization: Multiscale Harris corner detection
2. Scale selection based on Laplacian (same procedure with Hessian \Rightarrow Hessian-Laplace)



Slide adapted from Krystian Mikolajczyk

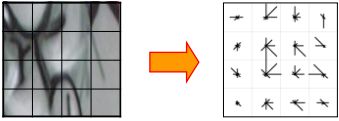
B. Leibe

7

RWTH AACHEN UNIVERSITY

Recap: SIFT Feature Descriptor

- **Scale Invariant Feature Transform**
- **Descriptor computation:**
 - Divide patch into 4x4 sub-patches: 16 cells
 - Compute histogram of gradient orientations (8 reference angles) for all pixels inside each sub-patch
 - Resulting descriptor: 4x4x8 = 128 dimensions



David G. Lowe. "Distinctive image features from scale-invariant keypoints." *IJCV* 60 (2), pp. 91-110, 2004.

Slide credit: Svetlana Lazebnik. B. Leibe

8

RWTH AACHEN UNIVERSITY

Topics of This Lecture

- **Recognition with Local Features**
 - Matching local features
 - Finding consistent configurations
 - Alignment: linear transformations
 - Affine estimation
 - Homography estimation
- **Dealing with Outliers**
 - RANSAC
 - Generalized Hough Transform
- **Indexing with Local Features**
 - Inverted file index
 - Visual Words
 - Visual Vocabulary construction
 - tf-idf weighting

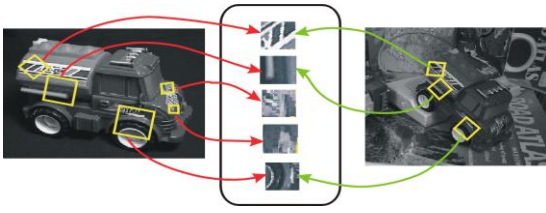
Computer Vision WS 16/17 B. Leibe

10

RWTH AACHEN UNIVERSITY

Recognition with Local Features

- Image content is transformed into local features that are invariant to translation, rotation, and scale
- Goal: Verify if they belong to a consistent configuration



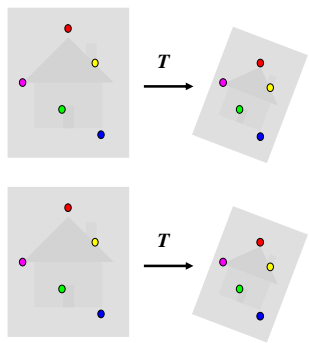
Local Features, e.g. SIFT

Computer Vision WS 16/17 B. Leibe

12

RWTH AACHEN UNIVERSITY

Concepts: Warping vs. Alignment



Warping: Given a source image and a transformation, what does the transformed output look like?

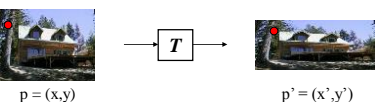
Alignment: Given two images with corresponding features, what is the transformation between them?

Computer Vision WS 16/17 B. Leibe

13

RWTH AACHEN UNIVERSITY

Parametric (Global) Warping



$p = (x, y)$ $p' = (x', y')$

- Transformation T is a coordinate-changing machine:

$$p' = T(p)$$
- What does it mean that T is global?
 - It's the same for any point p
 - It can be described by just a few numbers (parameters)
- Let's represent T as a matrix:

$$p' = \mathbf{M}p, \quad \begin{bmatrix} x' \\ y' \end{bmatrix} = \mathbf{M} \begin{bmatrix} x \\ y \end{bmatrix}$$

Computer Vision WS 16/17 B. Leibe

14

RWTH AACHEN UNIVERSITY

What Can be Represented by a 2x2 Matrix?

- **2D Scaling?**

$$\begin{aligned} x' &= s_x * x \\ y' &= s_y * y \end{aligned} \quad \begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} s_x & 0 \\ 0 & s_y \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$
- **2D Rotation around (0,0)?**

$$\begin{aligned} x' &= \cos \theta * x - \sin \theta * y \\ y' &= \sin \theta * x + \cos \theta * y \end{aligned} \quad \begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$
- **2D Shearing?**

$$\begin{aligned} x' &= x + sh_x * y \\ y' &= sh_y * x + y \end{aligned} \quad \begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & sh_x \\ sh_y & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

Computer Vision WS 16/17 B. Leibe

15

RWTH AACHEN UNIVERSITY

What Can be Represented by a 2x2 Matrix?

- **2D Mirror about y axis?**
 $x' = -x$
 $y' = y$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$
- **2D Mirror over (0,0)?**
 $x' = -x$
 $y' = -y$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$
- **2D Translation?**
 $x' = x + t_x$
 $y' = y + t_y$

NO!

16

RWTH AACHEN UNIVERSITY

2D Linear Transformations

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

- Only linear 2D transformations can be represented with a 2x2 matrix.
- Linear transformations are combinations of ...
 - Scale,
 - Rotation,
 - Shear, and
 - Mirror

17

RWTH AACHEN UNIVERSITY

Homogeneous Coordinates

- **Q:** How can we represent translation as a 3x3 matrix using homogeneous coordinates?
 $x' = x + t_x$
 $y' = y + t_y$
- **A:** Using the rightmost column:

$$\text{Translation} = \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix}$$

18

RWTH AACHEN UNIVERSITY

Basic 2D Transformations

- Basic 2D transformations as 3x3 matrices

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Translation

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} s_x & 0 & 0 \\ 0 & s_y & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Scaling

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Rotation

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & sh_x & 0 \\ sh_y & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Shearing

19

RWTH AACHEN UNIVERSITY

2D Affine Transformations

$$\begin{bmatrix} x' \\ y' \\ w \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

- **Affine transformations** are combinations of ...
 - Linear transformations, and
 - Translations
- *Parallel lines remain parallel*

20

RWTH AACHEN UNIVERSITY

Projective Transformations

$$\begin{bmatrix} x' \\ y' \\ w \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

- **Projective transformations:**
 - Affine transformations, and
 - Projective warps
- *Parallel lines do not necessarily remain parallel*

21

RWTH AACHEN UNIVERSITY

Alignment Problem

- We have previously considered how to fit a model to image evidence
 - E.g., a line to edge points
- In alignment, we will fit the parameters of some transformation according to a set of matching feature pairs ("correspondences").

Computer Vision WS 16/17 22

Slide credit: Kristen Grauman B. Leibe

RWTH AACHEN UNIVERSITY

Let's Start with Affine Transformations

- Simple fitting procedure (linear least squares)
- Approximates viewpoint changes for roughly planar objects and roughly orthographic cameras
- Can be used to initialize fitting for more complex models

Computer Vision WS 16/17 23

Slide credit: Svetlana Lazebnik B. Leibe

RWTH AACHEN UNIVERSITY

Fitting an Affine Transformation

- Affine model approximates perspective projection of planar objects

Computer Vision WS 16/17 24

Slide credit: Kristen Grauman B. Leibe Image source: David Lowe

RWTH AACHEN UNIVERSITY

Fitting an Affine Transformation

- Assuming we know the correspondences, how do we get the transformation?

$$\begin{bmatrix} x'_i \\ y'_i \end{bmatrix} = \begin{bmatrix} m_1 & m_2 \\ m_3 & m_4 \end{bmatrix} \begin{bmatrix} x_i \\ y_i \end{bmatrix} + \begin{bmatrix} t_1 \\ t_2 \end{bmatrix}$$

Computer Vision WS 16/17 25

B. Leibe

RWTH AACHEN UNIVERSITY

Recall: Least Squares Estimation

- Set of data points: $(X_1, X'_1), (X_2, X'_2), (X_3, X'_3)$
- Goal: a linear function to predict X' 's from X 's:

$$Xa + b = X'$$
- We want to find a and b .
- How many (X, X') pairs do we need?

$$\begin{matrix} X_1 a + b = X'_1 \\ X_2 a + b = X'_2 \end{matrix} \quad \begin{bmatrix} X_1 & 1 \\ X_2 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} X'_1 \\ X'_2 \end{bmatrix} \quad Ax = B$$
- What if the data is noisy?

$$\begin{bmatrix} X_1 & 1 \\ X_2 & 1 \\ X_3 & 1 \\ \dots & \dots \end{bmatrix} \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} X'_1 \\ X'_2 \\ X'_3 \\ \dots \end{bmatrix}$$

Overconstrained problem

min $\|Ax - B\|^2$

⇒ Least-squares minimization

Solution: $x = A^+ B$

Matlab: $x = A \setminus B$

Computer Vision WS 16/17 26

Slide credit: Alexei Efros B. Leibe

RWTH AACHEN UNIVERSITY

Fitting an Affine Transformation

- Assuming we know the correspondences, how do we get the transformation?

$$\begin{bmatrix} x'_i \\ y'_i \end{bmatrix} = \begin{bmatrix} m_1 & m_2 \\ m_3 & m_4 \end{bmatrix} \begin{bmatrix} x_i \\ y_i \end{bmatrix} + \begin{bmatrix} t_1 \\ t_2 \end{bmatrix}$$

$$\begin{bmatrix} m_1 \\ m_2 \\ m_3 \\ m_4 \\ t_1 \\ t_2 \end{bmatrix} = \begin{bmatrix} \\ \\ \\ \\ \\ \end{bmatrix}$$

Computer Vision WS 16/17 27

B. Leibe

RWTH AACHEN UNIVERSITY

Fitting an Affine Transformation

$$\begin{bmatrix} \dots & & & & & & m_1 \\ x_i & y_i & 0 & 0 & 1 & 0 & m_2 \\ 0 & 0 & x_i & y_i & 0 & 1 & m_3 \\ \dots & & & & & & m_4 \\ & & & & & & t_1 \\ & & & & & & t_2 \end{bmatrix} = \begin{bmatrix} \dots \\ x'_i \\ y'_i \\ \dots \end{bmatrix}$$

- How many matches (correspondence pairs) do we need to solve for the transformation parameters?
- Once we have solved for the parameters, how do we compute the coordinates of the corresponding point for (x_{new}, y_{new}) ?

Computer Vision WS 16/17 28

RWTH AACHEN UNIVERSITY

Homography

- A projective transform is a mapping between any two perspective projections with the same center of projection.
 - I.e. two planes in 3D along the same sight ray
- Properties
 - Rectangle should map to arbitrary quadrilateral
 - Parallel lines aren't
 - but must preserve straight lines
- This is called a **homography**

$$\begin{bmatrix} wx' \\ wy' \\ w \end{bmatrix} = \begin{bmatrix} * & * & * \\ * & * & * \\ * & * & * \end{bmatrix} \begin{bmatrix} x \\ y \\ I \end{bmatrix}$$

$p' \quad H \quad p$

Computer Vision WS 16/17 29

RWTH AACHEN UNIVERSITY

Homography

- A projective transform is a mapping between any two perspective projections with the same center of projection.
 - I.e. two planes in 3D along the same sight ray
- Properties
 - Rectangle should map to arbitrary quadrilateral
 - Parallel lines aren't
 - but must preserve straight lines
- This is called a **homography**

$$\begin{bmatrix} wx' \\ wy' \\ w \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ I \end{bmatrix}$$

$p' \quad H \quad p$

Set scale factor to 1
⇒ 8 parameters left.

Computer Vision WS 16/17 30

RWTH AACHEN UNIVERSITY

Fitting a Homography

- Estimating the transformation

Homogenous coordinates Image coordinates

$$\begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$x' = Hx$
 $x'' = \frac{1}{z'} x'$

Computer Vision WS 16/17 31

RWTH AACHEN UNIVERSITY

Fitting a Homography

- Estimating the transformation

Homogenous coordinates Image coordinates

$$\begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$x' = Hx$
 $x'' = \frac{1}{z'} x'$

Computer Vision WS 16/17 32

RWTH AACHEN UNIVERSITY

Fitting a Homography

- Estimating the transformation

Homogenous coordinates Image coordinates

$$\begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$x' = Hx$
 $x'' = \frac{1}{z'} x'$

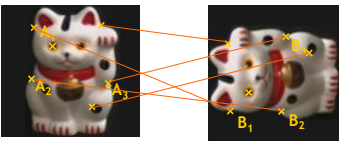
$$x'_A = \frac{h_{11}x_{A0} + h_{12}y_{A0} + h_{13}}{h_{31}x_{A0} + h_{32}y_{A0} + 1}$$

Computer Vision WS 16/17 33

RWTH AACHEN UNIVERSITY

Fitting a Homography

- Estimating the transformation



Homogenous coordinates

$$\begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Image coordinates

$$\begin{bmatrix} x'' \\ y'' \\ z'' \end{bmatrix} = \begin{bmatrix} x' \\ y' \\ z' \end{bmatrix}$$

Matrix notation

$$x'' = Hx'$$

$$x'' = \frac{1}{z'} x'$$

$$x_A \leftrightarrow x_{B_1}$$

$$x_A \leftrightarrow x_{B_2}$$

$$x_A \leftrightarrow x_{B_3}$$

$$\vdots$$

$$x_A = \frac{h_{11}x_{B_1} + h_{12}y_{B_1} + h_{13}}{h_{31}x_{B_1} + h_{32}y_{B_1} + 1}$$

$$y_A = \frac{h_{21}x_{B_1} + h_{22}y_{B_1} + h_{23}}{h_{31}x_{B_1} + h_{32}y_{B_1} + 1}$$

$$x_A \leftrightarrow x_{B_1}$$

$$x_A \leftrightarrow x_{B_2}$$

$$x_A \leftrightarrow x_{B_3}$$

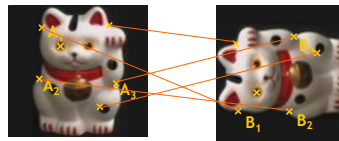
$$\vdots$$

Computer Vision WS 16/17 34
Slide credit: Krystian Mikolajczyk B. Leibe

RWTH AACHEN UNIVERSITY

Fitting a Homography

- Estimating the transformation



$$x_A \leftrightarrow x_{B_1}$$

$$x_A \leftrightarrow x_{B_2}$$

$$x_A \leftrightarrow x_{B_3}$$

$$\vdots$$

$$x_A = \frac{h_{11}x_{B_1} + h_{12}y_{B_1} + h_{13}}{h_{31}x_{B_1} + h_{32}y_{B_1} + 1}$$

$$y_A = \frac{h_{21}x_{B_1} + h_{22}y_{B_1} + h_{23}}{h_{31}x_{B_1} + h_{32}y_{B_1} + 1}$$

$$x_A \leftrightarrow x_{B_1}$$

$$x_A \leftrightarrow x_{B_2}$$

$$x_A \leftrightarrow x_{B_3}$$

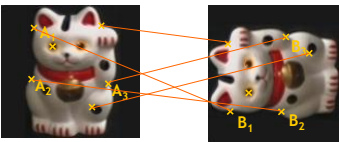
$$\vdots$$

Computer Vision WS 16/17 35
Slide credit: Krystian Mikolajczyk B. Leibe

RWTH AACHEN UNIVERSITY

Fitting a Homography

- Estimating the transformation



Homogenous coordinates

$$\begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Image coordinates

$$\begin{bmatrix} x'' \\ y'' \\ z'' \end{bmatrix} = \begin{bmatrix} x' \\ y' \\ z' \end{bmatrix}$$

$$x_A \leftrightarrow x_{B_1}$$

$$x_A \leftrightarrow x_{B_2}$$

$$x_A \leftrightarrow x_{B_3}$$

$$\vdots$$

$$x_A = \frac{h_{11}x_{B_1} + h_{12}y_{B_1} + h_{13}}{h_{31}x_{B_1} + h_{32}y_{B_1} + 1}$$

$$y_A = \frac{h_{21}x_{B_1} + h_{22}y_{B_1} + h_{23}}{h_{31}x_{B_1} + h_{32}y_{B_1} + 1}$$

$$x_A h_{31} x_{B_1} + x_A h_{32} y_{B_1} + x_A = h_{11} x_{B_1} + h_{12} y_{B_1} + h_{13}$$

$$h_{11} x_{B_1} + h_{12} y_{B_1} + h_{13} - x_A h_{31} x_{B_1} - x_A h_{32} y_{B_1} - x_A = 0$$

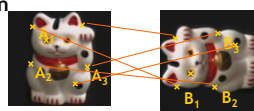
$$h_{21} x_{B_1} + h_{22} y_{B_1} + h_{23} - y_A h_{31} x_{B_1} - y_A h_{32} y_{B_1} - y_A = 0$$

Computer Vision WS 16/17 36
Slide credit: Krystian Mikolajczyk B. Leibe

RWTH AACHEN UNIVERSITY

Fitting a Homography

- Estimating the transformation



$$h_{11} x_{B_1} + h_{12} y_{B_1} + h_{13} - x_A h_{31} x_{B_1} - x_A h_{32} y_{B_1} - x_A = 0$$

$$h_{21} x_{B_1} + h_{22} y_{B_1} + h_{23} - y_A h_{31} x_{B_1} - y_A h_{32} y_{B_1} - y_A = 0$$

$$Ah = 0$$

$$x_A \leftrightarrow x_{B_1}$$

$$x_A \leftrightarrow x_{B_2}$$

$$x_A \leftrightarrow x_{B_3}$$

$$\vdots$$

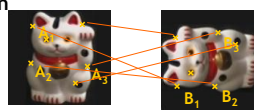
$$\begin{bmatrix} x_{B_1} & y_{B_1} & 1 & 0 & 0 & 0 & -x_A & -x_A y_{B_1} & -x_A \\ 0 & 0 & 0 & x_{B_1} & y_{B_1} & 1 & -y_A & -y_A x_{B_1} & -y_A \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \end{bmatrix} \begin{bmatrix} h_{11} \\ h_{12} \\ h_{13} \\ h_{21} \\ h_{22} \\ h_{23} \\ h_{31} \\ h_{32} \\ h_{33} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ \vdots \\ \vdots \\ \vdots \\ \vdots \\ 0 \\ 0 \\ 1 \end{bmatrix}$$

Computer Vision WS 16/17 37
Slide credit: Krystian Mikolajczyk B. Leibe

RWTH AACHEN UNIVERSITY

Fitting a Homography

- Estimating the transformation
- Solution:
 - Null-space vector of A



SVD $Ah = 0$

$$A = ?$$

$$x_A \leftrightarrow x_{B_1}$$

$$x_A \leftrightarrow x_{B_2}$$

$$x_A \leftrightarrow x_{B_3}$$

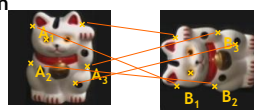
$$\vdots$$

Computer Vision WS 16/17 38
Slide credit: Krystian Mikolajczyk B. Leibe

RWTH AACHEN UNIVERSITY

Fitting a Homography

- Estimating the transformation
- Solution:
 - Null-space vector of A
 - Corresponds to smallest singular vector



SVD $Ah = 0$

$$A = UDV^T = U \begin{bmatrix} d_{11} & \dots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \dots & d_{99} \end{bmatrix} \begin{bmatrix} v_{11} & \dots & v_{19} \\ \vdots & \ddots & \vdots \\ v_{91} & \dots & v_{99} \end{bmatrix}^T$$

$$h = \begin{bmatrix} v_{19} \\ \vdots \\ v_{99} \end{bmatrix}$$

Minimizes least square error

Computer Vision WS 16/17 39
Slide credit: Krystian Mikolajczyk B. Leibe

Computer Vision WS 16/17

Image Warping with Homographies

Image plane in front

Black area where no pixel maps to

Slide credit: Steve Seitz

RWTH AACHEN UNIVERSITY

40

Computer Vision WS 16/17

Uses: Analyzing Patterns and Shapes

- What is the shape of the b/w floor pattern?

The floor (enlarged)

Slide credit: Antonio Criminisi

RWTH AACHEN UNIVERSITY

41

Computer Vision WS 16/17

Analyzing Patterns and Shapes

Automatic rectification

From Martin Kemp *The Science of Art* (manual reconstruction)

Slide credit: Antonio Criminisi

RWTH AACHEN UNIVERSITY

42

Computer Vision WS 16/17

Topics of This Lecture

- Recognition with Local Features
 - Matching local features
 - Finding consistent configurations
 - Alignment: linear transformations
 - Affine estimation
 - Homography estimation
- Dealing with Outliers
 - RANSAC
 - Generalized Hough Transform
- Indexing with Local Features
 - Inverted file index
 - Visual Words
 - Visual Vocabulary construction
 - tf-idf weighting

Slide credit: B. Leibe

RWTH AACHEN UNIVERSITY

43

Computer Vision WS 16/17

Problem: Outliers

- Outliers can hurt the quality of our parameter estimates, e.g.,
 - An erroneous pair of matching points from two images
 - A feature point that is noise or doesn't belong to the transformation we are fitting.

Slide credit: Kristen Grauman

RWTH AACHEN UNIVERSITY

44

Computer Vision WS 16/17

Example: Least-Squares Line Fitting

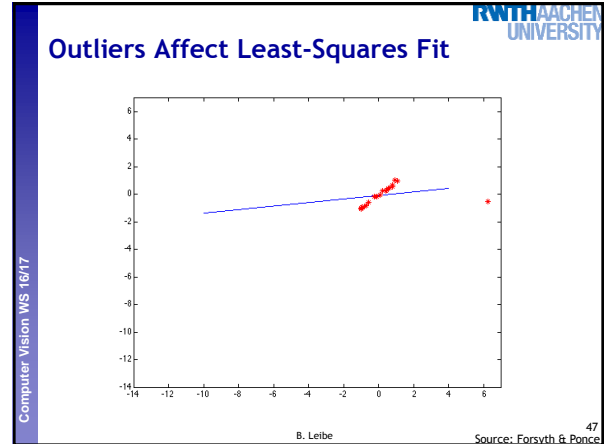
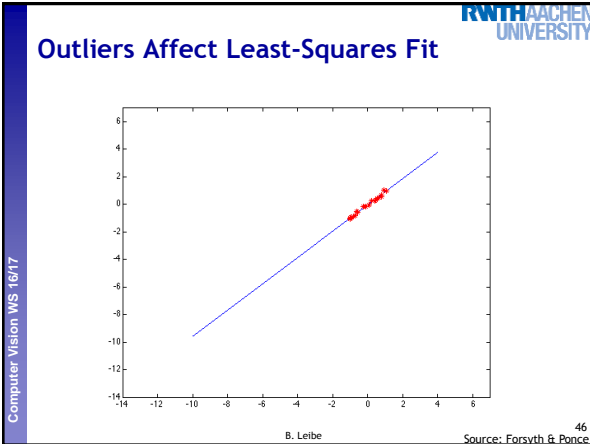
- Assuming all the points that belong to a particular line are known

Slide credit: B. Leibe

RWTH AACHEN UNIVERSITY

45

Source: Forsyth & Ponce



Computer Vision WS 16/17

Strategy 1: RANSAC [Fischler81]

- **R**andom **S**ample **C**onsensus
- Approach: we want to avoid the impact of outliers, so let's look for "inliers", and use only those.
- Intuition: if an outlier is chosen to compute the current fit, then the resulting line won't have much support from rest of the points.

Slide credit: Kristen Grauman B. Leibe 48

Computer Vision WS 16/17

RANSAC

RANSAC loop:

1. Randomly select a *seed group* of points on which to base transformation estimate (e.g., a group of matches)
2. Compute transformation from seed group
3. Find *inliers* to this transformation
4. If the number of inliers is sufficiently large, re-compute least-squares estimate of transformation on all of the inliers

- Keep the transformation with the largest number of inliers

Slide credit: Kristen Grauman B. Leibe 49

Computer Vision WS 16/17

RANSAC Line Fitting Example

- Task: Estimate the best line
 - How many points do we need to estimate the line?

Slide credit: linxiang Chai B. Leibe 50

Computer Vision WS 16/17

RANSAC Line Fitting Example

- Task: Estimate the best line

Sample two points

Slide credit: linxiang Chai B. Leibe 51

Computer Vision WS 16/17

RWTH AACHEN UNIVERSITY

RANSAC Line Fitting Example

- Task: Estimate the best line

Fit a line to them

Slide credit: Jinxiang Chai

B. Leibe

52

Computer Vision WS 16/17

RWTH AACHEN UNIVERSITY

RANSAC Line Fitting Example

- Task: Estimate the best line

Total number of points within a threshold of line.

Slide credit: Jinxiang Chai

B. Leibe

53

Computer Vision WS 16/17

RWTH AACHEN UNIVERSITY

RANSAC Line Fitting Example

- Task: Estimate the best line

"7 inlier points"

Total number of points within a threshold of line.

Slide credit: Jinxiang Chai

B. Leibe

54

Computer Vision WS 16/17

RWTH AACHEN UNIVERSITY

RANSAC Line Fitting Example

- Task: Estimate the best line

Repeat, until we get a good result.

Slide credit: Jinxiang Chai

B. Leibe

55

Computer Vision WS 16/17

RWTH AACHEN UNIVERSITY

RANSAC Line Fitting Example

- Task: Estimate the best line

"11 inlier points"

Repeat, until we get a good result.

Slide credit: Jinxiang Chai

B. Leibe

56

Computer Vision WS 16/17

RWTH AACHEN UNIVERSITY

RANSAC: How many samples?

- How many samples are needed?
 - Suppose w is fraction of inliers (points from line).
 - n points needed to define hypothesis (2 for lines)
 - k samples chosen.
- Prob. that a single sample of n points is correct: w^n
- Prob. that all k samples fail is: $(1 - w^n)^k$

⇒ Choose k high enough to keep this below desired failure rate.

Slide credit: David Lowe

B. Leibe

57

RWTH AACHEN UNIVERSITY

RANSAC: Computed k ($p=0.99$)

Sample size n	Proportion of outliers						
	5%	10%	20%	25%	30%	40%	50%
2	2	3	5	6	7	11	17
3	3	4	7	9	11	19	35
4	3	5	9	13	17	34	72
5	4	6	12	17	26	57	146
6	4	7	16	24	37	97	293
7	4	8	20	33	54	163	588
8	5	9	26	44	78	272	1177

Computer Vision WS 16/17 58

Slide credit: David Lowe B. Leibe

RWTH AACHEN UNIVERSITY

After RANSAC

- RANSAC divides data into inliers and outliers and yields estimate computed from minimal set of inliers.
- Improve this initial estimate with estimation over all inliers (e.g. with standard least-squares minimization).
- But this may change inliers, so alternate fitting with re-classification as inlier/outlier.

Computer Vision WS 16/17 59

Slide credit: David Lowe B. Leibe

RWTH AACHEN UNIVERSITY

Example: Finding Feature Matches

- Find best stereo match within a square search window (here 300 pixels²)
- Global transformation model: epipolar geometry

Computer Vision WS 16/17 60

Slide credit: David Lowe B. Leibe

RWTH AACHEN UNIVERSITY

Example: Finding Feature Matches

- Find best stereo match within a square search window (here 300 pixels²)
- Global transformation model: epipolar geometry

before RANSAC after RANSAC

Computer Vision WS 16/17 61

Slide credit: David Lowe B. Leibe

RWTH AACHEN UNIVERSITY

Problem with RANSAC

- In many practical situations, the percentage of outliers (incorrect putative matches) is often very high (90% or above).
- Alternative strategy: Generalized Hough Transform

Computer Vision WS 16/17 62

Slide credit: Svetlana Lazebnik B. Leibe

RWTH AACHEN UNIVERSITY

Strategy 2: Generalized Hough Transform

- Suppose our features are scale- and rotation-invariant
 - Then a single feature match provides an alignment hypothesis (translation, scale, orientation).

Computer Vision WS 16/17 63

Slide credit: Svetlana Lazebnik B. Leibe

RWTH AACHEN UNIVERSITY

Strategy 2: Generalized Hough Transform

- Suppose our features are scale- and rotation-invariant
 - Then a single feature match provides an alignment hypothesis (translation, scale, orientation).
 - Of course, a hypothesis from a single match is unreliable.
 - Solution: let each match vote for its hypothesis in a Hough space with very coarse bins.

model

Computer Vision WS 16/17 64

Slide credit: Svetlana Lazebnik B. Leibe Image source: David Lowe

RWTH AACHEN UNIVERSITY

Pose Clustering and Verification with SIFT

- To detect instances of objects from a model base:
 - Index descriptors
 - Distinctive features narrow down possible matches

Computer Vision WS 16/17 65

Slide credit: Kristen Grauman B. Leibe Image source: David Lowe

RWTH AACHEN UNIVERSITY

Indexing Local Features

New image

Model base

Computer Vision WS 16/17 66

Slide credit: Kristen Grauman Image source: David Lowe

RWTH AACHEN UNIVERSITY

Pose Clustering and Verification with SIFT

- To detect instances of objects from a model base:
 - Index descriptors
 - Distinctive features narrow down possible matches
 - Generalized Hough transform to vote for poses
 - Keypoints have record of parameters relative to model coordinate system
 - Affine fit to check for agreement between model and image features
 - Fit and verify using features from Hough bins with 3+ votes

Computer Vision WS 16/17 67

Slide credit: Kristen Grauman B. Leibe Image source: David Lowe

RWTH AACHEN UNIVERSITY

Object Recognition Results

Background subtract for model boundaries

Objects recognized

Recognition in spite of occlusion

Computer Vision WS 16/17 68

Slide credit: Kristen Grauman B. Leibe Image source: David Lowe

RWTH AACHEN UNIVERSITY

Location Recognition

Training

Computer Vision WS 16/17 69

B. Leibe [Lowe, IJCV'04] Slide credit: David Lowe

Recall: Difficulties of Voting

- Noise/clutter can lead to as many votes as true target.
- Bin size for the accumulator array must be chosen carefully.
- (Recall Hough Transform)
- In practice, good idea to make broad bins and spread votes to nearby bins, since verification stage can prune bad vote peaks.

Summary

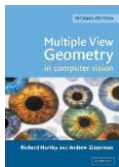
- Recognition by alignment: looking for object and pose that fits well with image
 - Use good correspondences to designate hypotheses.
 - Invariant local features offer more reliable matches.
 - Find consistent "inlier" configurations in clutter
 - Generalized Hough Transform
 - RANSAC
- Alignment approach to recognition can be effective if we find reliable features within clutter.
 - Application: large-scale image retrieval
 - Application: recognition of specific (mostly planar) objects
 - Movie posters
 - Books
 - CD covers

References and Further Reading

- A detailed description of local feature extraction and recognition can be found in Chapters 3-5 of Grauman & Leibe ([available on the L2P](#)).



➢ K. Grauman, B. Leibe
Visual Object Recognition
Morgan & Claypool publishers, 2011



➢ R. Hartley, A. Zisserman
Multiple View Geometry in
Computer Vision
2nd Ed., Cambridge Univ. Press, 2004

- More details on RANSAC can also be found in Chapter 4.7 of Hartley & Zisserman.