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Computer Vision - Lecture 10

Local Features

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Computer Vision WS 16/17

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Course Outline

- Image Processing Basics
- Segmentation & Grouping
- Object Recognition & Categorization I
 - Sliding Window based Object Detection
- Local Features & Matching
 - Local Features - Detection and Description
 - Recognition with Local Features
- Object Categorization II
 - Part based Approaches
 - Deep Learning Approaches
- 3D Reconstruction
- Motion and Tracking

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Recap: Sliding-Window Object Detection

- If object may be in a cluttered scene, slide a window around looking for it.



- Essentially, this is a brute-force approach with many local decisions.

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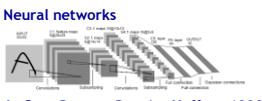
Classifier Construction: Many Choices...

Nearest Neighbor



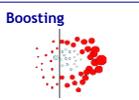
Berg, Berg, Malik 2005,
Chum, Zisserman 2007,
Boiman, Shechtman, Irani 2008, ...

Neural networks



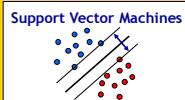
LeCun, Bottou, Bengio, Haffner 1998
Rowley, Baluja, Kanade 1998
...

Boosting



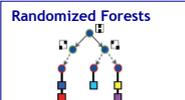
Viola, Jones 2001,
Torralba et al. 2004,
Opelt et al. 2006,
Benenson 2012, ...

Support Vector Machines



Vapnik, Schölkopf 1995,
Papageorgiou, Poggio '01,
Dalal, Triggs 2005,
Vedaldi, Zisserman 2012

Randomized Forests



Amit, Geman 1997,
Breiman 2001,
Lepetit, Fua 2006,
Gall, Lempitsky 2009, ...

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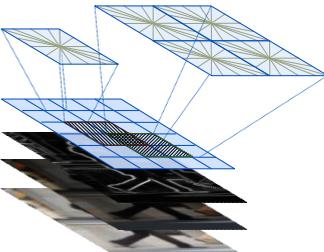
Slide adapted from Kristen Grauman

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Recap: HOG Descriptor Processing Chain



Object/Non-object

Linear SVM

Collect HOGs over detection window

Contrast normalize over overlapping spatial cells

Weighted vote in spatial & orientation cells

Compute gradients

Gamma compression

Image Window

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Slide credit: Navneet Dalal

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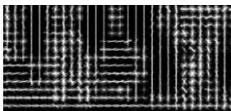
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Recap: Pedestrian Detection with HOG

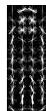
- Train a pedestrian template using a linear SVM
- At test time, convolve feature map with template
 - Linear SVM classification function

$$y(x) = w^T x + b$$

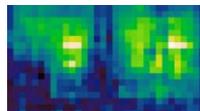
HOG feature map



Template



Detector response map



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N. Dalal and B. Triggs, *Histograms of Oriented Gradients for Human Detection*, CVPR 2005

Slide credit: Svetlana Lazebnik

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Classifier Construction: Many Choices...

Nearest Neighbor

Shakhnarovich, Viola, Darrell 2003
Berg, Berg, Malik 2005,
Boiman, Shechtman, Irani 2008, ...

Neural networks

LeCun, Bottou, Bengio, Haffner 1998
Rowley, Baluja, Kanade 1998
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Boosting

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Randomized Forests

Amit, Geman 1997,
Breiman 2001,
Lepetit, Fua 2006,
Gall, Lempitsky 2009, ...

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Recap: AdaBoost

Final classifier is combination of the weak classifiers

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Recap: AdaBoost Feature+Classifier Selection

- Want to select the single rectangle feature and threshold that best separates **positive** (faces) and **negative** (non-faces) training examples, in terms of *weighted error*.

Resulting weak classifier:

$$h_t(x) = \begin{cases} +1 & \text{if } f_t(x) > \theta_t \\ -1 & \text{otherwise} \end{cases}$$

For next round, reweight the examples according to errors, choose another filter/threshold combo.

Outputs of a possible rectangle feature on faces and non-faces.

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Recap: Viola-Jones Face Detector

- Train with 5K positives, 350M negatives
- Real-time detector using 38 layer cascade
- 6061 features in final layer
- [Implementation available in OpenCV: <http://sourceforge.net/projects/opencvlibrary/>]

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Limitations: Low Training Resolutions

- Many (older) S/W detectors operate on tiny images
 - Viola&Jones: 24x24 pixels
 - Torralba et al.: 32x32 pixels
 - Dalal&Triggs: 64x96 pixels (notable exception)
- Main reasons
 - Training efficiency (exhaustive feature selection in AdaBoost)
 - Evaluation speed
 - Want to recognize objects at small scales
- But...
 - Limited information content available at those resolutions
 - Not enough support to compensate for occlusions!

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Limitations: Changing Aspect Ratios

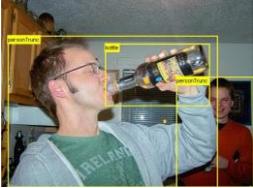
- Sliding window requires fixed window size
 - Basis for learning efficient cascade classifier
- How to deal with changing aspect ratios?
 - Fixed window size
 - Wastes training dimensions
 - Adapted window size
 - Difficult to share features
 - "Squashed" views [Dalal&Triggs]
 - Need to squash test image, too

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Limitations (continued)

- Not all objects are “box” shaped

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Limitations (continued)

- Non-rigid, deformable objects not captured well with representations assuming a fixed 2D structure; or must assume fixed viewpoint
- Objects with less-regular textures not captured well with holistic appearance-based descriptions



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Limitations (continued)

- If considering windows in isolation, context is lost




Sliding window Detector's view

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Figure credit: Derek Hoiem B. Leibe

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Limitations (continued)

- In practice, often entails large, cropped training set (expensive)
- Requiring good match to a global appearance description can lead to sensitivity to partial occlusions




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Image credit: Adam, Rivlin, & Shimshoni K. Grauman, B. Leibe

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Topics of This Lecture

- Local Invariant Features**
 - Motivation
 - Requirements, Invariances
- Keypoint Localization**
 - Harris detector
 - Hessian detector
- Scale Invariant Region Selection**
 - Automatic scale selection
 - Laplacian-of-Gaussian detector
 - Difference-of-Gaussian detector
 - Combinations
- Local Descriptors**
 - Orientation normalization
 - SIFT

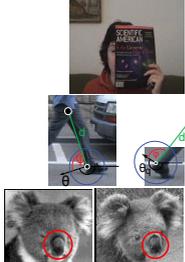
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Motivation

- Global representations have major limitations
- Instead, describe and match only local regions
- Increased robustness to
 - Occlusions
 - Articulation
 - Intra-category variations



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Application: Image Matching

by Diva Sian

by swashford

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Harder Case

by Diva Sian

by scqbt

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Harder Still?

NASA Mars Rover images

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Answer Below (Look for tiny colored squares)

NASA Mars Rover images with SIFT feature matches (Figure by Noah Snavely)

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Application: Image Stitching

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Application: Image Stitching

- Procedure:
 - Detect feature points in both images

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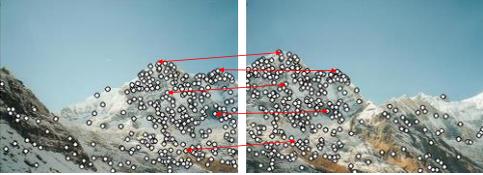
Slide credit: Darya Frolaya, Denis Simakov

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Application: Image Stitching



- Procedure:
 - Detect feature points in both images
 - Find corresponding pairs

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Application: Image Stitching



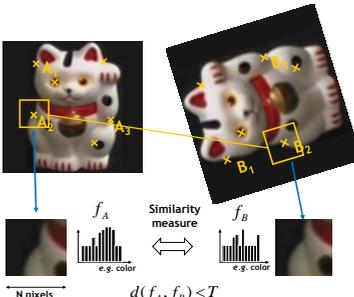
- Procedure:
 - Detect feature points in both images
 - Find corresponding pairs
 - Use these pairs to align the images

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General Approach



1. Find a set of distinctive keypoints
2. Define a region around each keypoint
3. Extract and normalize the region content
4. Compute a local descriptor from the normalized region
5. Match local descriptors

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Common Requirements

- Problem 1:
 - Detect the same point *independently* in both images



No chance to match!

We need a repeatable detector!

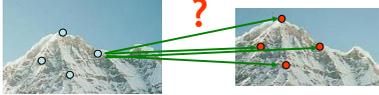
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Common Requirements

- Problem 1:
 - Detect the same point *independently* in both images
- Problem 2:
 - For each point correctly recognize the corresponding one



We need a reliable and distinctive descriptor!

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Invariance: Geometric Transformations



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Levels of Geometric Invariance

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Requirements

- Region extraction needs to be **repeatable** and **accurate**
 - **Invariant** to translation, rotation, scale changes
 - **Robust** or **covariant** to out-of-plane (≠affine) transformations
 - **Robust** to lighting variations, noise, blur, quantization
- **Locality**: Features are local, therefore robust to occlusion and clutter.
- **Quantity**: We need a sufficient number of regions to cover the object.
- **Distinctiveness**: The regions should contain “interesting” structure.
- **Efficiency**: Close to real-time performance.

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Many Existing Detectors Available

- **Hessian & Harris** [Beaudet '78], [Harris '88]
- **Laplacian, DoG** [Lindeberg '98], [Lowe '99]
- **Harris-/Hessian-Laplace** [Mikolajczyk & Schmid '01]
- **Harris-/Hessian-Affine** [Mikolajczyk & Schmid '04]
- **EBR and IBR** [Tuytelaars & Van Gool '04]
- **MSER** [Matas '02]
- **Salient Regions** [Kadir & Brady '01]
- **Others...**

• *Those detectors have become a basic building block for many recent applications in Computer Vision.*

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Keypoint Localization

- **Goals**:
 - Repeatable detection
 - Precise localization
 - Interesting content

⇒ Look for two-dimensional signal changes

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Finding Corners

- **Key property**:
 - In the region around a corner, image gradient has two or more dominant directions
- Corners are *repeatable* and *distinctive*

C.Harris and M.Stephens. "A Combined Corner and Edge Detector." *Proceedings of the 4th Alvey Vision Conference, 1988.*

Slide credit: Svetlana Lazebnik

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Corners as Distinctive Interest Points

- **Design criteria**
 - We should easily recognize the point by looking through a small window (*locality*)
 - Shifting the window in *any* direction should give a *large* change in intensity (*good localization*)

"flat" region: no change in all directions

"edge": no change along the edge direction

"corner": significant change in all directions

Slide credit: Alexei Efros

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Harris Detector Formulation

- Change of intensity for the shift $[u, v]$:

$$E(u, v) = \sum_{x, y} w(x, y) [I(x+u, y+v) - I(x, y)]^2$$

Window function

Shifted intensity

Intensity

Window function $w(x, y) =$ or
 1 in window, 0 outside Gaussian

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Harris Detector Formulation

- This measure of change can be approximated by:

$$E(u, v) \approx [u \ v] M \begin{bmatrix} u \\ v \end{bmatrix}$$

where M is a 2×2 matrix computed from image derivatives:

$$M = \sum_{x, y} w(x, y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

Gradient with respect to x , times gradient with respect to y

Sum over image region - the area we are checking for corner

$$M = \begin{bmatrix} \sum I_x I_x & \sum I_x I_y \\ \sum I_x I_y & \sum I_y I_y \end{bmatrix} = \sum \begin{bmatrix} I_x \\ I_y \end{bmatrix} \begin{bmatrix} I_x & I_y \end{bmatrix}$$

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Harris Detector Formulation

where M is a 2×2 matrix computed from image derivatives:

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Gradient with respect to x , times gradient with respect to y

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What Does This Matrix Reveal?

- First, let's consider an axis-aligned corner:

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What Does This Matrix Reveal?

- First, let's consider an axis-aligned corner:

$$M = \begin{bmatrix} \sum I_x^2 & \sum I_x I_y \\ \sum I_x I_y & \sum I_y^2 \end{bmatrix} = \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix}$$

- This means:
 - Dominant gradient directions align with x or y axis
 - If either λ is close to 0, then this is not a corner, so look for locations where both are large.
- What if we have a corner that is not aligned with the image axes?

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General Case

- Since M is symmetric, we have $M = R^{-1} \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} R$ (Eigenvalue decomposition)
- We can visualize M as an ellipse with axis lengths determined by the eigenvalues and orientation determined by R

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Interpreting the Eigenvalues

- Classification of image points using eigenvalues of M :

λ_1 and λ_2 are small;
 E is almost constant
in all directions

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Corner Response Function

$$R = \det(M) - \alpha \text{trace}(M)^2 = \lambda_1 \lambda_2 - \alpha (\lambda_1 + \lambda_2)^2$$

- Fast approximation
 - Avoid computing the eigenvalues
 - α : constant (0.04 to 0.06)

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Window Function $w(x,y)$

$$M = \sum_{x,y} w(x,y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

- Option 1: uniform window
 - Sum over square window
$$M = \sum_{x,y} \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

1 in window, 0 outside

 - Problem: not rotation invariant
- Option 2: Smooth with Gaussian
 - Gaussian already performs weighted sum
$$M = g(\sigma) * \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

Gaussian

 - Result is rotation invariant

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Summary: Harris Detector [Harris88]

- Compute second moment matrix (autocorrelation matrix)
$$M(\sigma_I, \sigma_D) = g(\sigma_I) * \begin{bmatrix} I_x^2(\sigma_D) & I_x I_y(\sigma_D) \\ I_x I_y(\sigma_D) & I_y^2(\sigma_D) \end{bmatrix}$$
 - Image derivatives
 - Square of derivatives
 - Gaussian filter $g(\sigma)$
- Cornerness function - two strong eigenvalues
$$R = \det[M(\sigma_I, \sigma_D)] - \alpha [\text{trace}(M(\sigma_I, \sigma_D))]^2$$

$$= g(I_x^2)g(I_y^2) - [g(I_x I_y)]^2 - \alpha [g(I_x^2) + g(I_y^2)]^2$$
- Perform non-maximum suppression

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Harris Detector: Workflow

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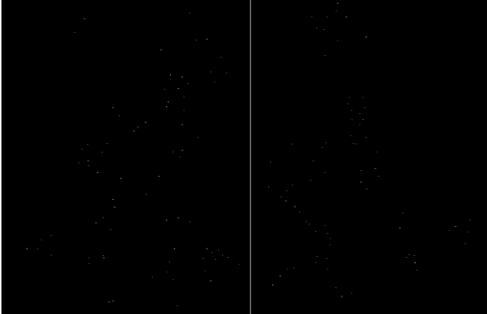
Harris Detector: Workflow

- Compute corner responses R

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Harris Detector: Workflow



- Take only the local maxima of R , where $R > \text{threshold}$.

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Harris Detector: Workflow

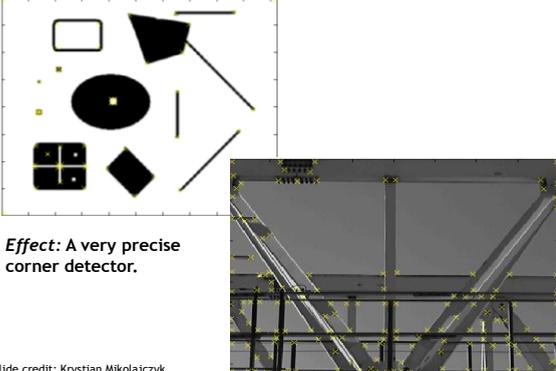


- Resulting Harris points

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Harris Detector - Responses [Harris88]



Effect: A very precise corner detector.

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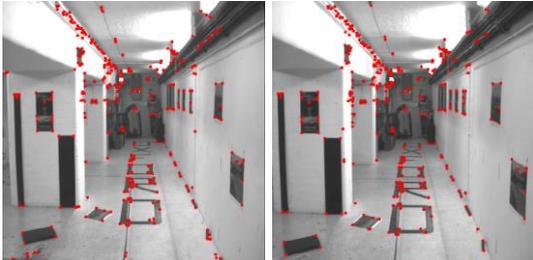
Harris Detector - Responses [Harris88]



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Harris Detector - Responses [Harris88]



- Results are well suited for finding stereo correspondences

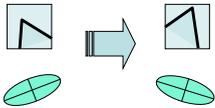


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Harris Detector: Properties

- Rotation invariance?



Ellipse rotates but its shape (i.e. eigenvalues) remains the same

Corner response R is invariant to image rotation

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Harris Detector: Properties

- Rotation invariance
- Scale invariance?

Corner

All points will be classified as edges!

Not invariant to image scale!

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Hessian Detector [Beaudet78]

- Hessian determinant

$$Hessian(I) = \begin{bmatrix} I_{xx} & I_{xy} \\ I_{xy} & I_{yy} \end{bmatrix}$$

Note: these are 2nd derivatives!

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Intuition: Search for strong derivatives in two orthogonal directions

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Hessian Detector [Beaudet78]

- Hessian determinant

$$Hessian(I) = \begin{bmatrix} I_{xx} & I_{xy} \\ I_{xy} & I_{yy} \end{bmatrix}$$

$$\det(Hessian(I)) = I_{xx}I_{yy} - I_{xy}^2$$

In Matlab:

$$I_{xx} * I_{yy} - (I_{xy})^2$$

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Hessian Detector - Responses [Beaudet78]

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Effect: Responses mainly on corners and strongly textured areas.

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Hessian Detector - Responses [Beaudet78]

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Topics of This Lecture

- Local Invariant Features
 - Motivation
 - Requirements, Invariances
- Keypoint Localization
 - Harris detector
 - Hessian detector
- Scale Invariant Region Selection
 - Automatic scale selection
 - Laplacian-of-Gaussian detector
 - Difference-of-Gaussian detector
 - Combinations
- Local Descriptors
 - Orientation normalization
 - SIFT

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From Points to Regions...

- The Harris and Hessian operators define interest points.
 - Precise localization
 - High repeatability



- In order to compare those points, we need to compute a descriptor over a region.
 - How can we define such a region in a scale invariant manner?
- i.e. how can we detect scale invariant interest regions?*

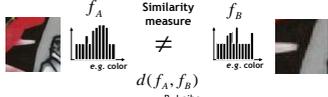
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Naïve Approach: Exhaustive Search

- Multi-scale procedure
 - Compare descriptors while varying the patch size

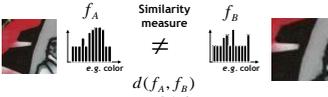
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Naïve Approach: Exhaustive Search

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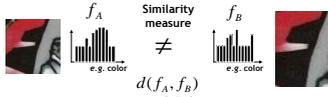
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Naïve Approach: Exhaustive Search

- Multi-scale procedure
 - Compare descriptors while varying the patch size

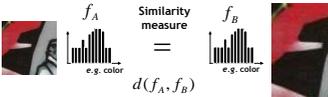
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Naïve Approach: Exhaustive Search

- Multi-scale procedure
 - Compare descriptors while varying the patch size

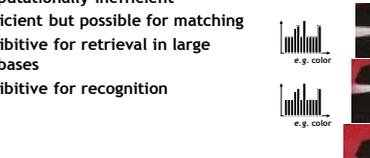
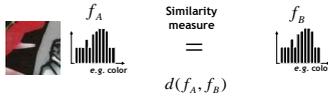
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Naïve Approach: Exhaustive Search

- Comparing descriptors while varying the patch size
 - Computationally inefficient
 - Inefficient but possible for matching
 - Prohibitive for retrieval in large databases
 - Prohibitive for recognition

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Automatic Scale Selection

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- **Solution:**
 - Design a function on the region, which is “scale invariant” (the same for corresponding regions, even if they are at different scales)

Example: average intensity. For corresponding regions (even of different sizes) it will be the same.

- For a point in one image, we can consider it as a function of region size (patch width)

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Automatic Scale Selection

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- **Common approach:**
 - Take a local maximum of this function.
 - Observation: region size for which the maximum is achieved should be *invariant* to image scale.

Important: this scale invariant region size is found in each image **independently!**

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Automatic Scale Selection

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- **Function responses for increasing scale (scale signature)**

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Automatic Scale Selection

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- **Function responses for increasing scale (scale signature)**

Slide credit: Krystian Mikolajczyk

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- **Function responses for increasing scale (scale signature)**

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Automatic Scale Selection

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- **Function responses for increasing scale (scale signature)**

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Automatic Scale Selection

- Function responses for increasing scale (scale signature)

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Automatic Scale Selection

- Function responses for increasing scale (scale signature)

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Automatic Scale Selection

- Normalize: Rescale to fixed size

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Slide credit: Tinne Tuytelaars

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What Is A Useful Signature Function?

- Laplacian-of-Gaussian = "blob" detector

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Characteristic Scale

- We define the *characteristic scale* as the scale that produces peak of Laplacian response

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Laplacian-of-Gaussian (LoG)

- Interest points:
 - Local maxima in scale space of Laplacian-of-Gaussian

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Slide adapted from Krystian Mikolajczyk

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Laplacian-of-Gaussian (LoG)

• Interest points:

- Local maxima in scale space of Laplacian-of-Gaussian

$L_{x1}(\sigma) + L_{y1}(\sigma)$

σ^4
 σ^3
 σ^2
 σ

Scale

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Laplacian-of-Gaussian (LoG)

• Interest points:

- Local maxima in scale space of Laplacian-of-Gaussian

$L_{x1}(\sigma) + L_{y1}(\sigma)$

σ^4
 σ^3
 σ^2
 σ

Scale

Slide adapted from Krystian Mikolajczyk B. Leibe

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Laplacian-of-Gaussian (LoG)

• Interest points:

- Local maxima in scale space of Laplacian-of-Gaussian

$L_{x1}(\sigma) + L_{y1}(\sigma)$

σ^4
 σ^3
 σ^2
 σ

Scale

⇒ List of (x, y, σ)

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LoG Detector: Workflow



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LoG Detector: Workflow



sigma = 11.9912

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LoG Detector: Workflow



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Technical Detail

- We can efficiently approximate the Laplacian with a difference of Gaussians:

$$L = \sigma^2 (G_{xx}(x, y, \sigma) + G_{yy}(x, y, \sigma))$$

(Laplacian)

$$DoG = G(x, y, k\sigma) - G(x, y, \sigma)$$

(Difference of Gaussians)

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Difference-of-Gaussian (DoG)

- Difference of Gaussians as approximation of the LoG
 - This is used e.g. in Lowe's SIFT pipeline for feature detection.
- Advantages
 - No need to compute 2nd derivatives
 - Gaussians are computed anyway, e.g. in a Gaussian pyramid.

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Key point localization with DoG

- Detect maxima of difference-of-Gaussian (DoG) in scale space
- Then reject points with low contrast (threshold)
- Eliminate edge responses

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DoG - Efficient Computation

- Computation in Gaussian scale pyramid

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Results: Lowe's DoG

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Example of Keypoint Detection

- (a) 233x189 image
- (b) 832 DoG extrema
- (c) 729 left after peak value threshold
- (d) 536 left after testing ratio of principle curvatures (removing edge responses)

Slide credit: David Lowe

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Harris-Laplace [Mikolajczyk '01]

1. Initialization: Multiscale Harris corner detection

Computing Harris function Detecting local maxima 93

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Harris-Laplace [Mikolajczyk '01]

1. Initialization: Multiscale Harris corner detection
2. Scale selection based on Laplacian (same procedure with Hessian \Rightarrow Hessian-Laplace)

Harris points

Harris-Laplace points

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Summary: Scale Invariant Detection

- **Given:** Two images of the same scene with a large *scale difference* between them.
- **Goal:** Find the *same* interest points *independently* in each image.
- **Solution:** Search for *maxima* of suitable functions in *scale* and in *space* (over the image).
- Two strategies
 - Laplacian-of-Gaussian (LoG)
 - Difference-of-Gaussian (DoG) as a fast approximation
 - *These can be used either on their own, or in combinations with single-scale keypoint detectors (Harris, Hessian).*

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You Can Try It At Home...

- For most local feature detectors, executables are available online:
- <http://robots.ox.ac.uk/~vgg/research/affine>
- <http://www.cs.ubc.ca/~lowe/keypoints/>
- <http://www.vision.ee.ethz.ch/~surf>
- <http://homes.esat.kuleuven.be/~ncorneli/gpusurf/>

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Affine Covariant Features

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Affine Covariant Region Detectors

Parameters defining an affine region

Code

Lines features	Example of use	Displaying
Hough & Hough-affine	<code>python3 -f3_affine.py -image1 10 -image2 10 -img1 2000 -img2 5000 -out 1000</code>	<code>img1 2000</code>
MORF - Minutely stable interest region (also Windows)	<code>python3 -f4_morf.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f5_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f6_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f7_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f8_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f9_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f10_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f11_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f12_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f13_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f14_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f15_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f16_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f17_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f18_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f19_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f20_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f21_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f22_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f23_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f24_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f25_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f26_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f27_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f28_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f29_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f30_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f31_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f32_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f33_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f34_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f35_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f36_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f37_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f38_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f39_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f40_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f41_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f42_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f43_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f44_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f45_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f46_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f47_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f48_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f49_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>
MSZ - Minutely stable interest region (also Windows)	<code>python3 -f50_msz.py -s 1 -m 2 -l 1000,1000 -o img1.png</code>	<code>img1 1000</code>

<http://www.robots.ox.ac.uk/~vgg/research/affine/detectors.html#binaries>

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References and Further Reading

- Read David Lowe's SIFT paper
 - D. Lowe, [Distinctive image features from scale-invariant keypoints](#), *IJCV* 60(2), pp. 91-110, 2004
- Good survey paper on Int. Pt. detectors and descriptors
 - T. Tuytelaars, K. Mikolajczyk, [Local Invariant Feature Detectors: A Survey](#), *Foundations and Trends in Computer Graphics and Vision*, Vol. 3, No. 3, pp 177-280, 2008.
- Try the example code, binaries, and Matlab wrappers
 - Good starting point: [Oxford interest point page](#) <http://www.robots.ox.ac.uk/~vgg/research/affine/detectors.html#binaries>