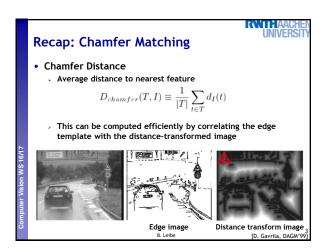
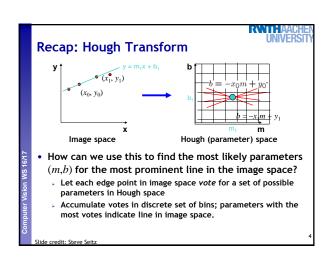
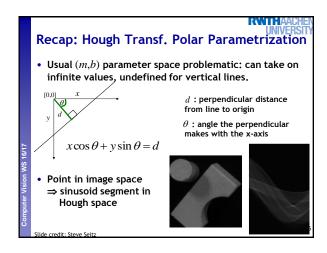
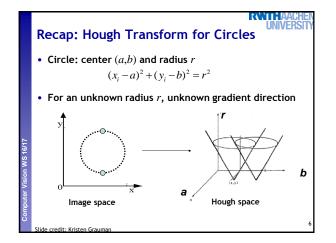
Computer Vision - Lecture 6 Segmentation 09.11.2016 Bastian Leibe RWTH Aachen http://www.vision.rwth-aachen.de

Course Outline Image Processing Basics Structure Extraction Segmentation Segmentation as Clustering Graph-theoretic Segmentation Recognition Global Representations Subspace representations Local Features & Matching Object Categorization 3D Reconstruction

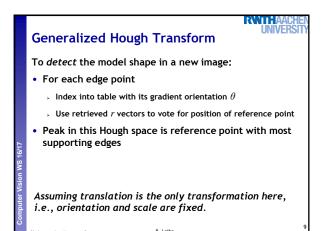


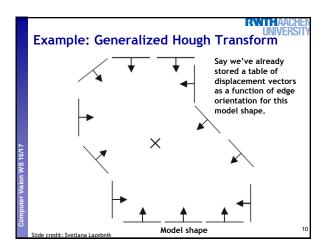


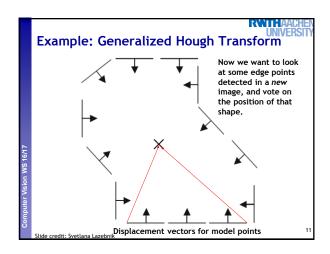


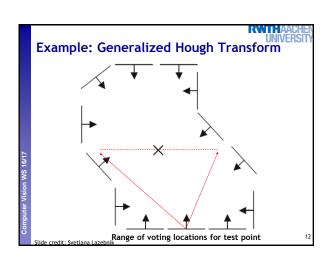


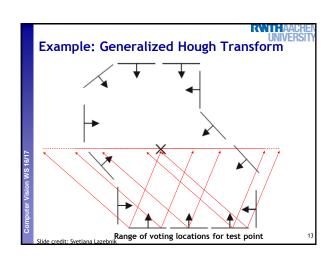
Generalized Hough Transform • What if we want to detect arbitrary shapes defined by boundary points and a reference point? At each boundary point, compute displacement vector: $\mathbf{r} = a - p_i$. For a given model shape: store these vectors in a table indexed by gradient orientation θ . [Dana H. Ballard, Generalizing the Hough Transform to Detect Arbitrary Shapes, 1980]

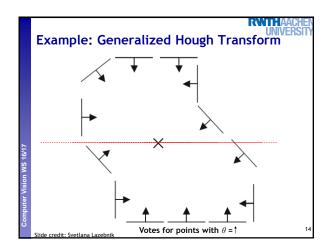


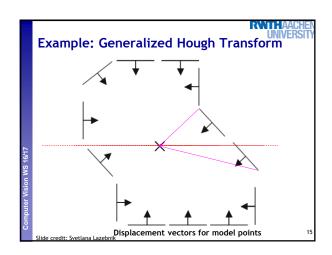


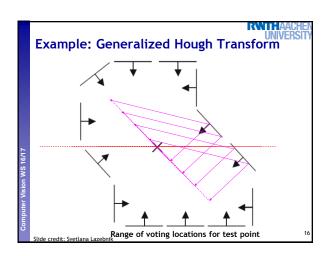


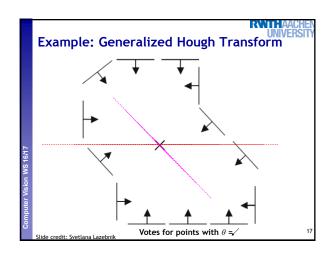


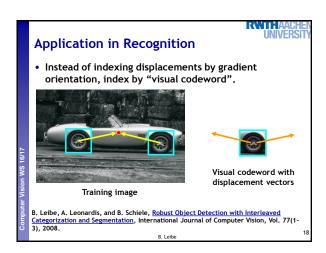


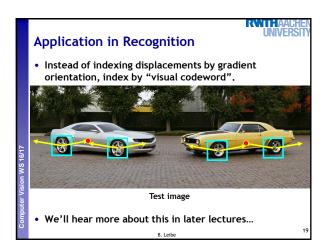


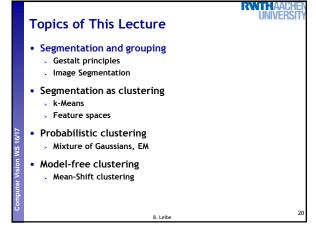


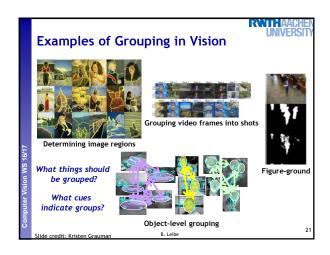


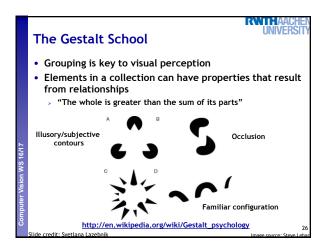


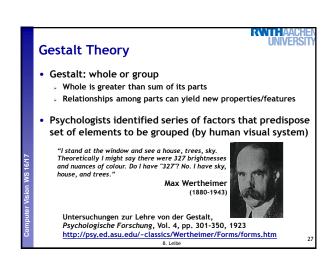


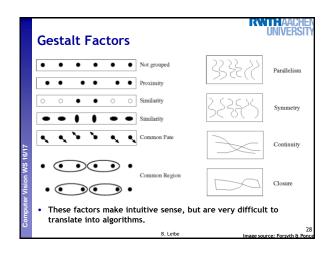


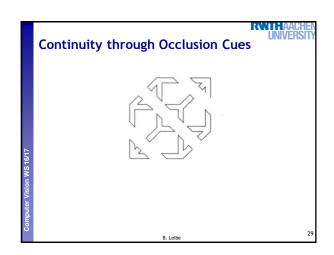


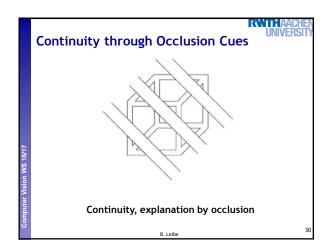


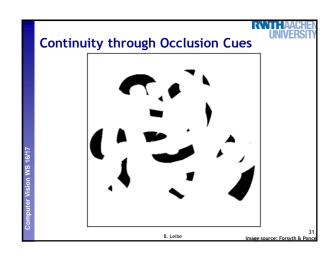


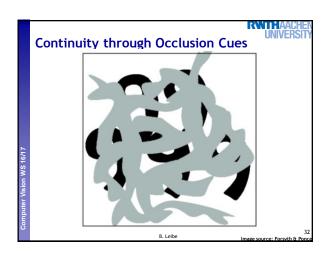


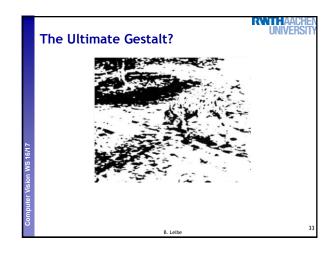


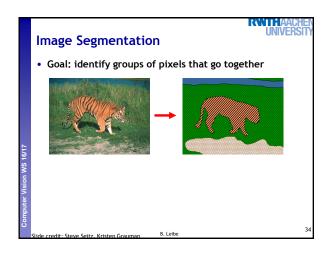


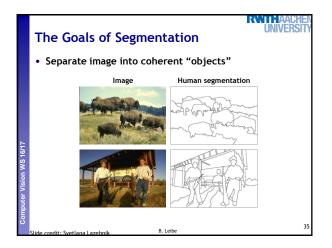


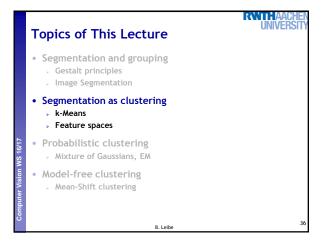


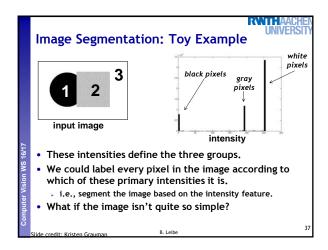


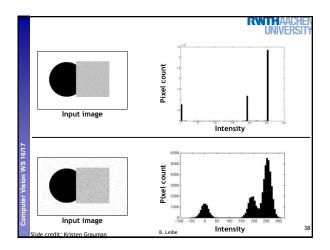


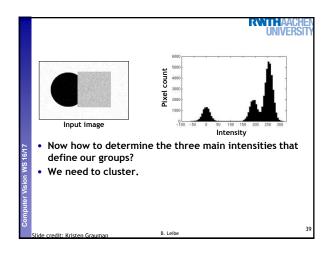


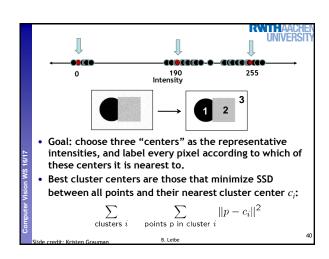


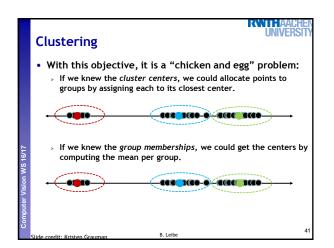


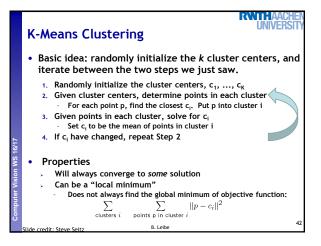


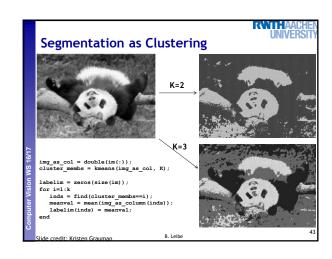


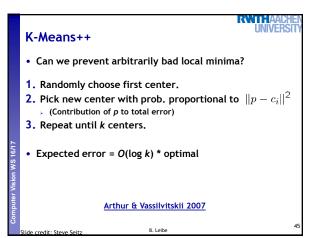


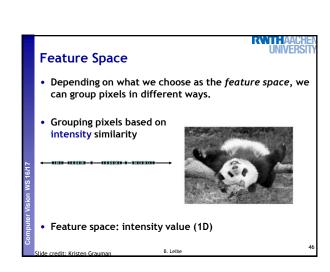


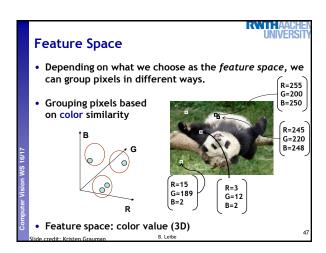


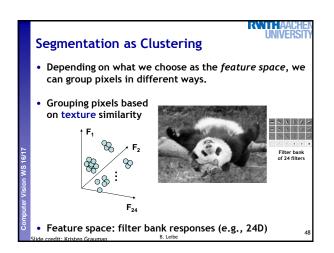


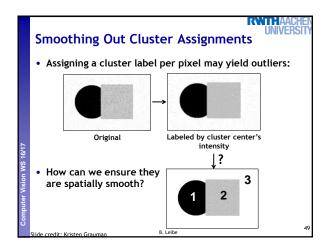


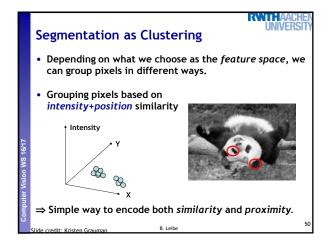


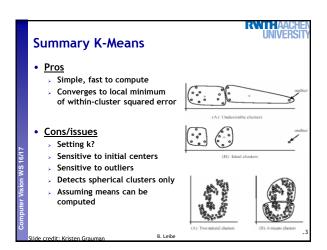


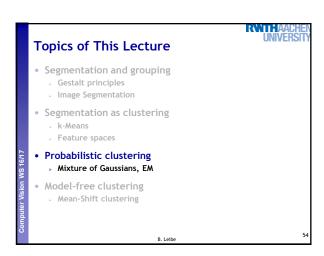


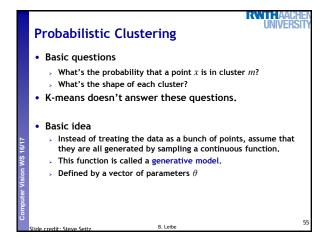


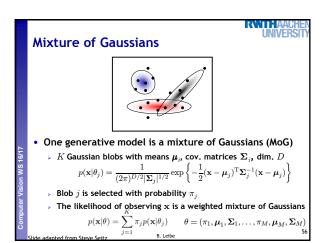




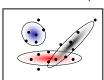








Expectation Maximization (EM)



Goal

 \succ Find blob parameters θ that maximize the likelihood function:

$$p(data|\theta) = \prod^{N} p(\mathbf{x}_n|\theta)$$

- 1. E-step: given current guess of blobs, compute ownership of each point
- 2. M-step: given ownership probabilities, update blobs to maximize likelihood function
- 3. Repeat until convergence

EM Algorithm

- · Expectation-Maximization (EM) Algorithm
 - E-Step: softly assign samples to mixture components

$$\gamma_{j}(\mathbf{x}_{n}) \leftarrow \frac{\pi_{j} \mathcal{N}(\mathbf{x}_{n} | \boldsymbol{\mu}_{j}, \boldsymbol{\Sigma}_{j})}{\sum_{k=1}^{K} \pi_{k} \mathcal{N}(\mathbf{x}_{n} | \boldsymbol{\mu}_{k}, \boldsymbol{\Sigma}_{k})} \quad \forall j = 1, \dots, K, \quad n = 1, \dots, N$$
Step: rescripted the parameters (separately for each mixture)

M-Step: re-estimate the parameters (separately for each mixture component) based on the soft assignments

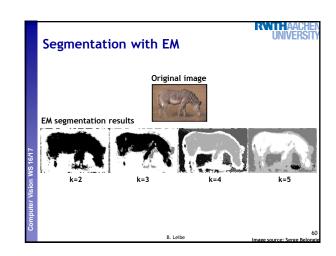
$$\hat{N}_j \leftarrow \sum_{n=1}^N \gamma_j(\mathbf{x}_n) = \text{soft number of samples labeled } j$$

$$\hat{\pi}_{j}^{\text{new}} \leftarrow \frac{\hat{N}_{j}}{N}$$

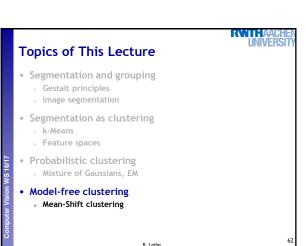
$$\hat{\mu}_{j}^{\text{new}} \leftarrow \frac{1}{\hat{N}_{j}} \sum_{n=1}^{N} \gamma_{j}(\mathbf{x}_{n}) \mathbf{x}_{n}$$

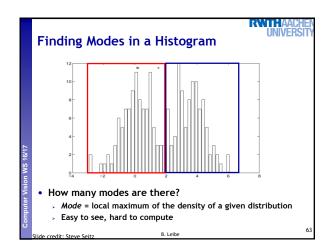
$$\begin{split} \hat{\mu}_{j}^{\text{new}} &\leftarrow \frac{1}{\hat{N}_{j}} \sum_{n=1}^{N} \gamma_{j}(\mathbf{x}_{n}) \mathbf{x}_{n} \\ \hat{\Sigma}_{j}^{\text{new}} &\leftarrow \frac{1}{\hat{N}_{j}} \sum_{n=1}^{N} \gamma_{j}(\mathbf{x}_{n}) (\mathbf{x}_{n} - \hat{\mu}_{j}^{\text{new}}) (\mathbf{x}_{n} - \hat{\mu}_{j}^{\text{new}})^{\text{T}} \\ &\text{om Bernt Schiele} \end{split}$$
B. Leibe

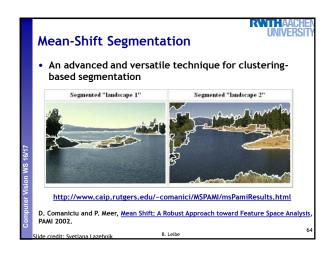
Applications of EM · Turns out this is useful for all sorts of problems > Any clustering problem > Any model estimation problem > Missing data problems > Finding outliers > Segmentation problems - Segmentation based on color - Segmentation based on motion - Foreground/background separation

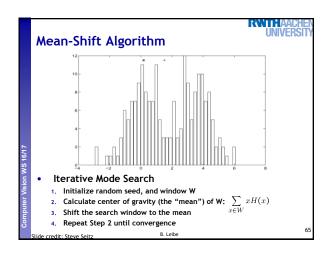


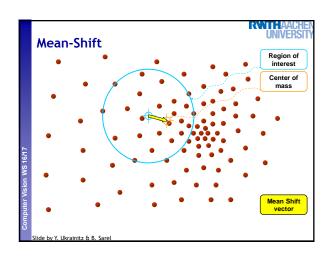
Summary: Mixtures of Gaussians, EM Pros > Probabilistic interpretation > Soft assignments between data points and clusters > Generative model, can predict novel data points > Relatively compact storage Cons Local minima - k-means is NP-hard even with k=2 Initialization Often a good idea to start with some k-means iterations. Need to know number of components Solutions: model selection (AIC, BIC), Dirichlet process mixture Need to choose generative model > Numerical problems are often a nuisance B. Leibe

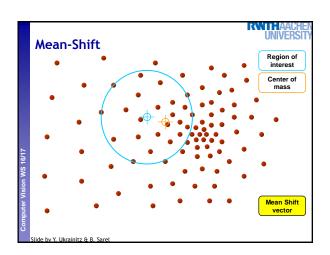


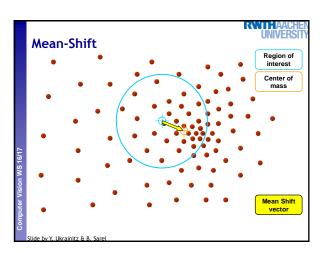


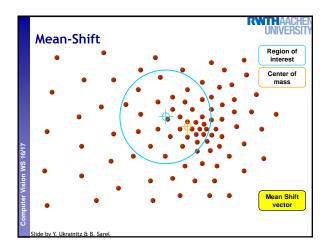


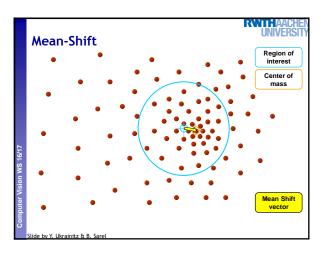


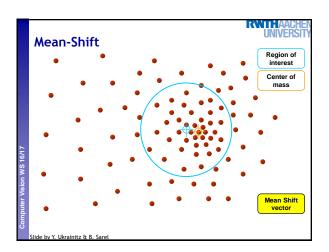


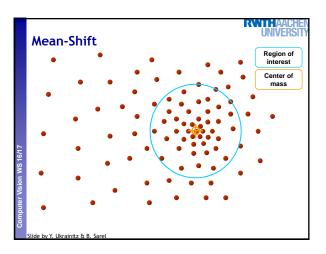


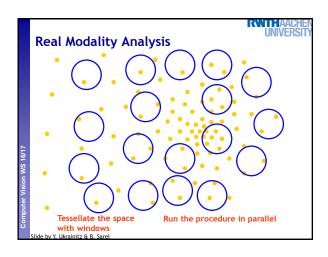


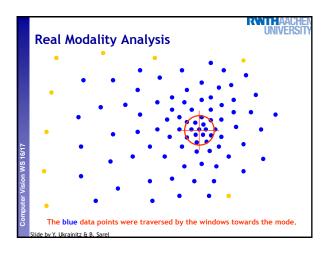


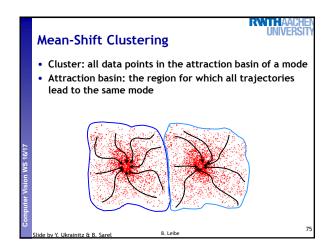


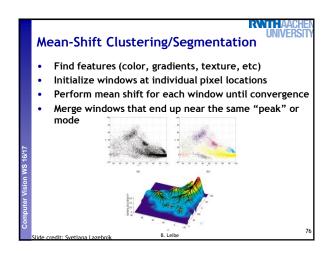


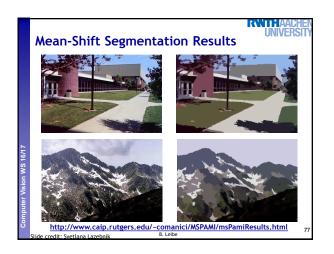


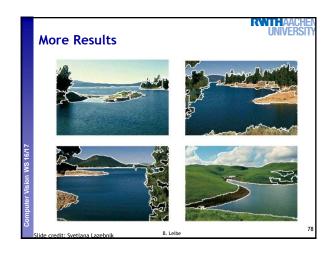


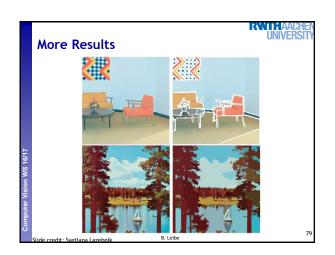


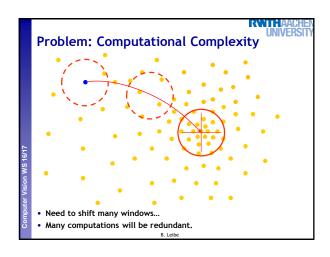


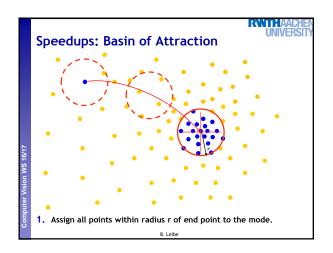


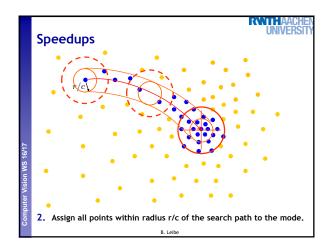




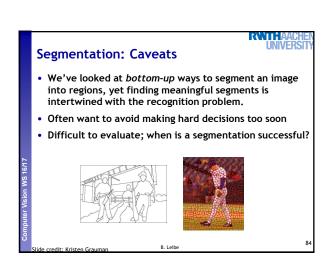








Pros General, application-independent tool Model-free, does not assume any prior shape (spherical, elliptical, etc.) on data clusters Just a single parameter (window size h) h has a physical meaning (unlike k-means) Finds variable number of modes Robust to outliers Cons Output depends on window size Window size (bandwidth) selection is not trivial Computationally (relatively) expensive (-2s/image) Does not scale well with dimension of feature space



Generic Clustering • We have focused on ways to group pixels into image segments based on their appearance • Find groups; "quantize" feature space • In general, we can use clustering techniques to find groups of similar "tokens", provided we know how to compare the tokens. • E.g., segment an image into the types of motions present • E.g., segment a video into the types of scenes (shots) present

