

# **Computer Vision - Lecture 19**

### **Uncalibrated Reconstruction**

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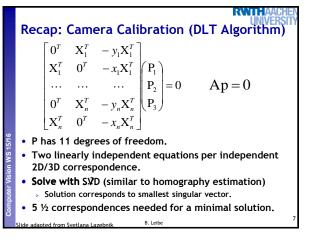
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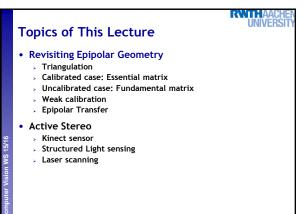
### **Course Outline**

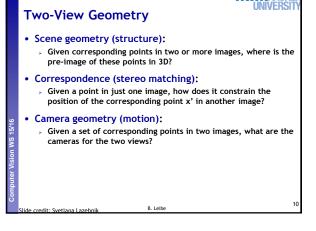
- Image Processing Basics
- · Segmentation & Grouping
- · Object Recognition
- · Local Features & Matching
- · Object Categorization
- 3D Reconstruction
  - Epipolar Geometry and Stereo Basics
  - > Camera calibration & Uncalibrated Reconstruction
  - > Active Stereo
  - > Structure-from-Motion
- Motion and Tracking

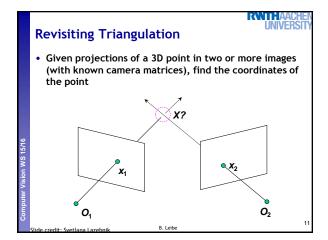
### Recap: Camera Parameters · Intrinsic parameters > Principal point coordinates $K = \begin{bmatrix} m_x & & \\ & m_y & \\ & & 1 \end{bmatrix} \begin{bmatrix} f & S & p_x \\ & f & p_y \\ & & 1 \end{bmatrix} =$ Focal length > Pixel magnification factors Skew (non-rectangular pixels) Radial distortion · Extrinsic parameters Rotation R Translation t (both relative to world coordinate system) Camera projection matrix P = K[R | t]⇒ General pinhole camera; ⇒ CCD Camera with square pixels: 10 DoF ⇒ General camera: 11 DoF

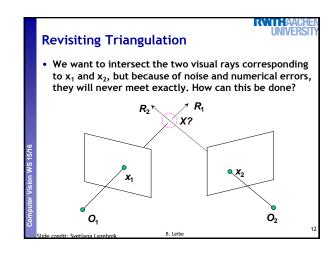
# Recap: Calibrating a Camera Goal Compute intrinsic and extrinsic parameters using observed camera data. Main idea Place "calibration object" with known geometry in the scene Get correspondences Solve for mapping from scene to image: estimate P=P<sub>int</sub>P<sub>ext</sub>

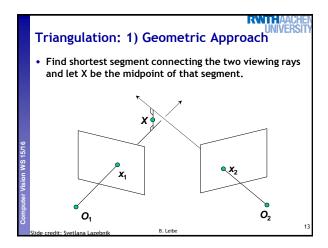


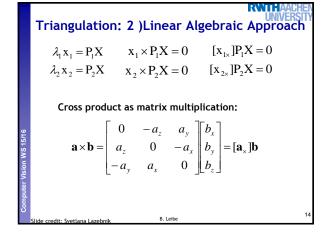




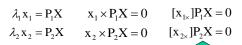








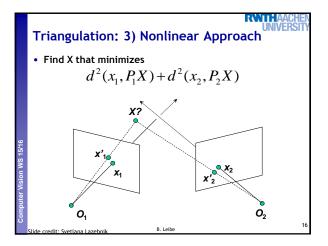
# Triangulation: 2) Linear Algebraic Approach



Two independent equations each in terms of three unknown entries of X

- ⇒ Stack them and solve using SVD!
- This approach is often preferable to the geometric approach, since it nicely generalizes to multiple cameras.

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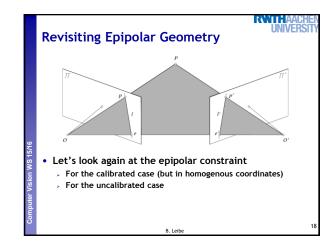
# Triangulation: 3) Nonlinear Approach

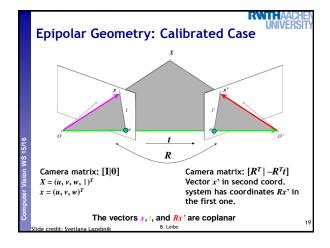
• Find X that minimizes

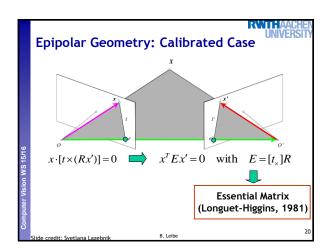
$$d^{2}(x_{1}, P_{1}X) + d^{2}(x_{2}, P_{2}X)$$

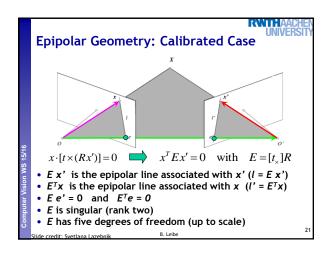
- This approach is the most accurate, but unlike the other two methods, it doesn't have a closed-form solution.
- · Iterative algorithm
  - > Initialize with linear estimate.
  - Optimize with Gauss-Newton or Levenberg-Marquardt (see F&P sec. 3.1.2 or H&Z Appendix 6).

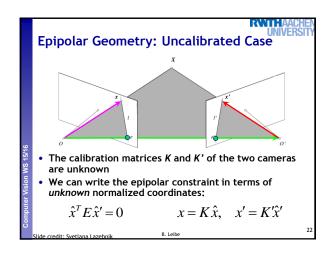
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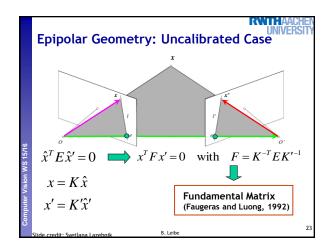


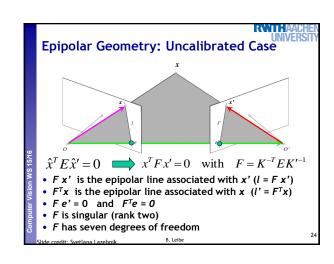


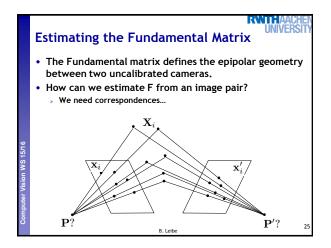


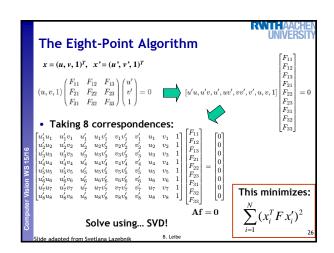












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### **Excursion: Properties of SVD**

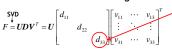
- Frobenius norm
  - > Generalization of the Euclidean norm to matrices

$$\left\| A \right\|_F = \sqrt{\sum_{i=1}^m \sum_{j=1}^n \left| a_{ij} \right|^2} \ = \sqrt{\sum_{i=1}^{\min(m,n)} \sigma_i^2}$$

- · Partial reconstruction property of SVD
  - Let  $\sigma_i$  i=1,...,N be the singular values of A.
  - . Let  $A_p = U_p D_p V_p^{\ T}$  be the reconstruction of A when we set  $\sigma_{p+1},...,\ \sigma_N$  to zero.
  - > Then  $A_p=U_pD_pV_p^{\ T}$  is the best rank-p approximation of A in the sense of the Frobenius norm
    - (i.e. the best least-squares approximation).

## The Eight-Point Algorithm

- Problem with noisy data
  - > The solution will usually not fulfill the constraint that F only has rank 2.
  - $\Rightarrow$  There will be no epipoles through which all epipolar lines pass!
- Enforce the rank-2 constraint using SVD



Set d<sub>33</sub> to zero and reconstruct F

 As we have just seen, this provides the best leastsquares approximation to the rank-2 solution.

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### Problem with the Eight-Point Algorithm

· In practice, this often looks as follows:

$$\begin{bmatrix} u_1'u_1 & u_1'v_1 & u_1' & u_1v_1' & v_1v_1' & v_1' & u_1 & v_1 & 1 \\ u_2'u_2 & u_2'v_2 & u_2' & u_2v_2' & v_2v_2' & v_2' & u_2 & v_2 & 1 \\ u_3'u_3 & u_3'v_3 & u_3' & u_3v_3' & v_3v_3' & v_3 & u_3 & v_3 & 1 \\ v_4'u_4 & u_4'v_4 & u_4' & u_4v_4' & v_4v_4' & v_4' & v_4 & 1 \\ v_5'u_5 & u_5'v_5 & u_5' & v_5v_5' & v_5' & v_5 & v_5 & v_5 & 1 \\ u_6'u_6 & u_6'v_6 & u_6 & u_6v_6' & v_6' & v_6 & u_6 & v_6 & 1 \\ u_7'v_7 & u_7'v_7 & v_7' & v_7v_7' & v_7v_7' & v_7 & v_7 & 1 \\ u_8'u_8 & u_8'v_8 & u_8' & u_8v_8' & v_8' & v_8' & u_8 & v_8 & 1 \end{bmatrix} \begin{bmatrix} F_{11} \\ F_{12} \\ F_{21} \\ F_{22} \\ F_{31} \\ F_{31} \\ G_{32} \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

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# Problem with the Eight-Point Algorithm

· In practice, this often looks as follows:

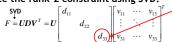
- ⇒ Poor numerical conditioning
  - $\Rightarrow$  Can be fixed by rescaling the data

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### RWTHAAL UNIVER The Normalized Eight-Point Algorithm

- Center the image data at the origin, and scale it so the mean squared distance between the origin and the data points is 2 pixels.
- 2. Use the eight-point algorithm to compute *F* from the normalized points.
- 3. Enforce the rank-2 constraint using SVD.



4. Transform fundamental matrix back to original units: if T and T' are the normalizing transformations in the two images, than the fundamental matrix in original coordinates is T<sup>T</sup>F T'.

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zero and econstruct F

# The Eight-Point Algorithm



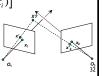
Sum of Euclidean distances between points  $x_i$  and epipolar lines  $Fx_i$  (or points  $x_i$  and epipolar lines  $F^Tx_i$ ), multiplied by a scale factor

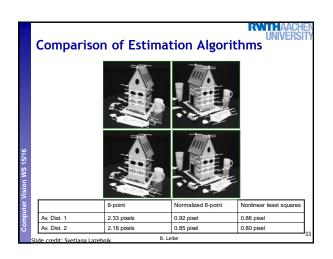
· Nonlinear approach: minimize

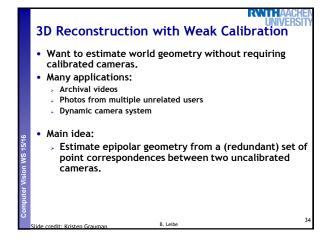
$$\sum_{i=1}^{N} \left[ d^{2}(x_{i}, F x_{i}') + d^{2}(x_{i}', F^{T} x_{i}) \right]$$

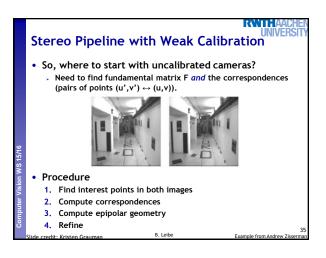
- Similar to nonlinear minimization approach for triangulation.
- Iterative approach (Gauss-Newton, Levenberg-Marquardt,...)

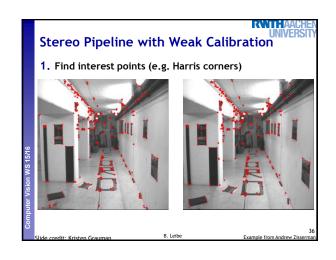
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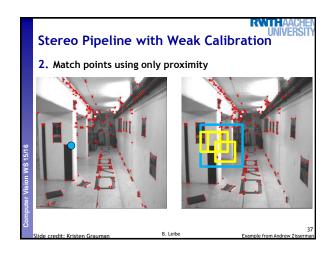


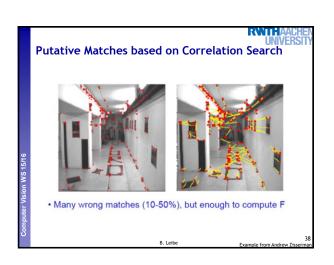


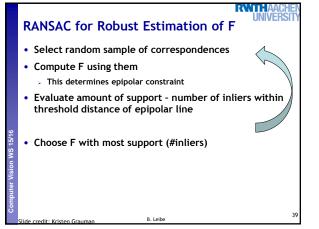


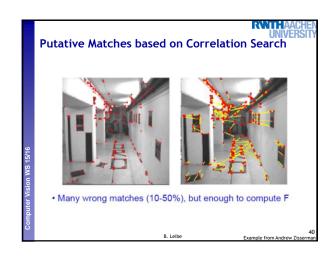


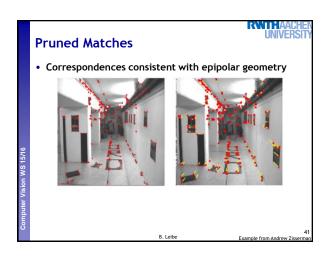


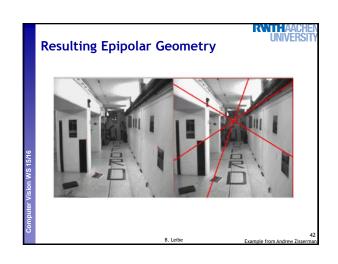


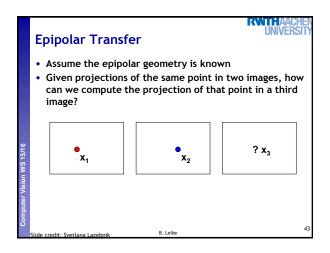


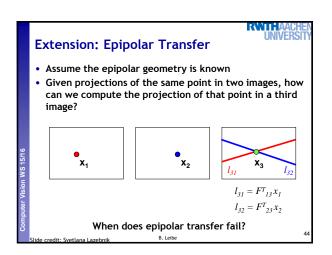


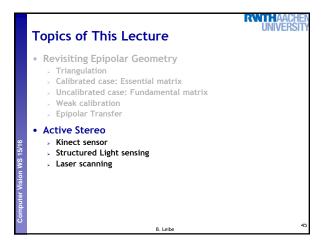




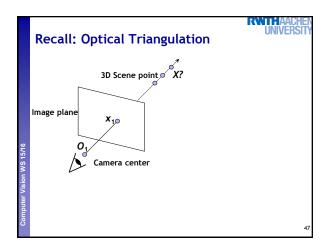


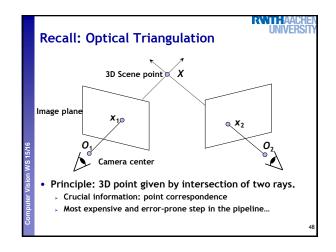


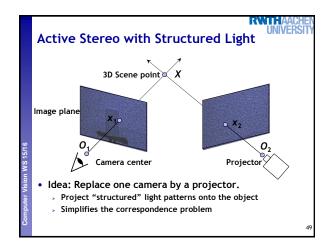


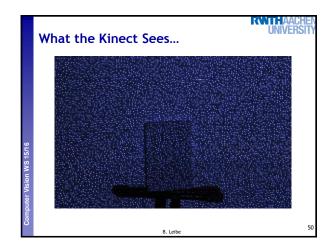


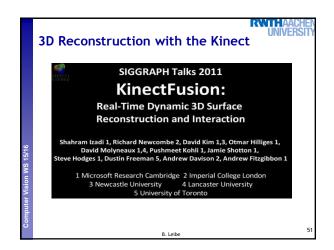


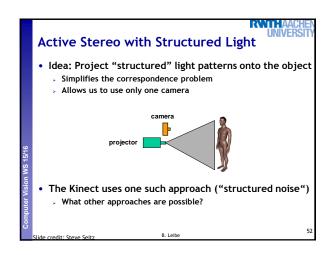


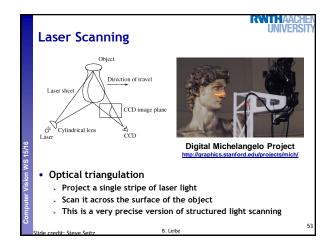


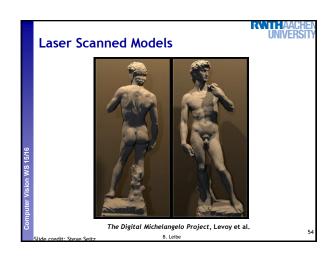


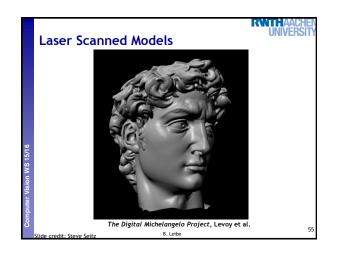


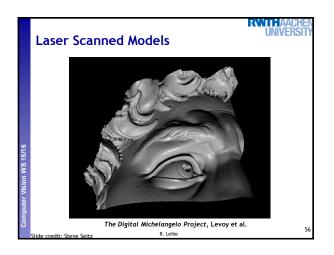


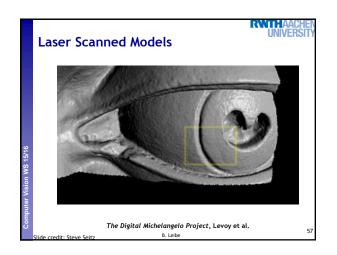


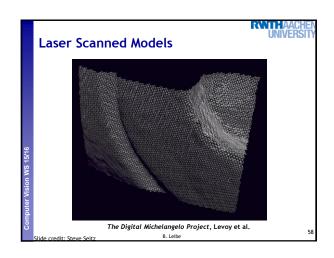


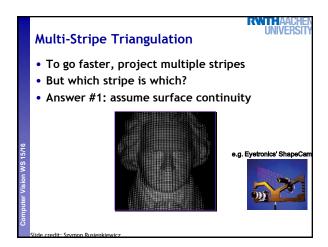


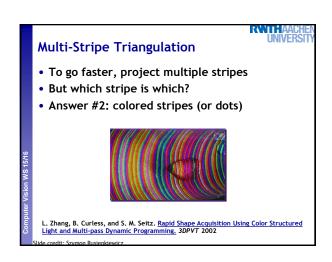


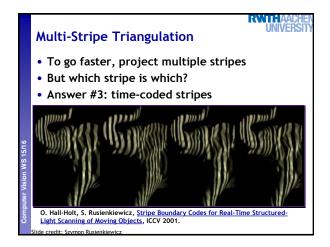


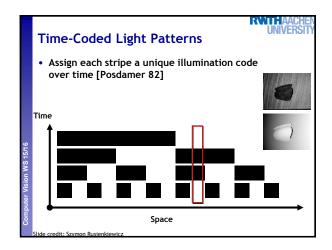


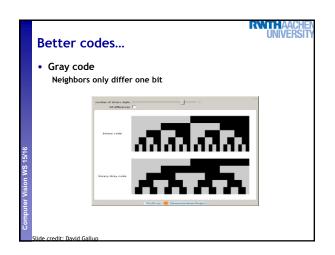


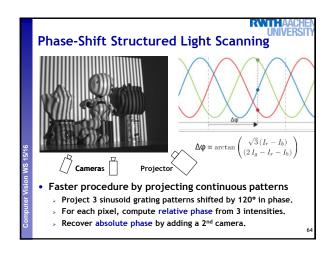


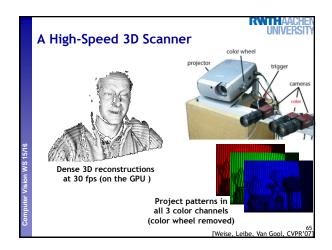


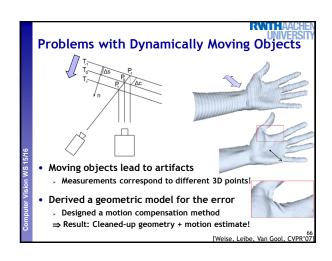


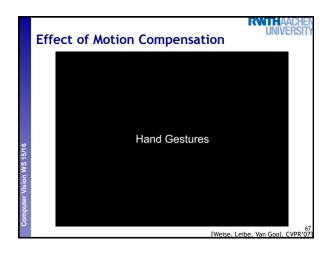


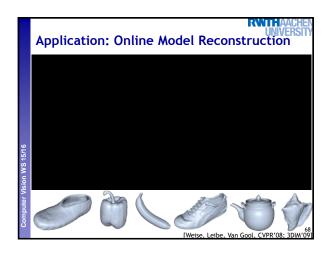


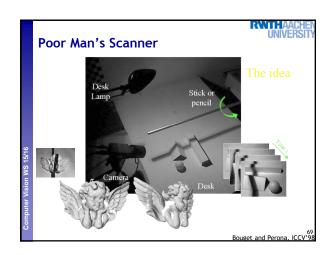














# References and Further Reading Background information on camera models and calibration algorithms can be found in Chapters 6 and 7 of R. Hartley, A. Zisserman Multiple View Geometry in Computer Vision 2nd Ed., Cambridge Univ. Press, 2004 Also recommended: Chapter 9 of the same book on Epipolar geometry and the Fundamental Matrix and Chapter 11.1-11.6 on automatic computation of F.

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