

Computer Vision - Lecture 15

Indexing and Visual Vocabularies

18.12.2014

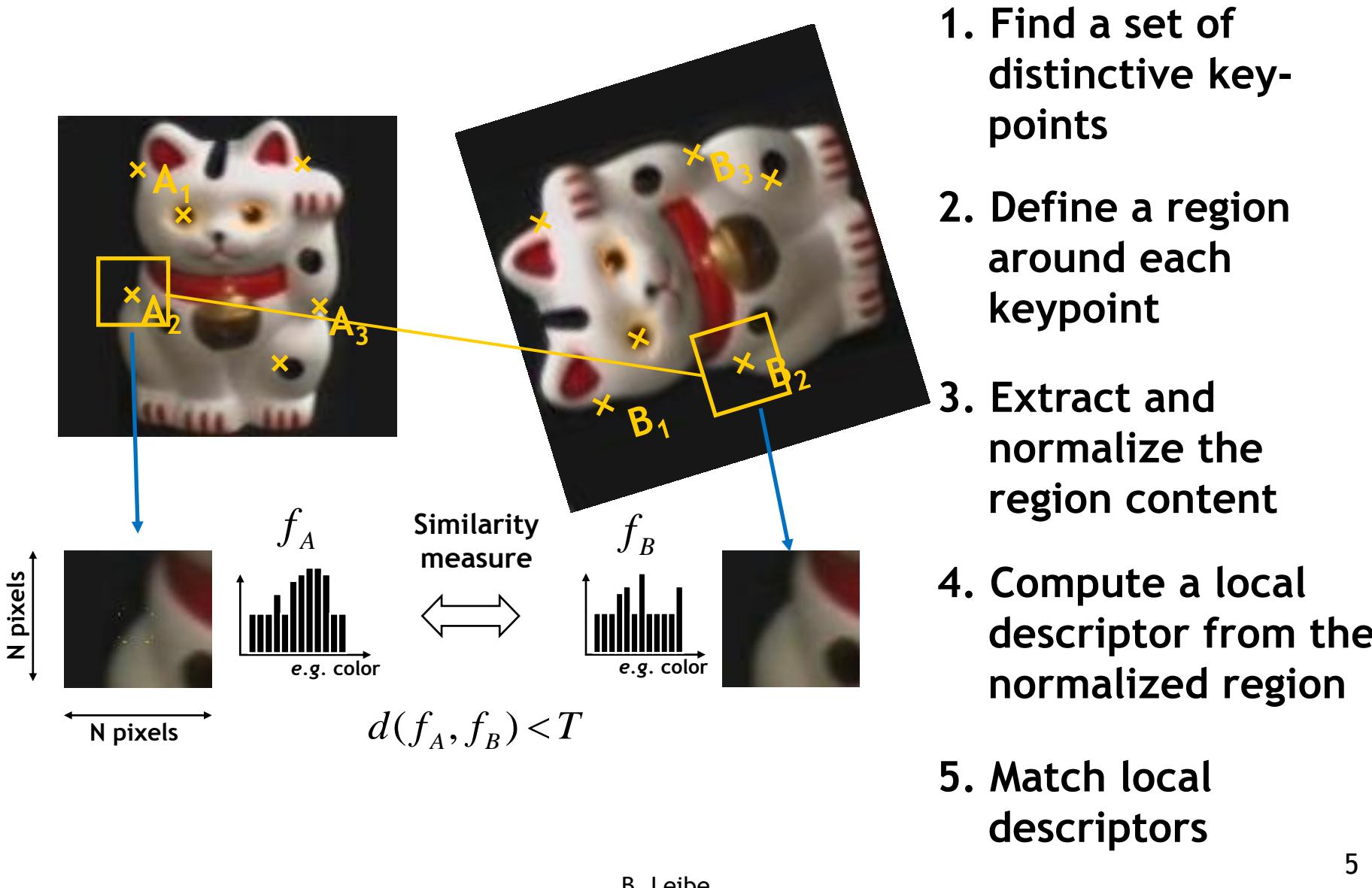
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Course Outline

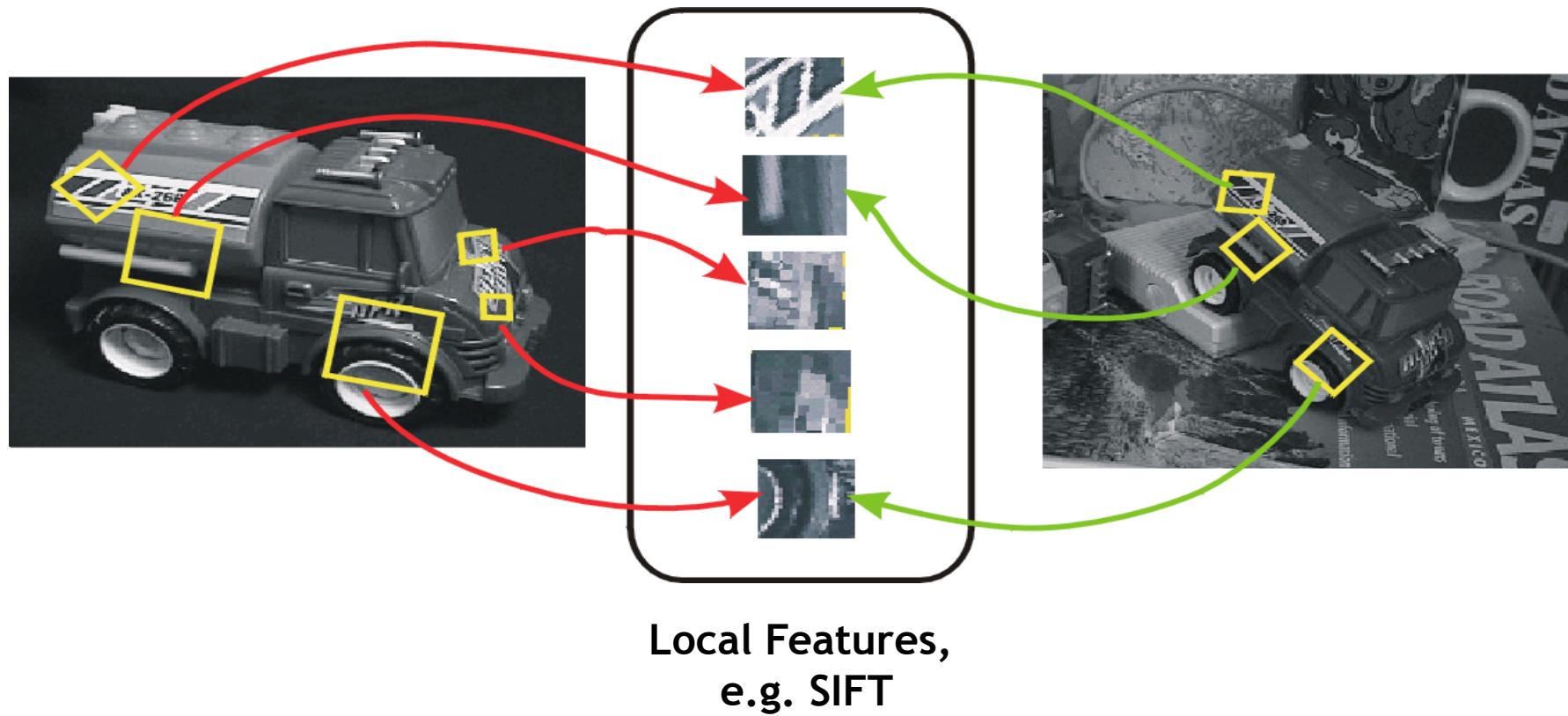
- **Image Processing Basics**
- **Segmentation & Grouping**
- **Object Recognition**
- **Object Categorization I**
 - Sliding Window based Object Detection
- **Local Features & Matching**
 - Local Features - Detection and Description
 - Recognition with Local Features
 - **Indexing & Visual Vocabularies**
- **Object Categorization II**
 - Bag-of-Words Approaches & Part-based Approaches
- **3D Reconstruction**

Recap: Local Feature Matching Outline



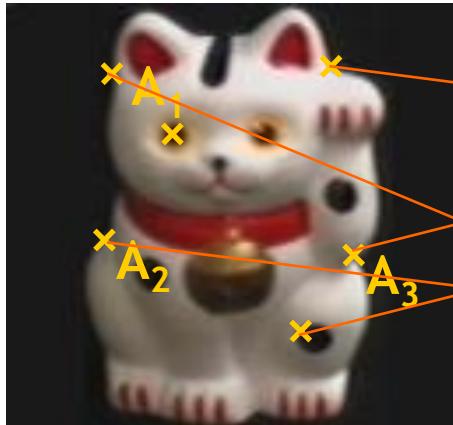
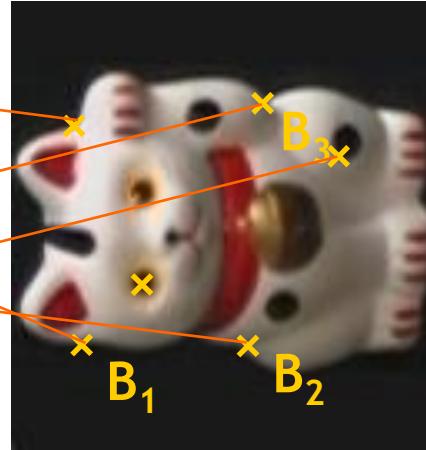
Recap: Recognition with Local Features

- Image content is transformed into local features that are invariant to translation, rotation, and scale
- Goal: Verify if they belong to a consistent configuration



Recap: Fitting an Affine Transformation

- Assuming we know the correspondences, how do we get the transformation?

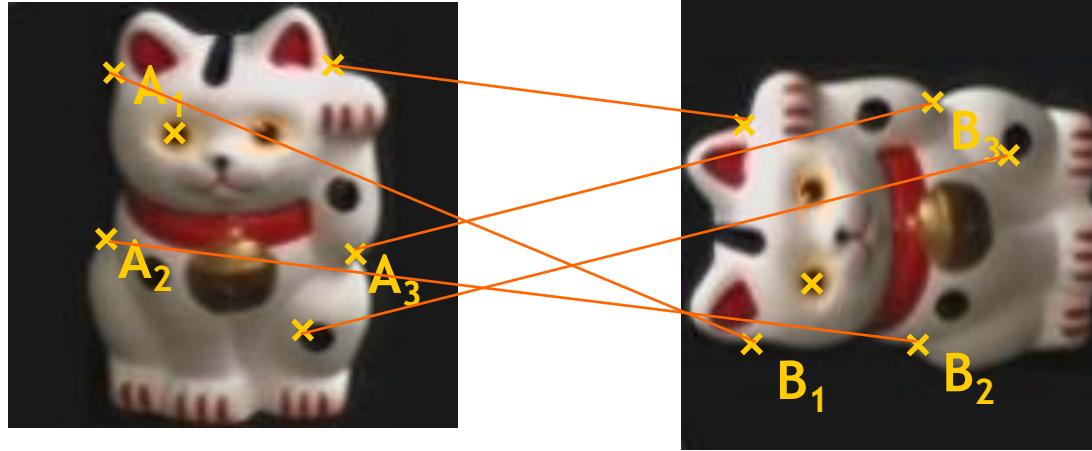
 (x_i, y_i)  (x'_i, y'_i)

$$\begin{bmatrix} x'_i \\ y'_i \end{bmatrix} = \begin{bmatrix} m_1 & m_2 \\ m_3 & m_4 \end{bmatrix} \begin{bmatrix} x_i \\ y_i \end{bmatrix} + \begin{bmatrix} t_1 \\ t_2 \end{bmatrix}$$

$$\begin{bmatrix} x_i & y_i & 0 & 0 & 1 & 0 \\ 0 & 0 & x_i & y_i & 0 & 1 \\ \dots & & & & & \end{bmatrix} \begin{bmatrix} m_1 \\ m_2 \\ m_3 \\ m_4 \\ t_1 \\ t_2 \end{bmatrix} = \begin{bmatrix} \dots \\ x'_i \\ y'_i \\ \dots \end{bmatrix}$$

Recap: Fitting a Homography

- Estimating the transformation



Homogenous coordinates

Image coordinates

$$\mathbf{x}_{A_1} \leftrightarrow \mathbf{x}_{B_1}$$

$$\mathbf{x}_{A_2} \leftrightarrow \mathbf{x}_{B_2}$$

$$\mathbf{x}_{A_3} \leftrightarrow \mathbf{x}_{B_3}$$

\vdots

$$\begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & 1 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$$x_{A_1} = \frac{h_{11} x_{B_1} + h_{12} y_{B_1} + h_{13}}{h_{31} x_{B_1} + h_{32} y_{B_1} + 1}$$

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$$\begin{bmatrix} x'' \\ y'' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & z' \end{bmatrix} \cdot \begin{bmatrix} x' \\ y' \\ z' \end{bmatrix}$$

$$y_{A_1} = \frac{h_{21} x_{B_1} + h_{22} y_{B_1} + h_{23}}{h_{31} x_{B_1} + h_{32} y_{B_1} + 1}$$

Matrix notation

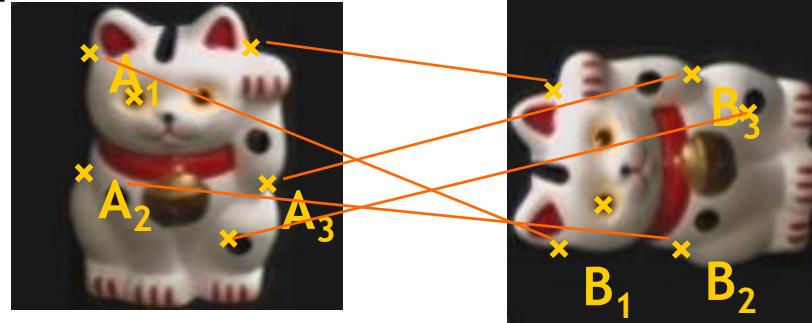
$$x' = Hx$$

$$x'' = \frac{1}{z'} x'$$

Recap: Fitting a Homography

- Estimating the transformation

$$\begin{aligned} h_{11}x_{B_1} + h_{12}y_{B_1} + h_{13} - x_{A_1}h_{31}x_{B_1} - x_{A_1}h_{32}y_{B_1} - x_{A_1} &= 0 \\ h_{21}x_{B_1} + h_{22}y_{B_1} + h_{23} - y_{A_1}h_{31}x_{B_1} - y_{A_1}h_{32}y_{B_1} - y_{A_1} &= 0 \end{aligned}$$



$$\mathbf{x}_{A_1} \leftrightarrow \mathbf{x}_{B_1}$$

$$\mathbf{x}_{A_2} \leftrightarrow \mathbf{x}_{B_2}$$

$$\mathbf{x}_{A_3} \leftrightarrow \mathbf{x}_{B_3}$$

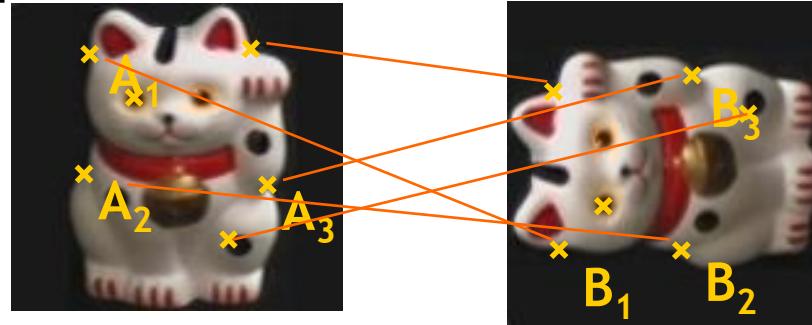
\vdots

$$\begin{bmatrix} x_{B_1} & y_{B_1} & 1 & 0 & 0 & 0 & -x_{A_1}x_{B_1} & -x_{A_1}y_{B_1} & -x_{A_1} \\ 0 & 0 & 0 & x_{B_1} & y_{B_1} & 1 & -y_{A_1}x_{B_1} & -y_{A_1}y_{B_1} & -y_{A_1} \\ \cdot & \cdot \\ \cdot & \cdot \\ \cdot & \cdot \end{bmatrix} \cdot \begin{bmatrix} h_{11} \\ h_{12} \\ h_{13} \\ h_{21} \\ h_{22} \\ h_{23} \\ h_{31} \\ h_{32} \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ \cdot \\ \cdot \\ \cdot \\ \cdot \\ \cdot \\ \cdot \end{bmatrix}$$

$$Ah = 0$$

Recap: Fitting a Homography

- Estimating the transformation
- Solution:
 - Null-space vector of \mathbf{A}
 - Corresponds to smallest eigenvector



SVD

$$\mathbf{A} = \mathbf{U} \mathbf{D} \mathbf{V}^T$$
$$Ah = 0$$
$$\begin{bmatrix} d_{11} & \cdots & d_{19} \\ \vdots & \ddots & \vdots \\ d_{91} & \cdots & d_{99} \end{bmatrix} \begin{bmatrix} v_{11} & \cdots & v_{19} \\ \vdots & \ddots & \vdots \\ v_{91} & \cdots & v_{99} \end{bmatrix}^T$$
$$\mathbf{h} = \frac{[v_{19}, \dots, v_{99}]}{v_{99}}$$

Minimizes least square error

Recap: Object Recognition by Alignment

- Assumption
 - Known object, rigid transformation compared to model image
⇒ *If we can find evidence for such a transformation, we have recognized the object.*
- You learned methods for
 - Fitting an **affine transformation** from ≥ 3 correspondences
 - Fitting a **homography** from ≥ 4 correspondences

Affine: solve a system

$$At = b$$

Homography: solve a system

$$Ah = 0$$

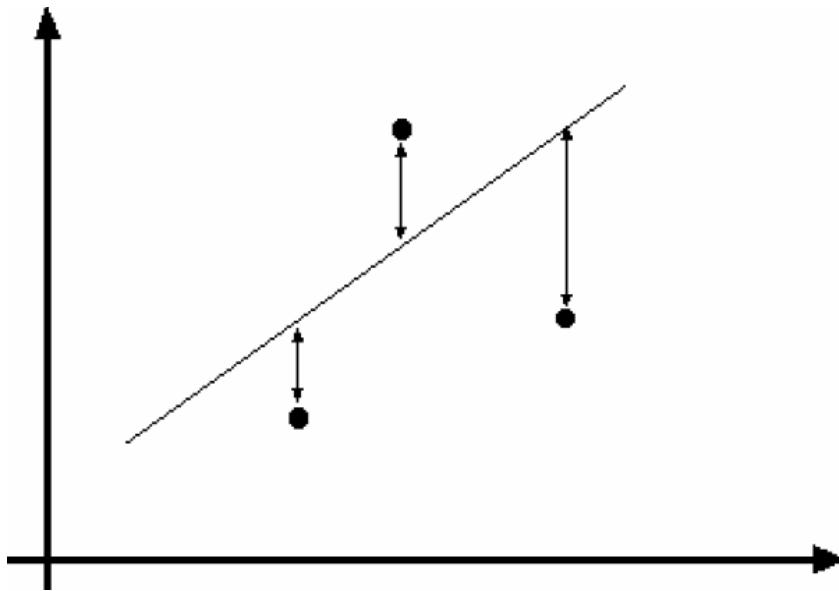
- Correspondences may be noisy and may contain outliers
⇒ Need to use robust methods that can filter out outliers

Topics of This Lecture

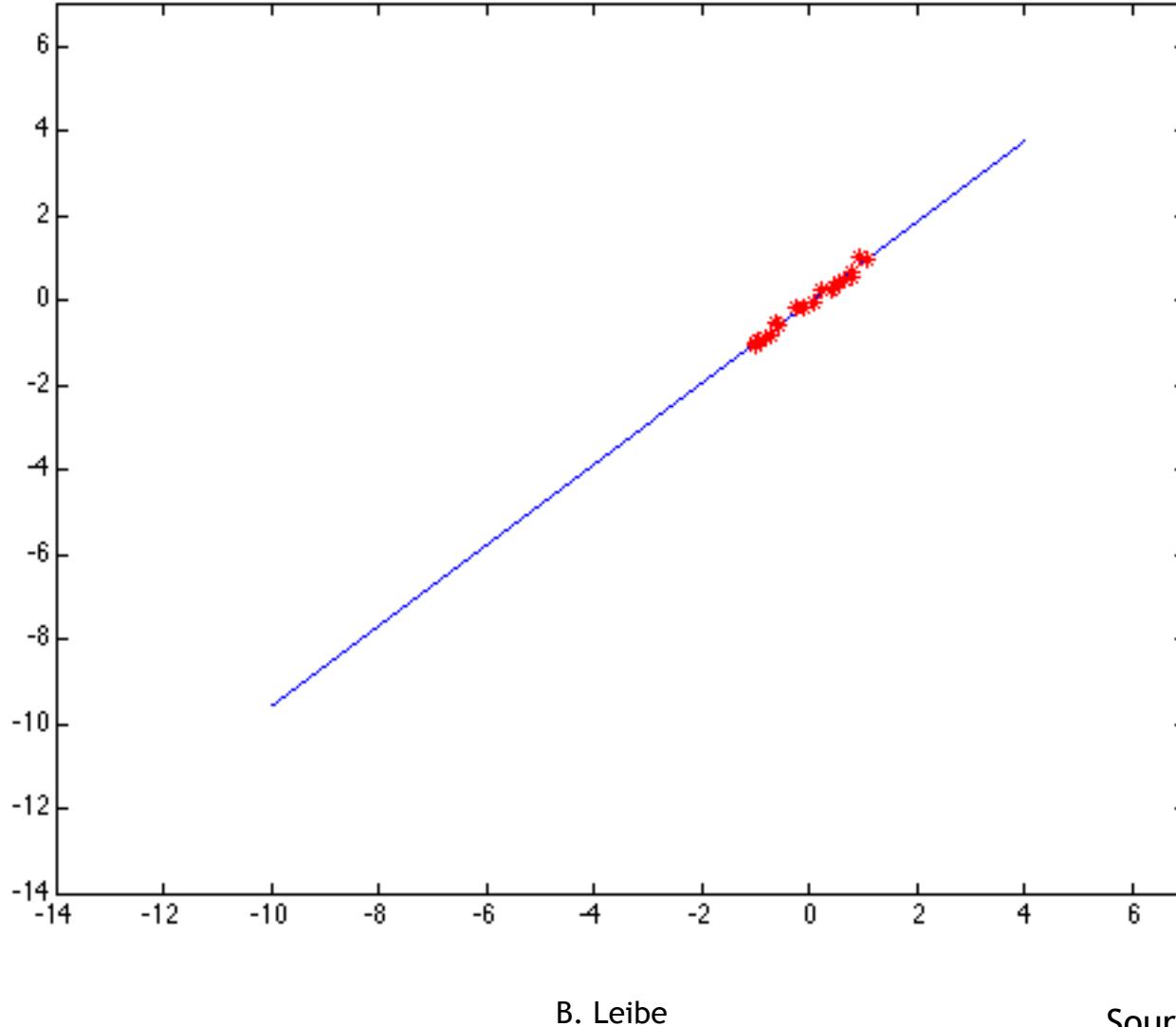
- **Dealing with Outliers**
 - RANSAC
 - Generalized Hough Transform
- **Indexing with Local Features**
 - Inverted file index
 - Visual Vocabularies
- **Bag-of-Words Model**
 - Use for image classification

Example: Least-Squares Line Fitting

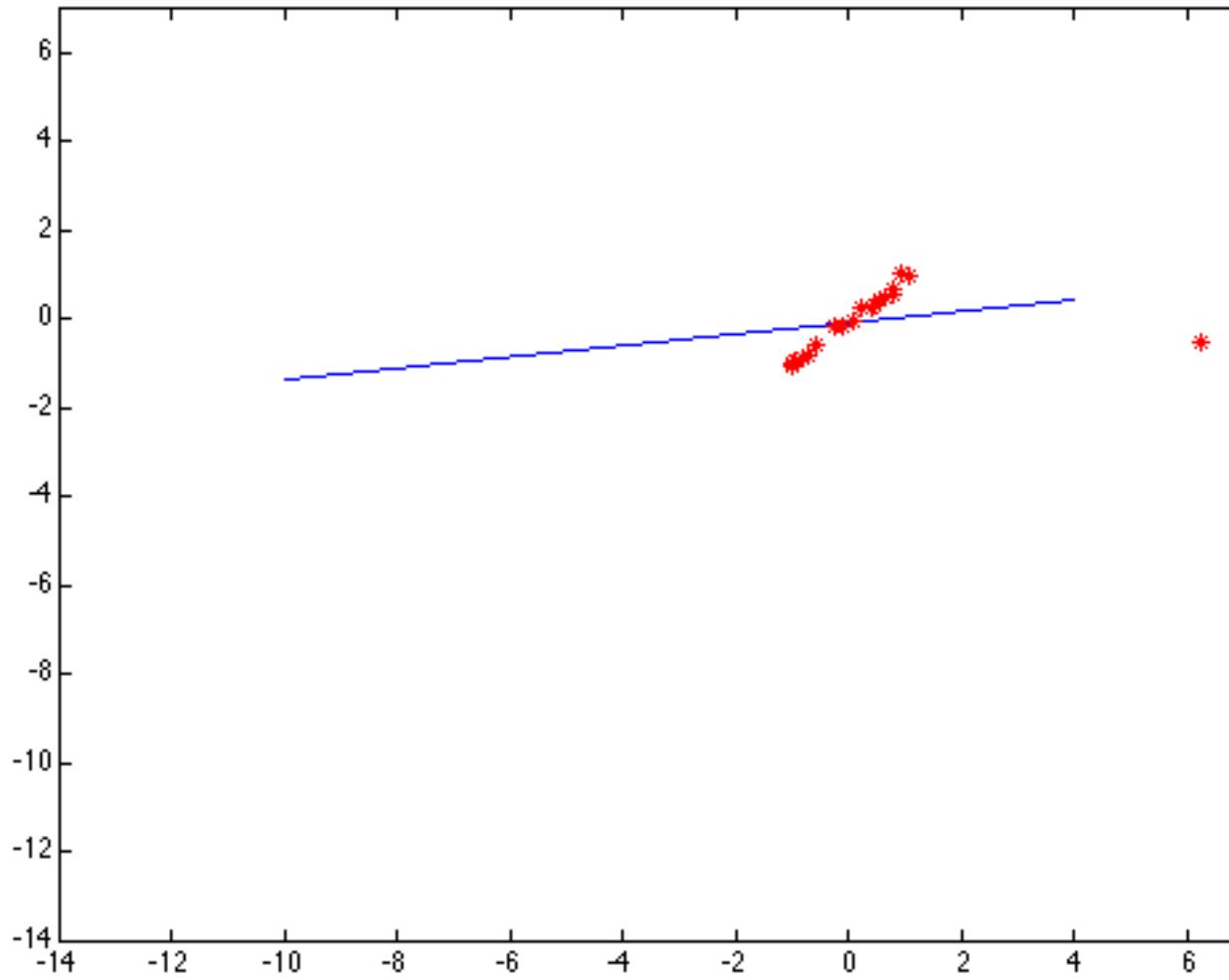
- Assuming all the points that belong to a particular line are known



Outliers Affect Least-Squares Fit



Outliers Affect Least-Squares Fit



Strategy 1: RANSAC [Fischler81]

- **RAN**dom **S**Ample **C**onsensus
- Approach: we want to avoid the impact of outliers, so let's look for “inliers”, and use only those.
- Intuition: if an outlier is chosen to compute the current fit, then the resulting line won't have much support from rest of the points.

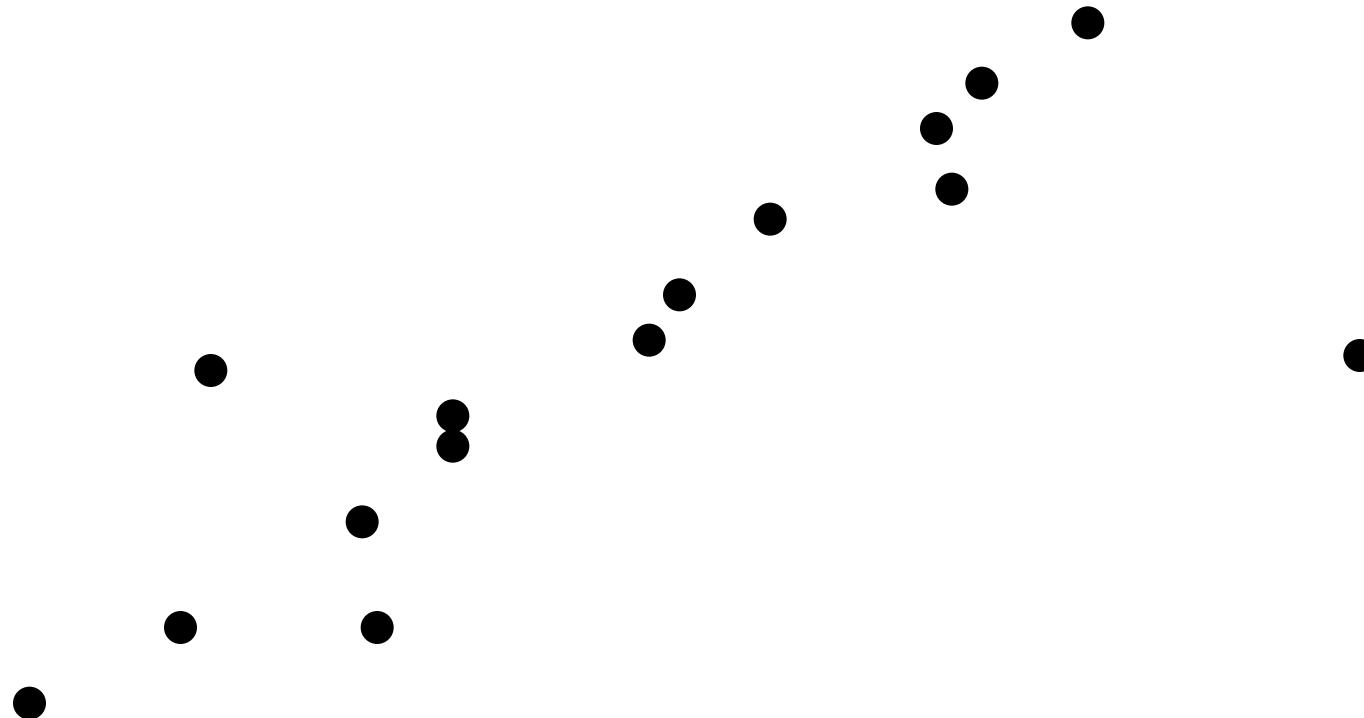
RANSAC

RANSAC loop:

1. Randomly select a *seed group* of points on which to base transformation estimate (e.g., a group of matches)
 2. Compute transformation from seed group
 3. Find *inliers* to this transformation
 4. If the number of inliers is sufficiently large, recompute least-squares estimate of transformation on all of the inliers
- Keep the transformation with the largest number of inliers

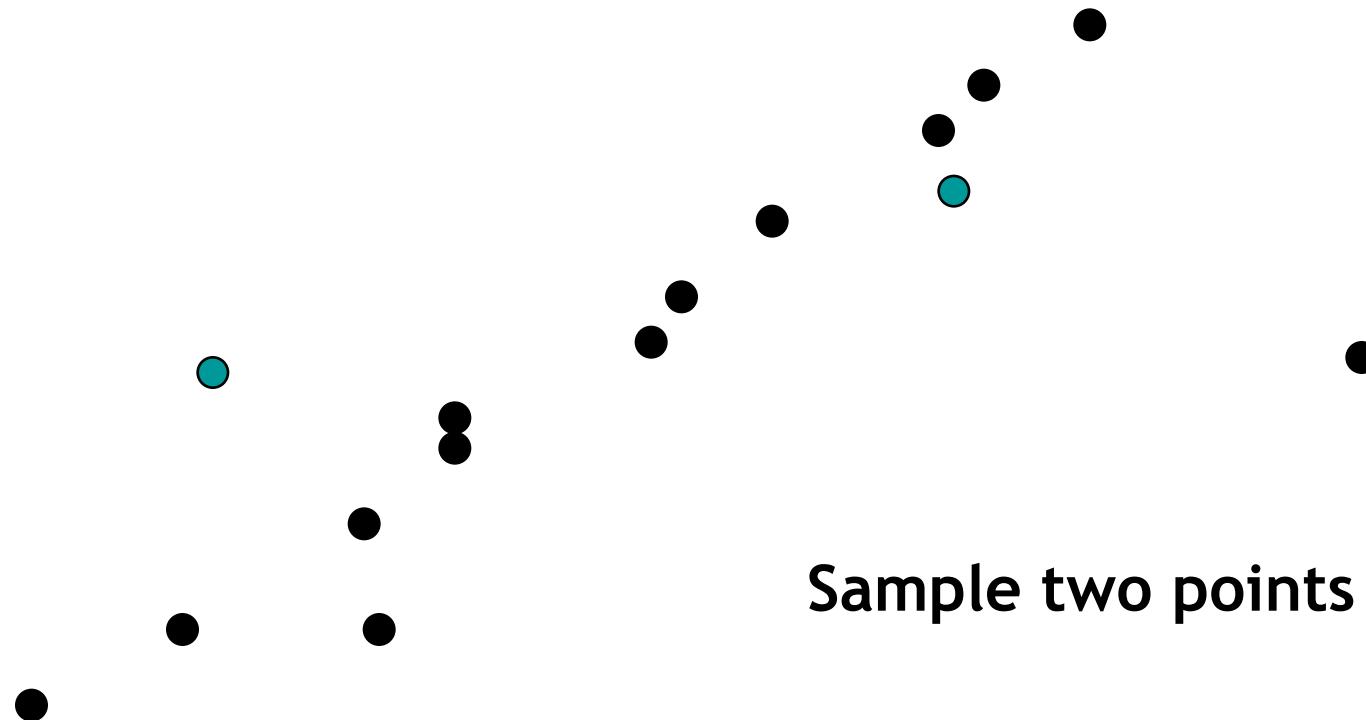
RANSAC Line Fitting Example

- Task: Estimate the best line
 - *How many points do we need to estimate the line?*



RANSAC Line Fitting Example

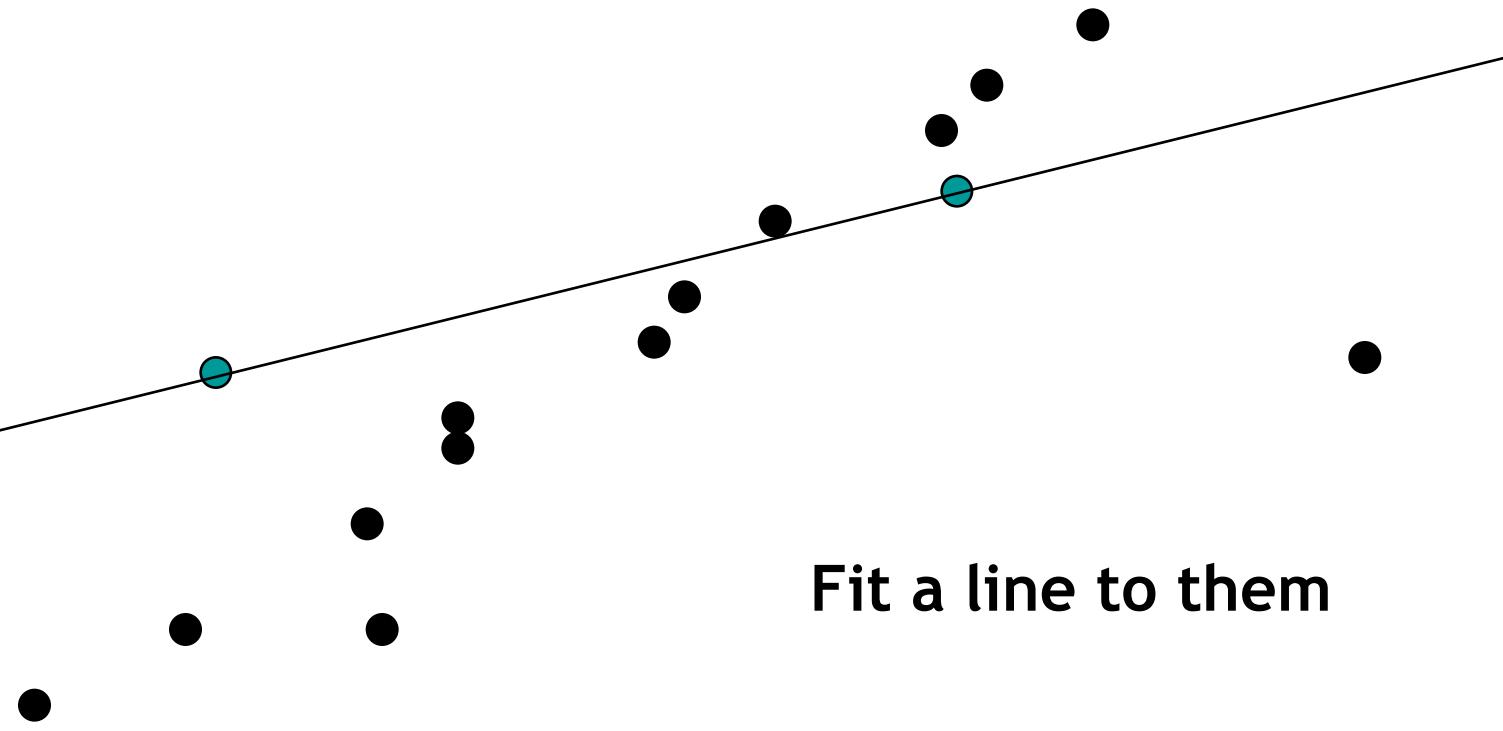
- Task: Estimate the best line



Sample two points

RANSAC Line Fitting Example

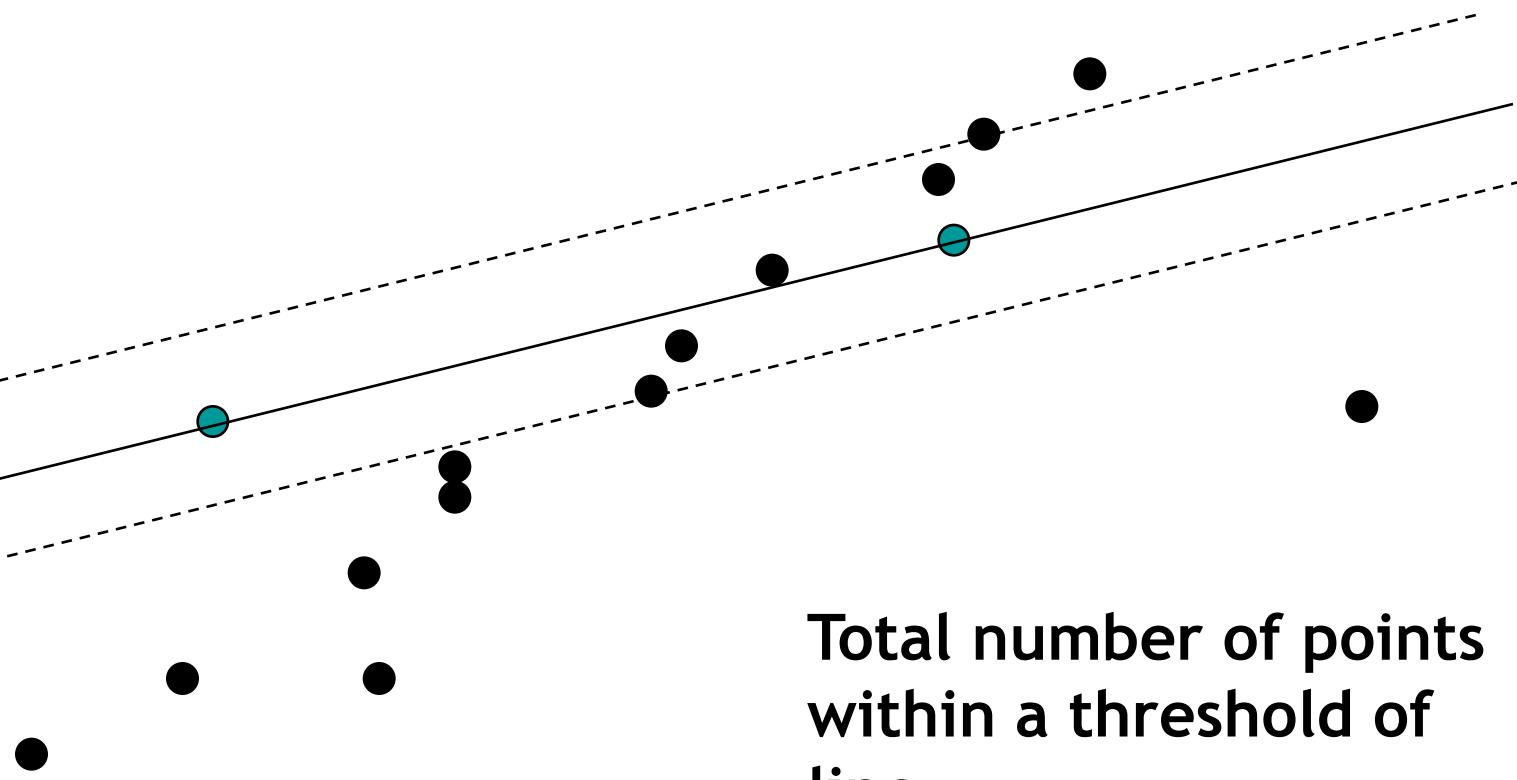
- Task: Estimate the best line



Fit a line to them

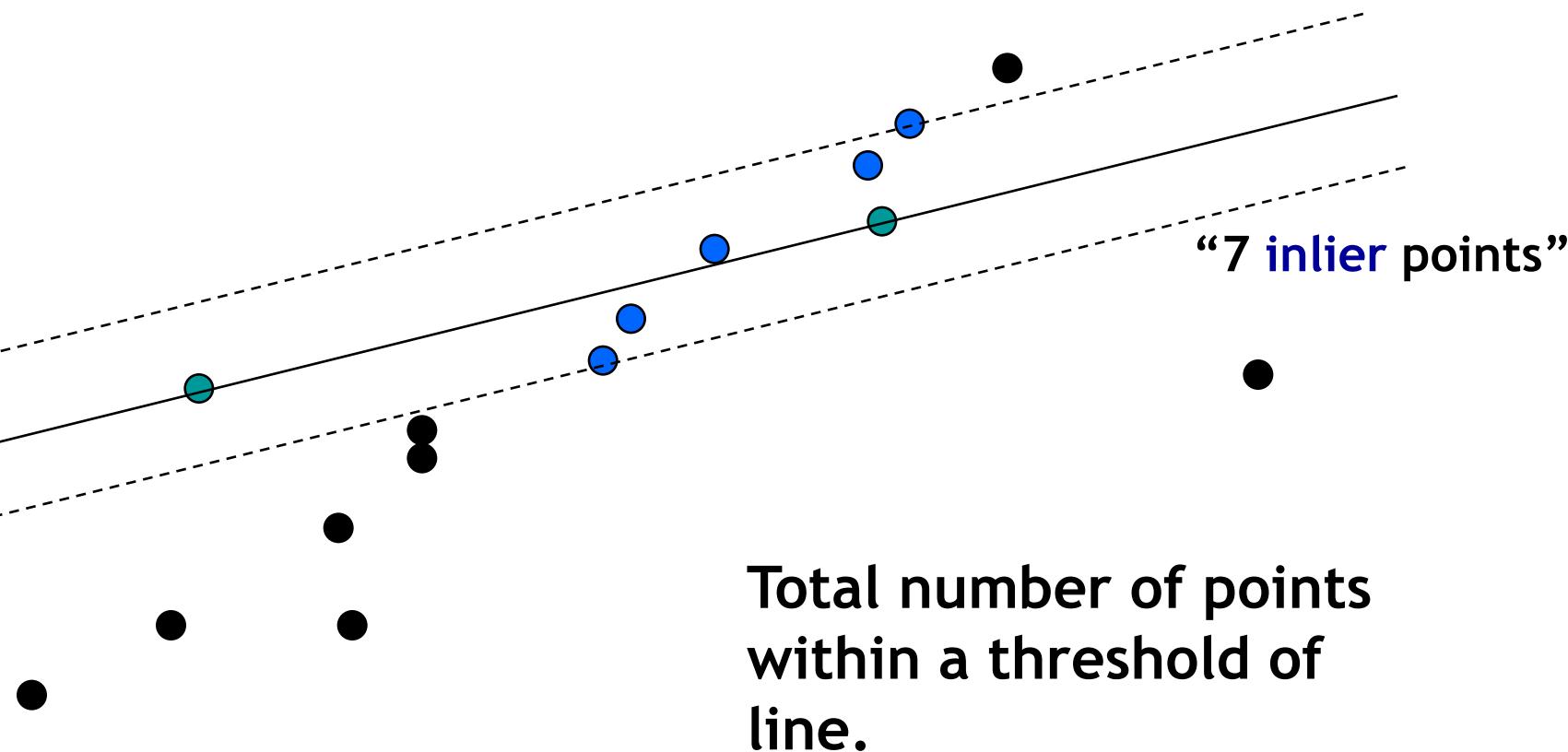
RANSAC Line Fitting Example

- Task: Estimate the best line



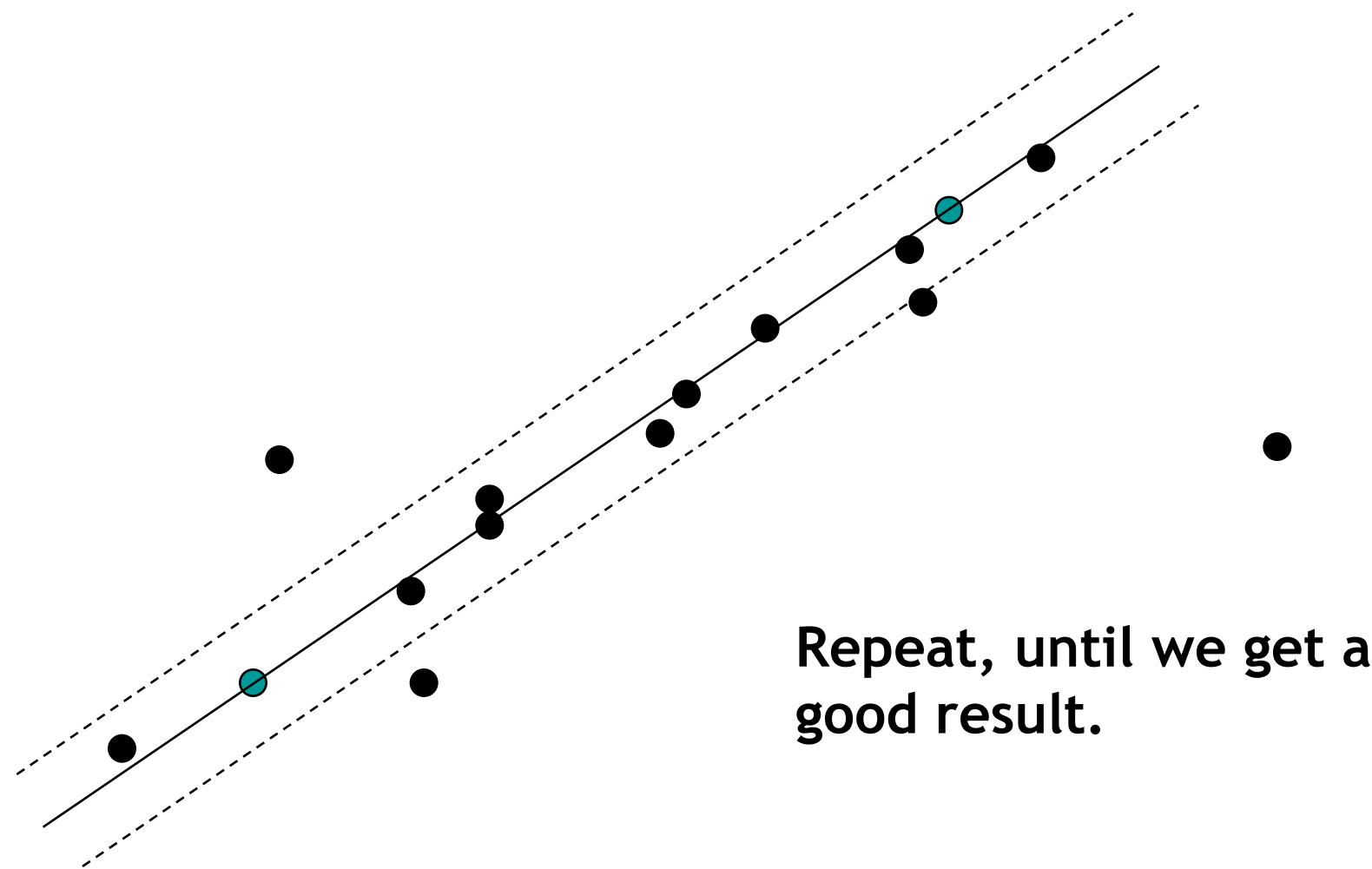
RANSAC Line Fitting Example

- Task: Estimate the best line



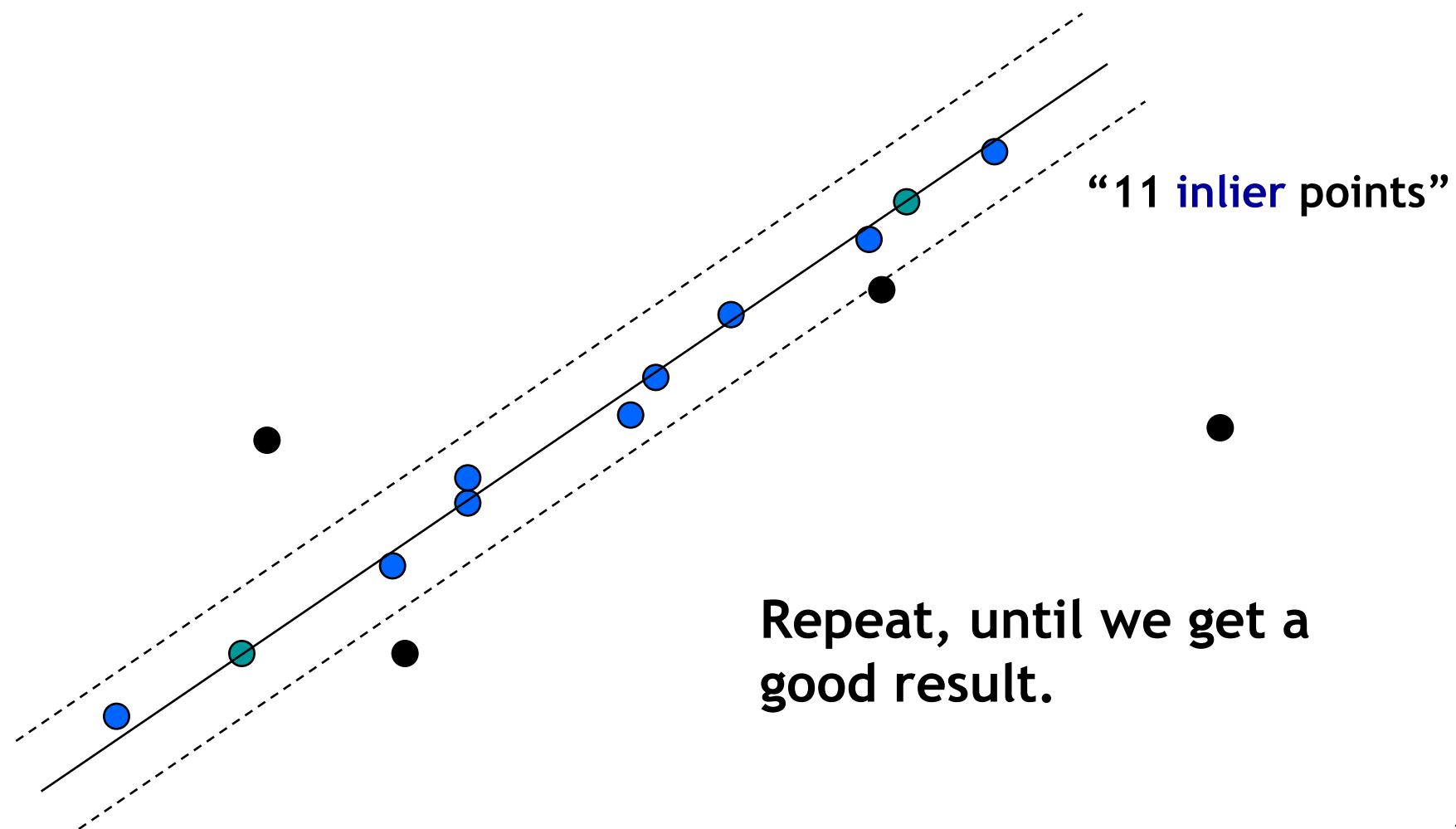
RANSAC Line Fitting Example

- Task: Estimate the best line



RANSAC Line Fitting Example

- Task: Estimate the best line



RANSAC: How many samples?

- How many samples are needed?
 - Suppose w is fraction of inliers (points from line).
 - n points needed to define hypothesis (2 for lines)
 - k samples chosen.
- Prob. that a single sample of n points is correct: w^n
- Prob. that all k samples fail is: $(1 - w^n)^k$

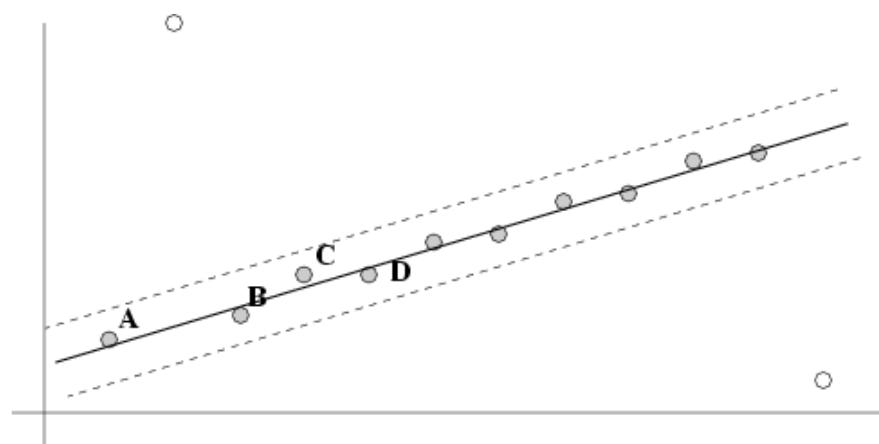
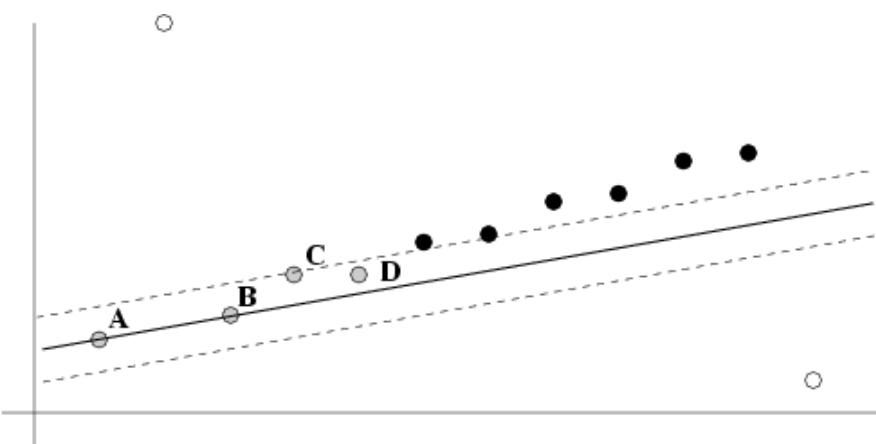
⇒ Choose k high enough to keep this below desired failure rate.

RANSAC: Computed k (p=0.99)

Sample size <i>n</i>	Proportion of outliers						
	5%	10%	20%	25%	30%	40%	50%
2	2	3	5	6	7	11	17
3	3	4	7	9	11	19	35
4	3	5	9	13	17	34	72
5	4	6	12	17	26	57	146
6	4	7	16	24	37	97	293
7	4	8	20	33	54	163	588
8	5	9	26	44	78	272	1177

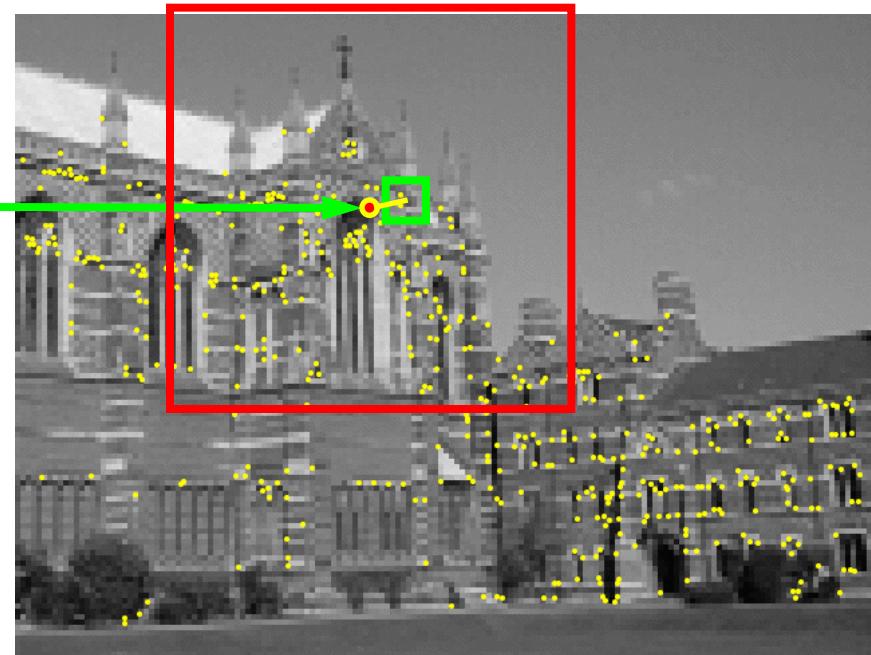
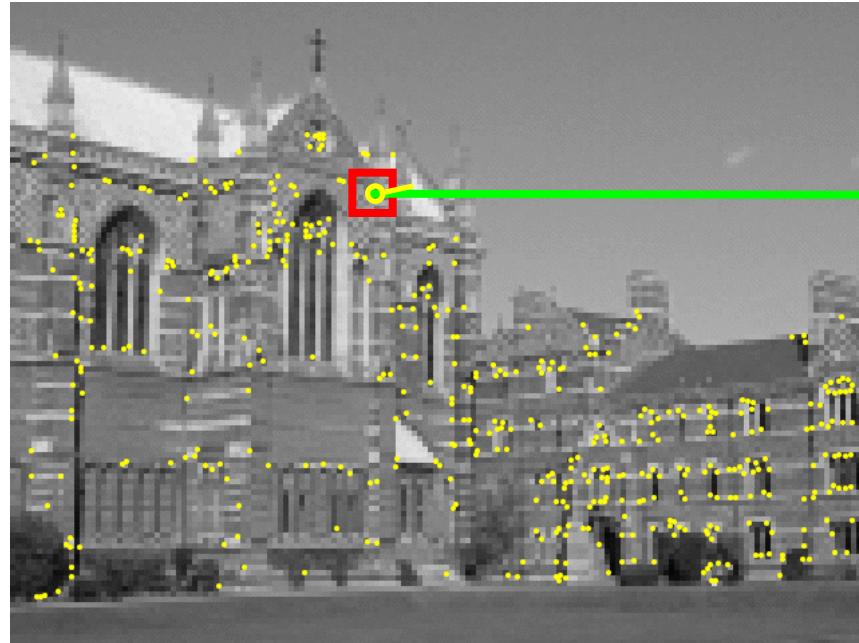
After RANSAC

- RANSAC divides data into inliers and outliers and yields estimate computed from minimal set of inliers.
- Improve this initial estimate with estimation over all inliers (e.g. with standard least-squares minimization).
- But this may change inliers, so alternate fitting with reclassification as inlier/outlier.



Example: Finding Feature Matches

- Find best stereo match within a square search window (here 300 pixels²)
- Global transformation model: epipolar geometry

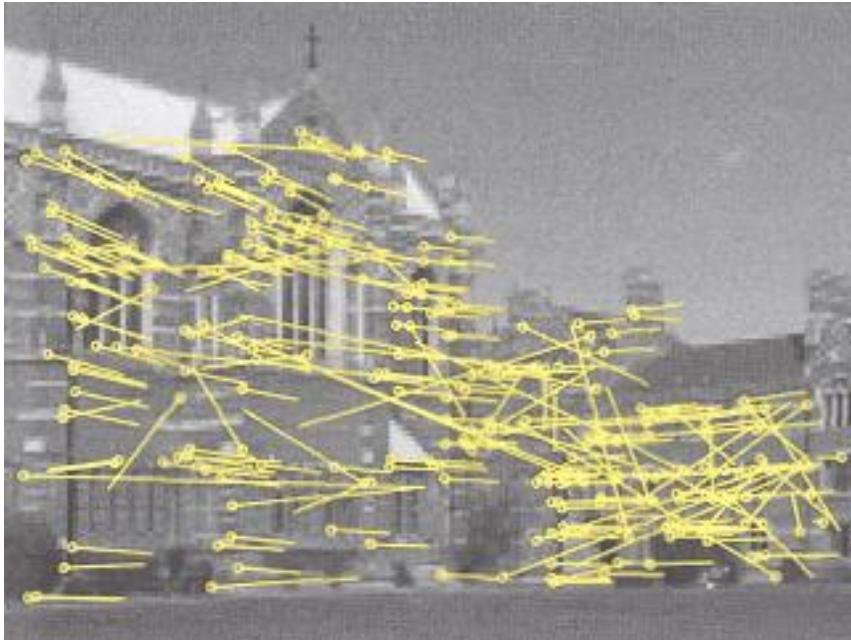


Images from Hartley & Zisserman

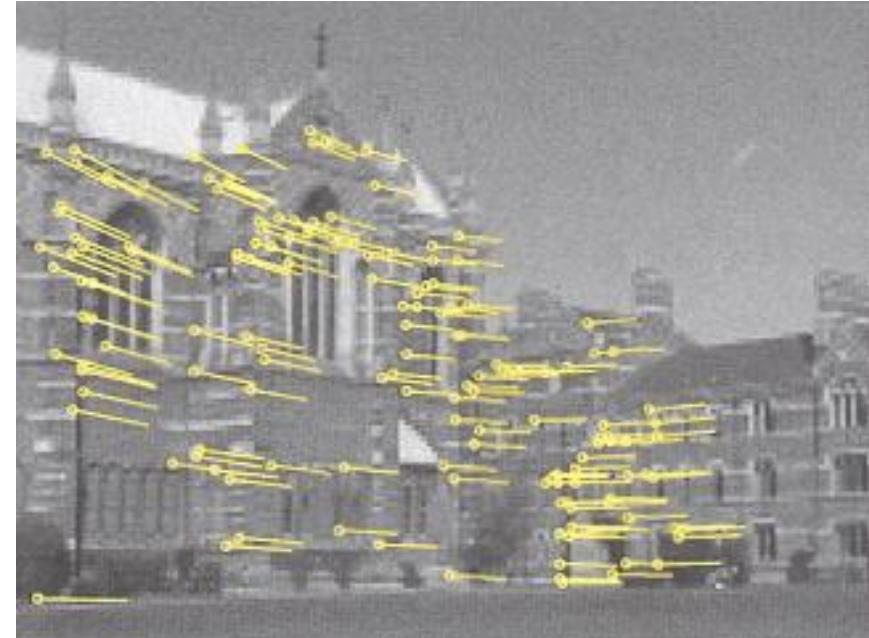
Example: Finding Feature Matches

- Find best stereo match within a square search window (here 300 pixels²)
- Global transformation model: epipolar geometry

before RANSAC



after RANSAC



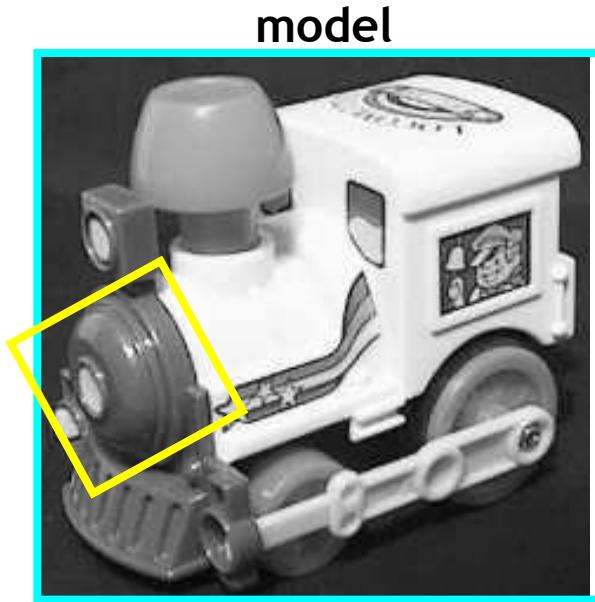
Images from Hartley & Zisserman

Problem with RANSAC

- In many practical situations, the percentage of outliers (incorrect putative matches) is often very high (90% or above).
- Alternative strategy: Generalized Hough Transform

Strategy 2: Generalized Hough Transform

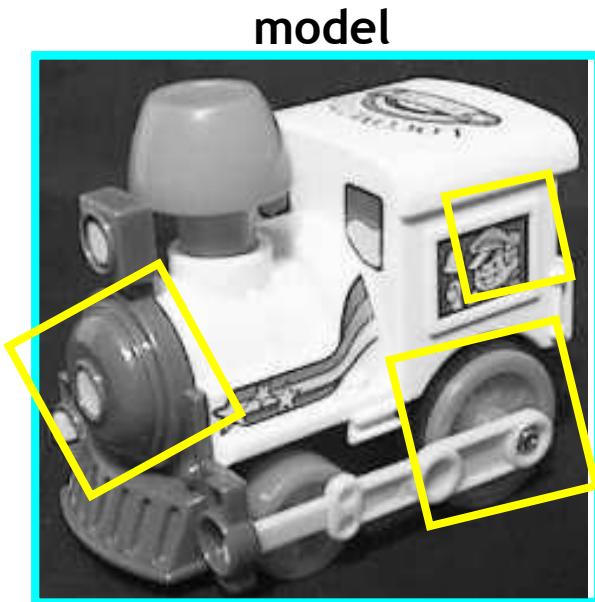
- Suppose our features are scale- and rotation-invariant
 - Then a single feature match provides an alignment hypothesis (translation, scale, orientation).



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Strategy 2: Generalized Hough Transform

- Suppose our features are scale- and rotation-invariant
 - Then a single feature match provides an alignment hypothesis (translation, scale, orientation).
 - Of course, a hypothesis from a single match is unreliable.
 - Solution: let each match vote for its hypothesis in a Hough space with very coarse bins.



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Pose Clustering and Verification with SIFT

- To detect instances of objects from a model base:



1. Index descriptors

- Distinctive features narrow down possible matches

Pose Clustering and Verification with SIFT

- To detect instances of objects from a model base:



1. Index descriptors
 - Distinctive features narrow down possible matches
2. Generalized Hough transform to vote for poses
 - Keypoints have record of parameters relative to model coordinate system
3. Affine fit to check for agreement between model and image features
 - Fit and verify using features from Hough bins with 3+ votes

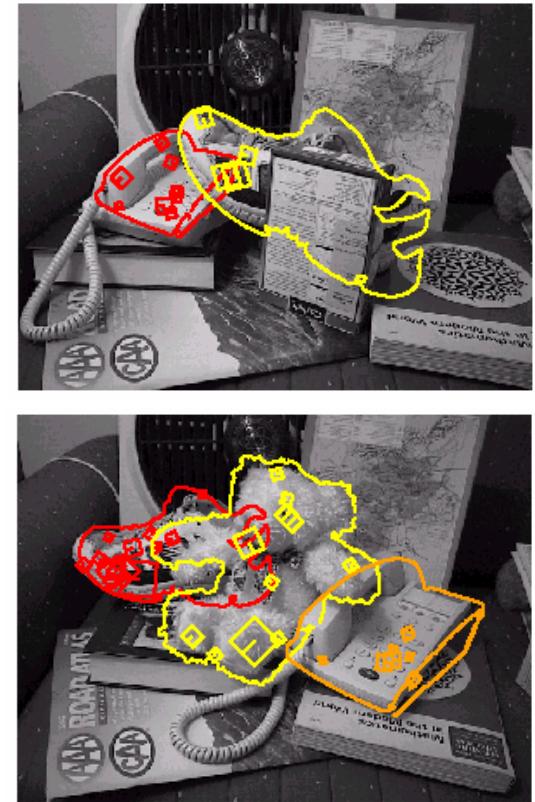
Object Recognition Results



Background subtract for model boundaries

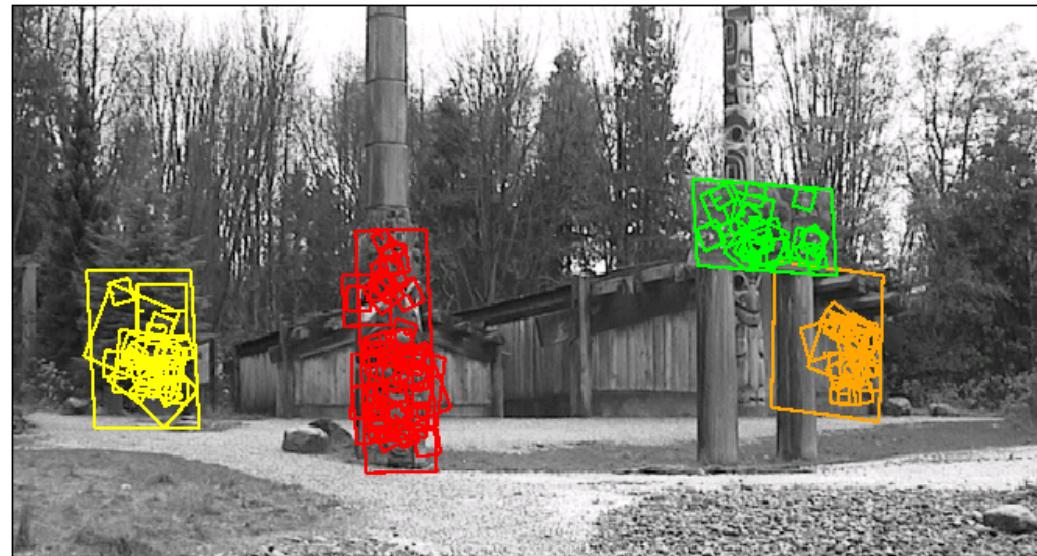


Objects recognized



Recognition in spite of occlusion

Location Recognition



[Lowe, IJCV'04]

Slide credit: David Lowe

Topics of This Lecture

- Dealing with Outliers
 - RANSAC
 - Generalized Hough Transform
- Indexing with Local Features
 - Inverted file index
 - Visual Vocabularies
- Bag-of-Words Model
 - Use for image classification

Application: Mobile Visual Search

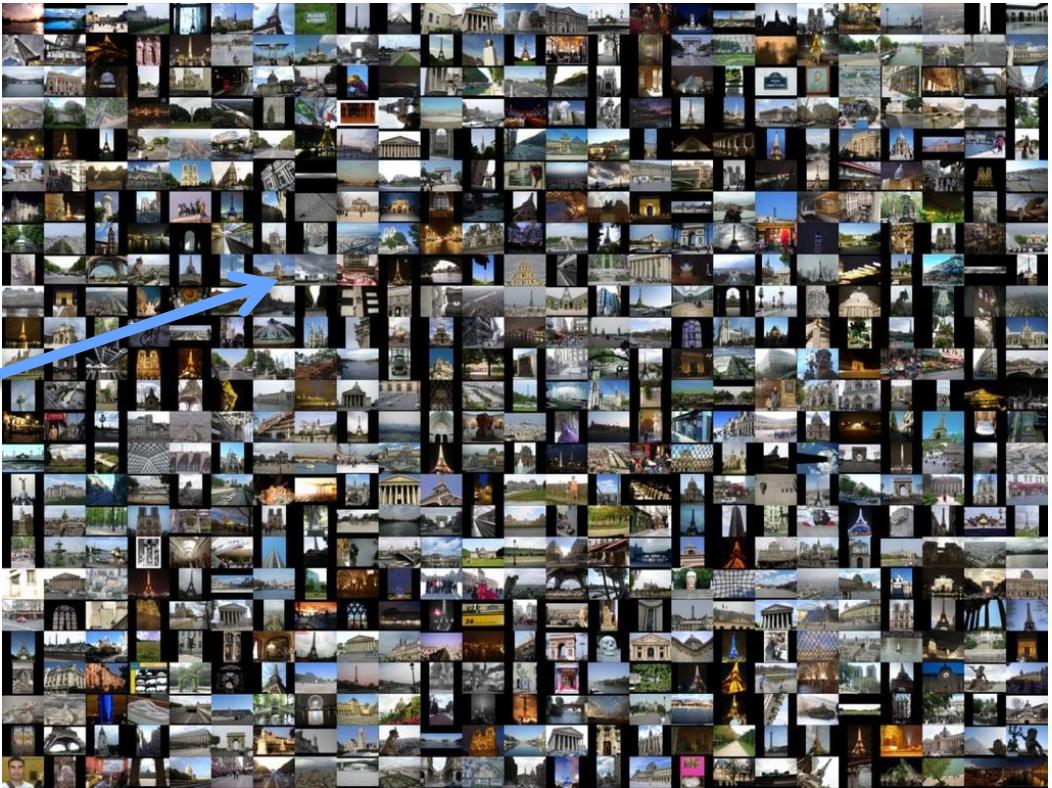
Google Goggles in Action

Click the icons below to see the different ways Google Goggles can be used.



- Take photos of objects as queries for visual search

Large-Scale Image Matching Problem

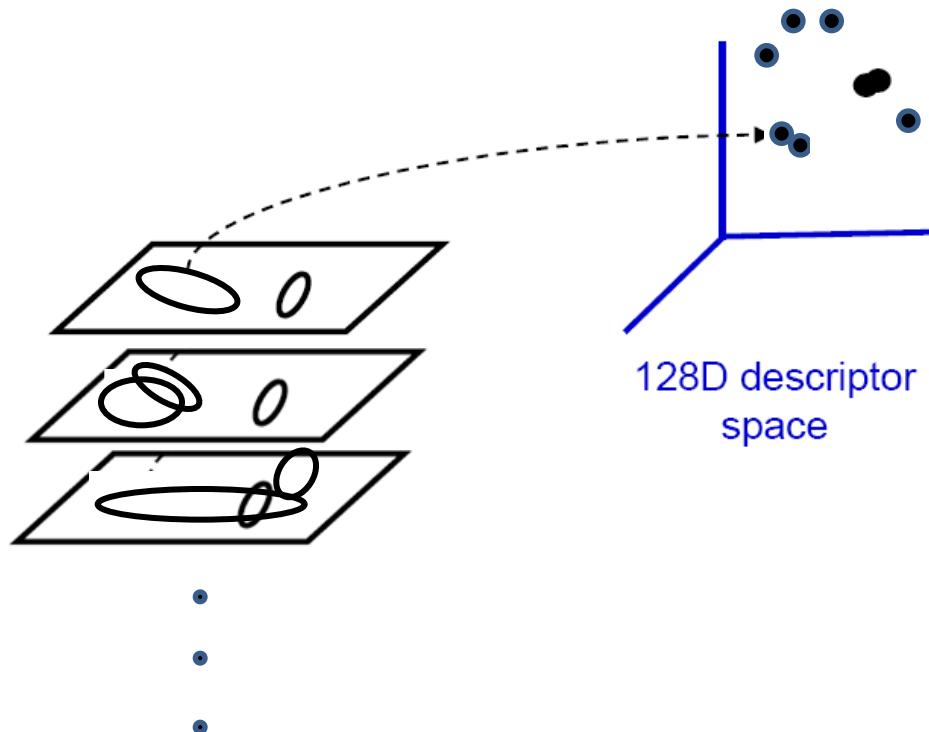


Database with thousands (millions) of images

- How can we perform this matching step efficiently?

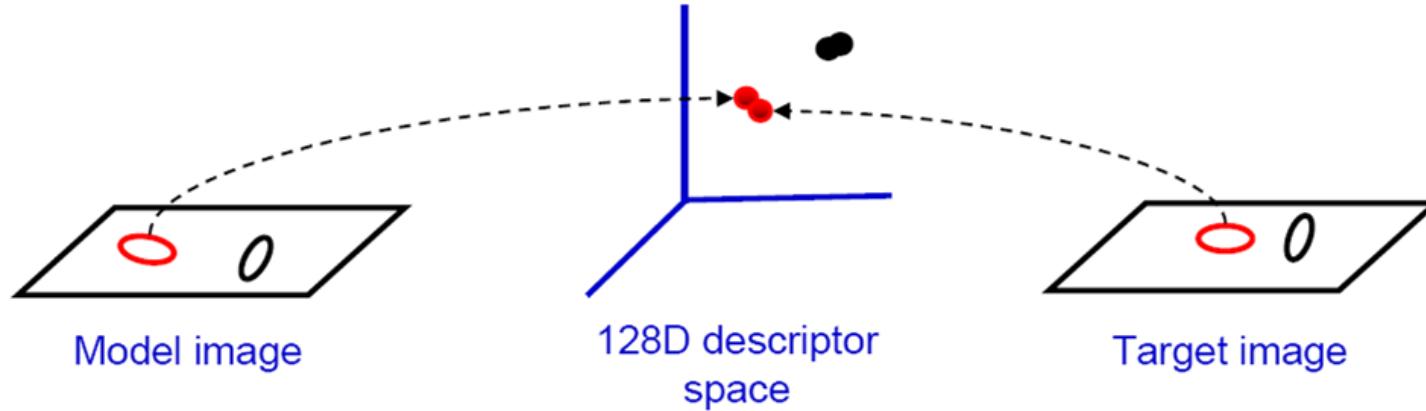
Indexing Local Features

- Each patch / region has a descriptor, which is a point in some high-dimensional feature space (e.g., SIFT)



Indexing Local Features

- When we see close points in feature space, we have similar descriptors, which indicates similar local content.



- This is of interest for many applications
 - E.g. Image matching,
 - E.g. Retrieving images of similar objects,
 - E.g. Object recognition, categorization, 3d Reconstruction,...

Indexing Local Features

- With potentially thousands of features per image, and hundreds to millions of images to search, how to efficiently find those that are relevant to a new image?
- Low-dimensional descriptors (e.g. through PCA):
 - Can use standard efficient data structures for nearest neighbor search
- High-dimensional descriptors
 - Approximate nearest neighbor search methods more practical
- Inverted file indexing schemes

Indexing Local Features: Inverted File Index

Index	
"Along I-75," From Detroit to Florida; <i>inside back cover</i>	
"Drive I-95," From Boston to Florida; <i>inside back cover</i>	
1929 Spanish Trail Roadway; 101-102,104	
511 Traffic Information; 83	
A1A (Barrier Isl) - I-95 Access; 86	
AAA (and CAA); 83	
AAA National Office; 88	
Abbreviations,	
Colored 25 mile Maps; cover	
Exit Services; 196	
Travelogue; 85	
Africa; 177	
Agricultural Inspection Stns; 126	
Ah-Tah-Thi-Ki Museum; 180	
Air Conditioning, First; 112	
Alabama; 124	
Alachua; 132	
County; 131	
Alafia River; 143	
Alapaha, Name; 126	
Alfred B Macay Gardens; 106	
Alligator Alley; 154-155	
Alligator Farm, St Augustine; 169	
Alligator Hole (definition); 157	
Alligator, Buddy; 155	
Alligators; 100,135,138,147,156	
Anastasia Island; 170	
Anhaisa; 108-109,146	
Apalachicola River; 112	
Appleton Mus of Art; 136	
Aquifer; 102	
Arabian Nights; 94	
Art Museum, Ringling; 147	
Aruba Beach Cafe; 183	
Aucilla River Project; 106	
Babcock-Web WMA; 151	
Bahia Mar Marina; 184	
Baker County; 99	
Barefoot Mallmen; 182	
Barge Canal; 137	
Bee Line Expy; 80	
Belz Outlet Mall; 89	
Bernard Castro; 136	
Big "I"; 165	
Big Cypress; 155,158	
Big Foot Monster; 105	
Billie Swamp Safari; 160	
Blackwater River SP; 117	
Blue Angels	
Butterfly Center, McGuire; 134	
CAA (see AAA)	
CCC, The; 111,113,115,135,142	
Ca d'Zan; 147	
Caloosahatchee River; 152	
Name; 150	
Canaveral Natnl Seashore; 173	
Cannon Creek Airpark; 130	
Canopy Road; 106,160	
Cape Canaveral; 174	
Castillo San Marcos; 169	
Cave Diving; 131	
Cayo Costa, Name; 150	
Celebration; 93	
Charlotte County; 149	
Charlotte Harbor; 150	
Chautauqua; 116	
Chipley; 114	
Name; 115	
Choctawatchee, Name; 115	
Circus Museum, Ringling; 147	
Citrus; 88,97,130,136,140,180	
CityPlace, W Palm Beach; 180	
City Maps,	
Ft Lauderdale Expyws; 194-195	
Jacksonville; 163	
Kissimmee Expyws; 192-193	
Miami Expressways; 194-195	
Orlando Expressways; 192-193	
Pensacola; 26	
Tallahassee; 191	
Tampa-St. Petersburg; 63	
St. Augustine; 191	
Civil War; 100,108,127,138,141	
Clearwater Marine Aquarium; 187	
Collier County; 154	
Collier, Barron; 152	
Colonial Spanish Quarters; 168	
Columbia County; 101,128	
Coquina Building Material; 165	
Corkscrew Swamp, Name; 154	
Cowboys; 95	
Crab Trap II; 144	
Cracker, Florida; 88,95,132	
Crosstown Expy; 11,35,98,143	
Cuban Bread; 184	
Dade Battlefield; 140	
Dade, Maj. Francis; 139-140,161	
Daniel Beach Hurricane; 184	
Daniel Boone, Florida Walk; 117	
Daytona Beach; 172-173	
De Land; 87	
Driving Lanes; 85	
Duval County; 163	
Eau Gallie; 175	
Edison, Thomas; 152	
Eglin AFB; 116-118	
Eight Reale; 176	
Ellenton; 144-145	
Emanuel Point Wreck; 120	
Emergency Callboxes; 83	
Epiphytes; 142,148,157,159	
Escambia Bay; 119	
Bridge (I-10); 119	
County; 120	
Estero; 153	
Everglade; 90,95,139-140,154-160	
Draining of; 156,181	
Wildlife MA; 160	
Wonder Gardens; 154	
Falling Waters SP; 115	
Fantasy of Flight; 95	
Fayer Dykes SP; 171	
Fires, Forest; 166	
Fires, Prescribed; 148	
Fisherman's Village; 151	
Flagler County; 171	
Flagler, Henry; 97,165,167,171	
Florida Aquarium; 186	
Florida,	
12,000 years ago; 187	
Cavern SP; 114	
Map of all Expressways; 2-3	
Mus of Natural History; 134	
National Cemetery ; 141	
Part of Africa; 177	
Platform; 187	
Sheriff's Boys Camp; 126	
Sports Hall of Fame; 130	
Sun 'n Fun Museum; 97	
Supreme Court; 107	
Florida's Turnpike (FTP); 178,189	
25 mile Strip Maps; 66	
Administration; 189	
Coin System; 190	
Exit Services; 189	
HEFT; 76,161,190	
History; 189	
Names; 189	
Service Plazas; 190	
Spur SR91; 76	
Ticket System; 190	
Toll Plazas; 190	
Ford, Henry; 152	

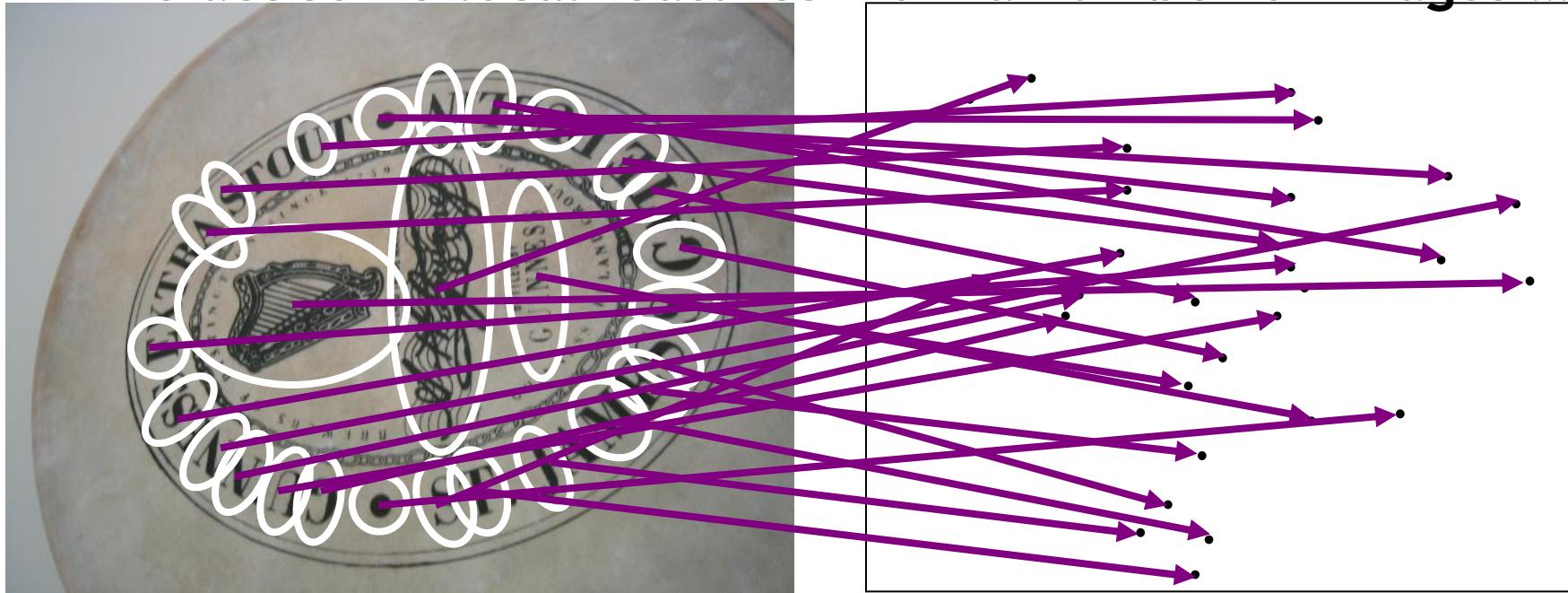
- For text documents, an efficient way to find all *pages* on which a *word* occurs is to use an index...
- We want to find all *images* in which a *feature* occurs.
- To use this idea, we'll need to map our features to “visual words”.

Text Retrieval vs. Image Search

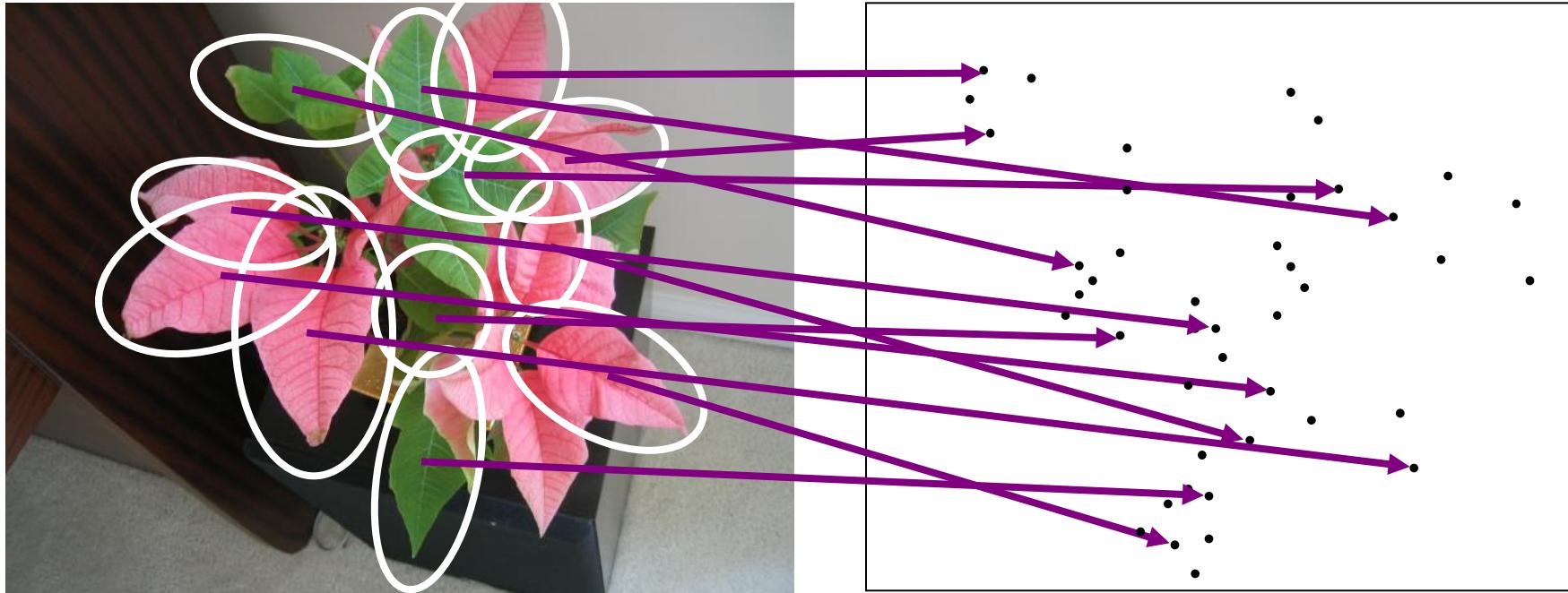
- What makes the problems similar, different?

Visual Words: Main Idea

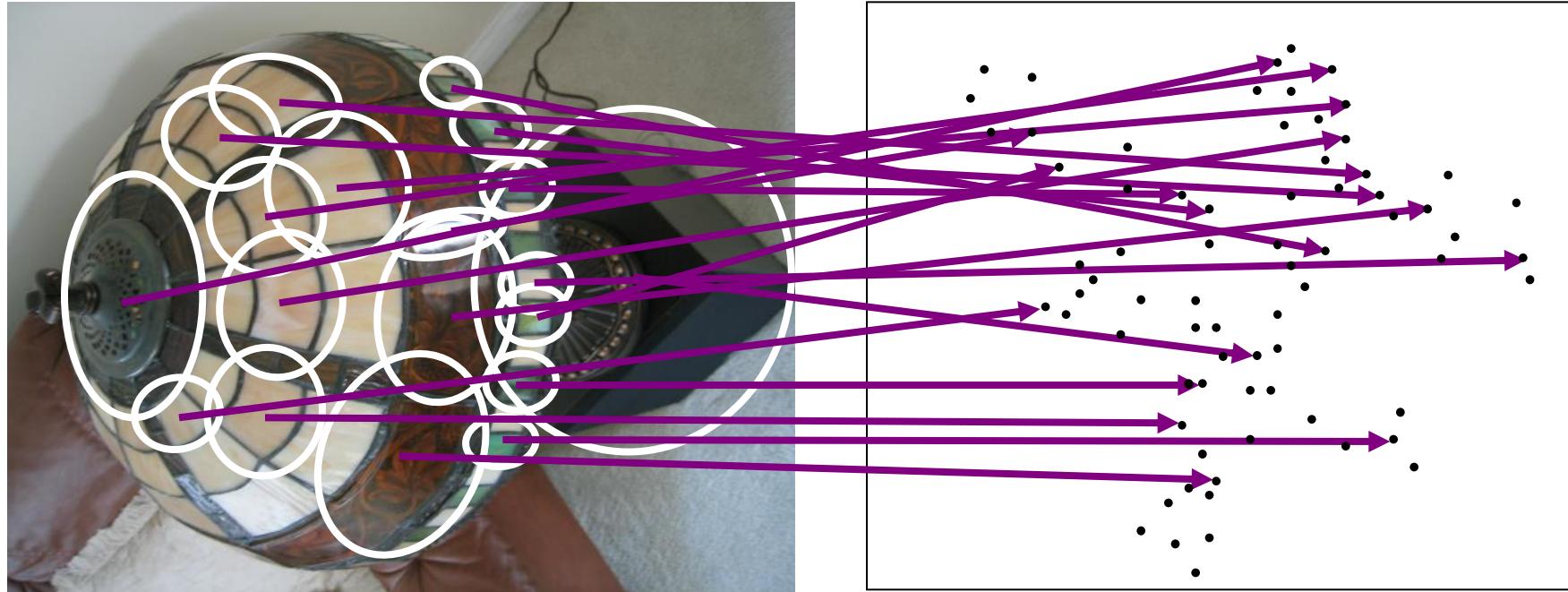
- Extract some local features from a number of images ...



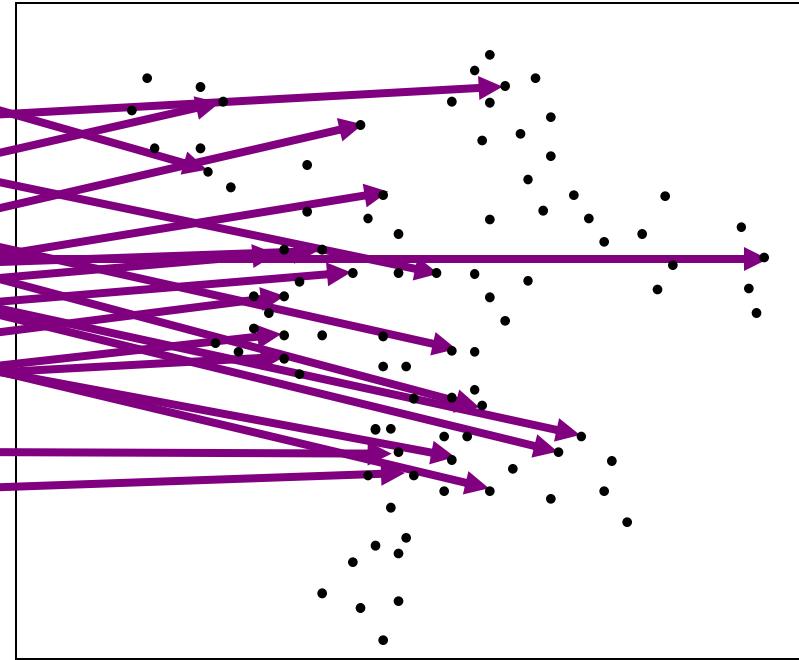
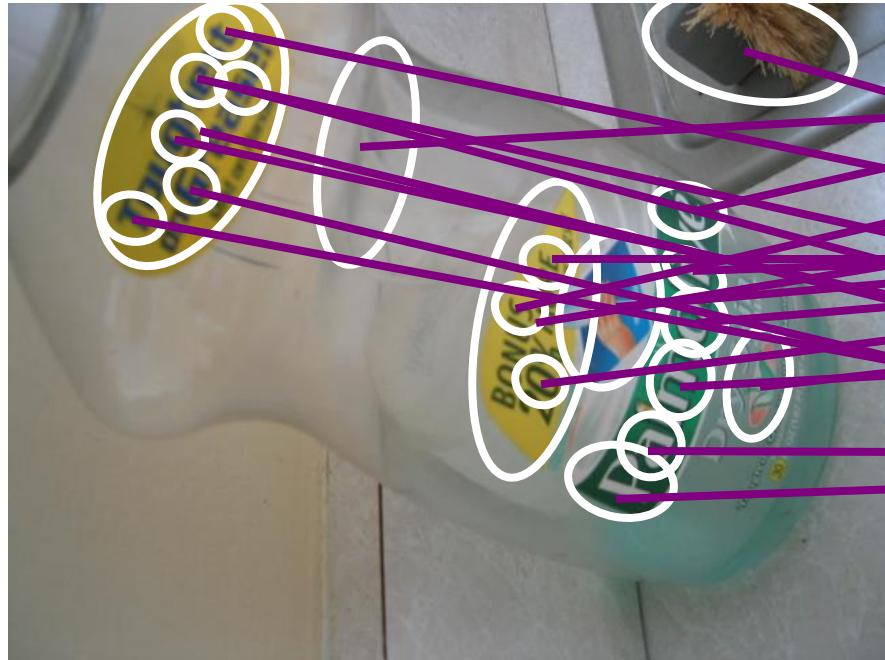
Visual Words: Main Idea



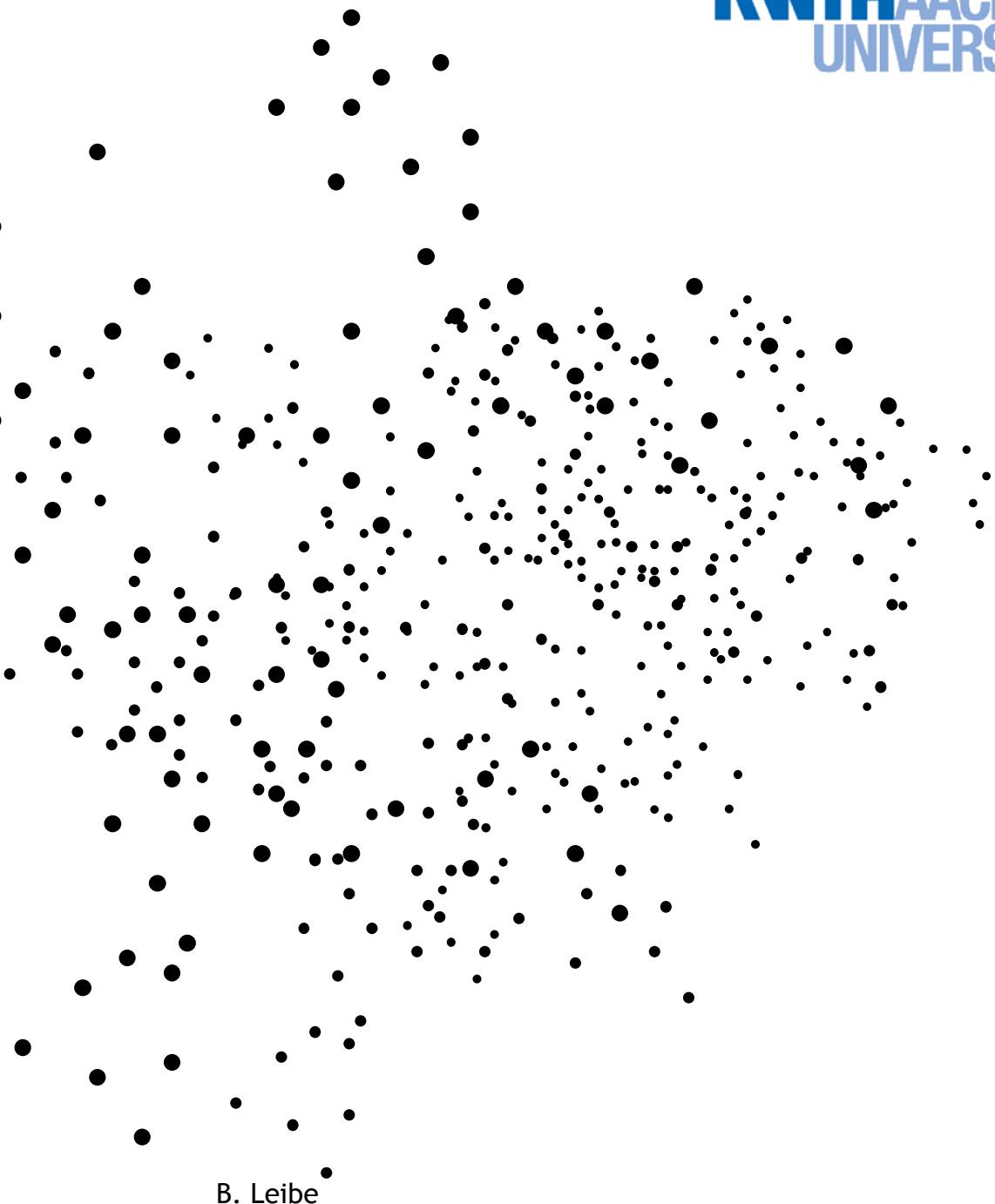
Visual Words: Main Idea

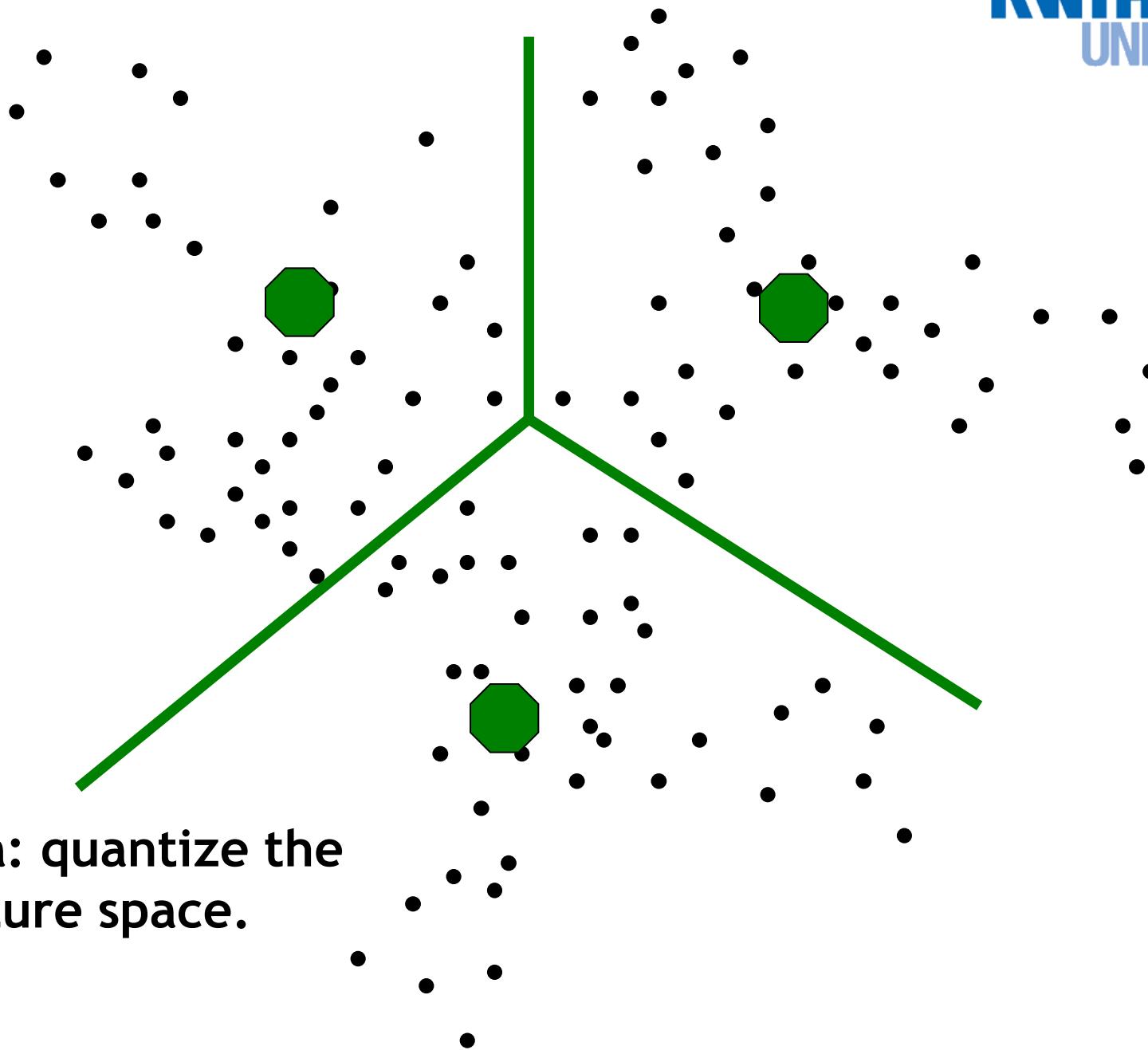


Visual Words: Main Idea



Each point is a local descriptor,
e.g. SIFT vector.

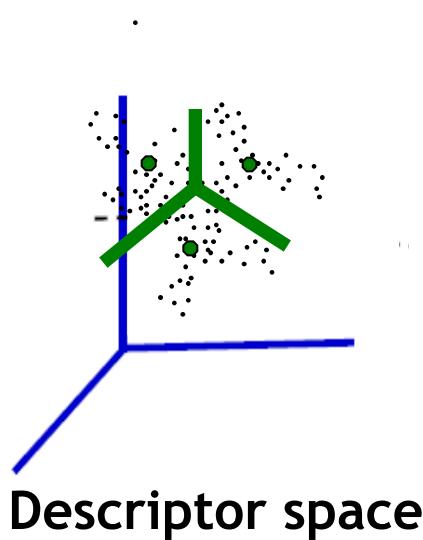
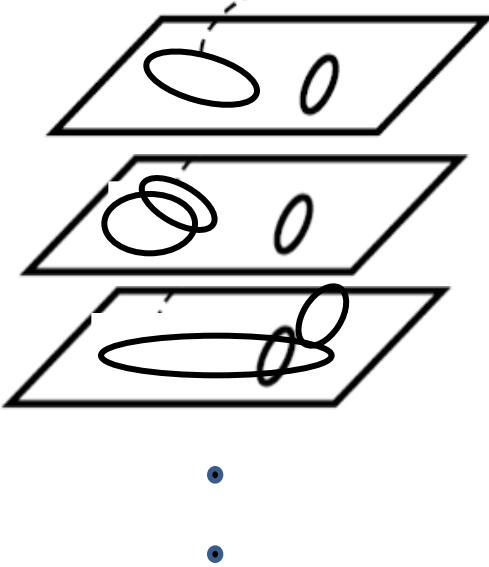




Idea: quantize the feature space.

Indexing with Visual Words

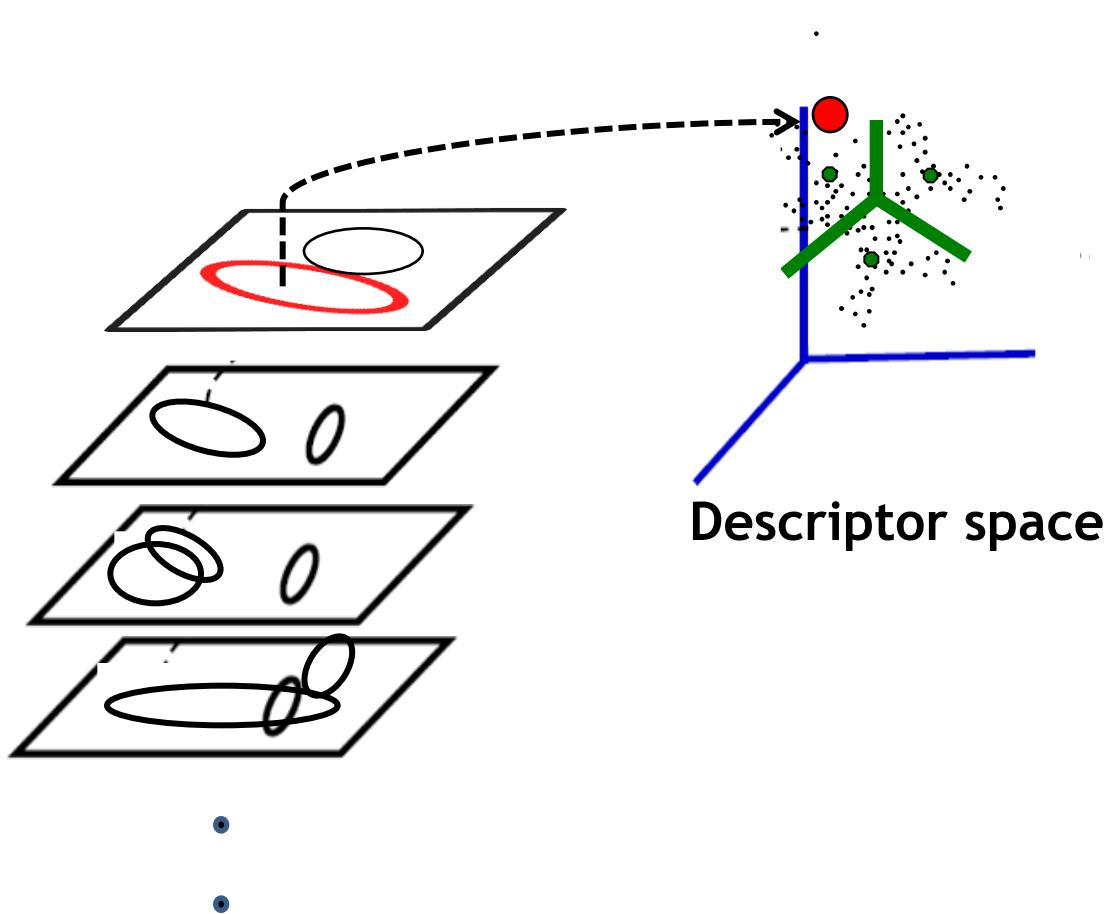
Map high-dimensional descriptors to tokens/words by quantizing the feature space



- Quantize via clustering, let cluster centers be the prototype “words”

Indexing with Visual Words

Map high-dimensional descriptors to tokens/words by quantizing the feature space



- Determine which word to assign to each new image region by finding the closest cluster center.

Visual Words

- Example: each group of points is a visual word

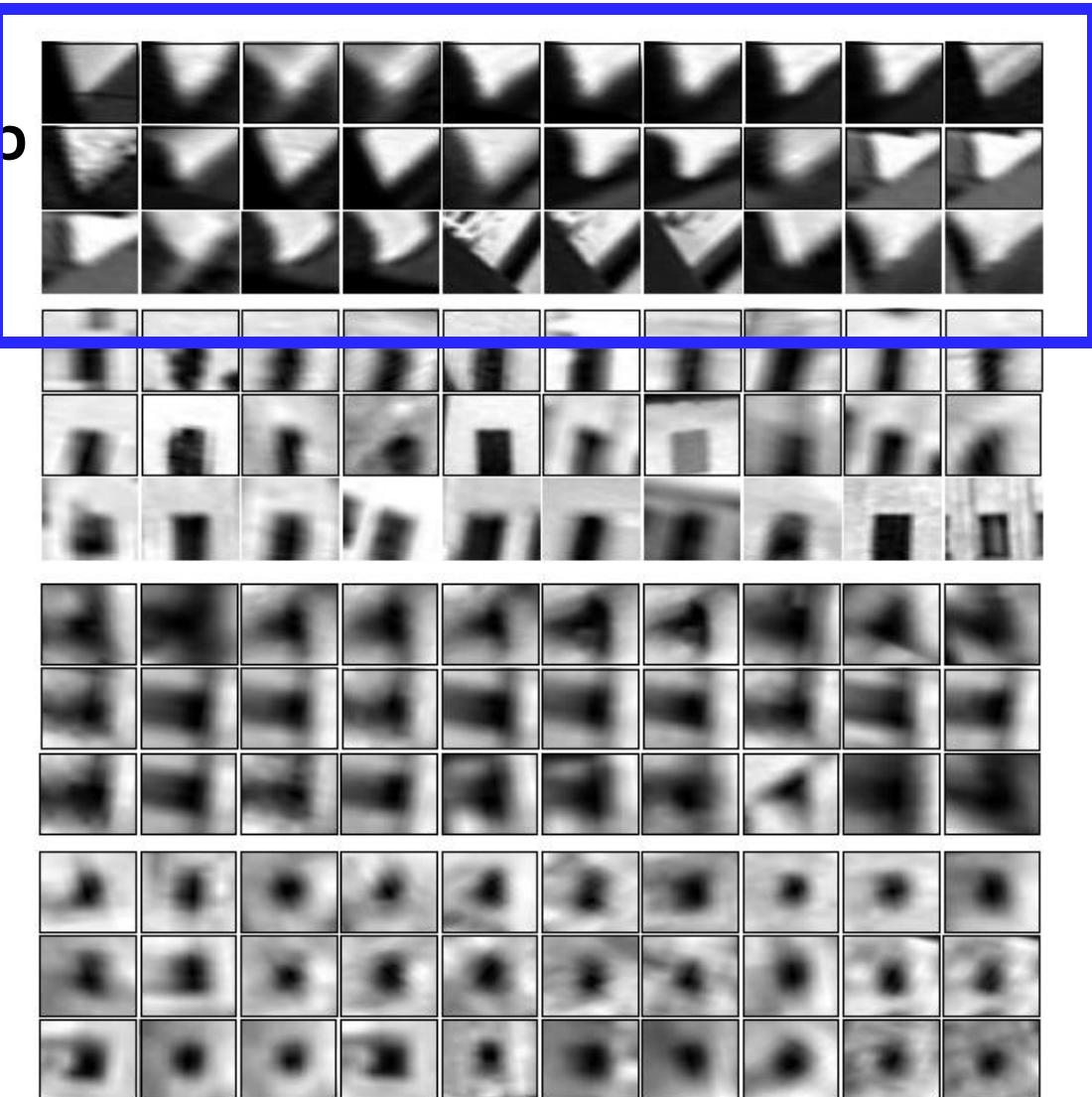
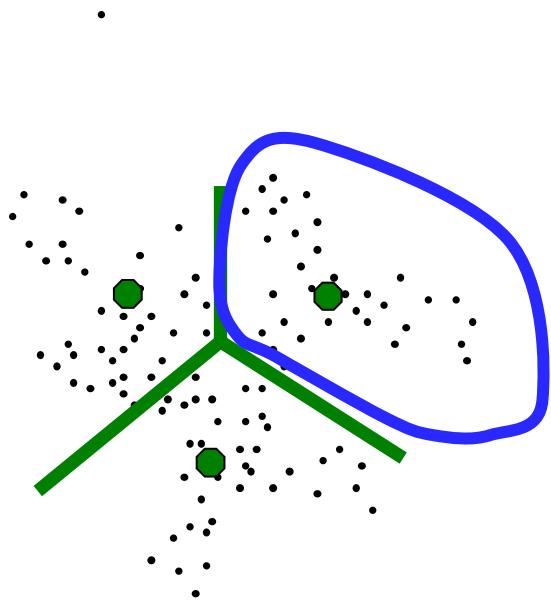
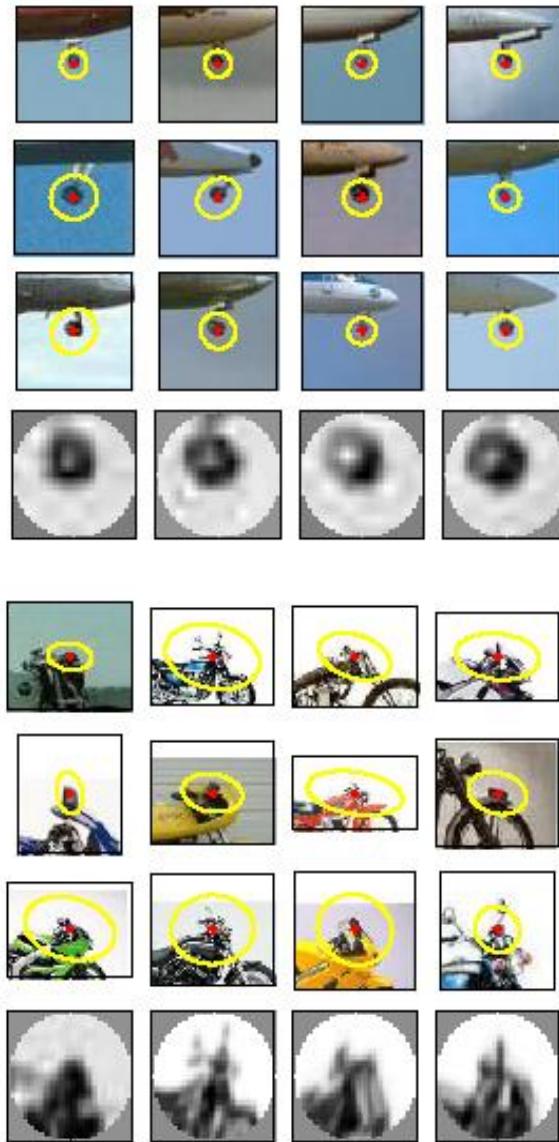


Figure from Sivic & Zisserman, ICCV 2003

Visual Words

- Often used for describing scenes and objects for the sake of indexing or classification.



Sivic & Zisserman 2003;
Csurka, Bray, Dance, & Fan
2004; many others.

Inverted File for Images of Visual Words



frame #5



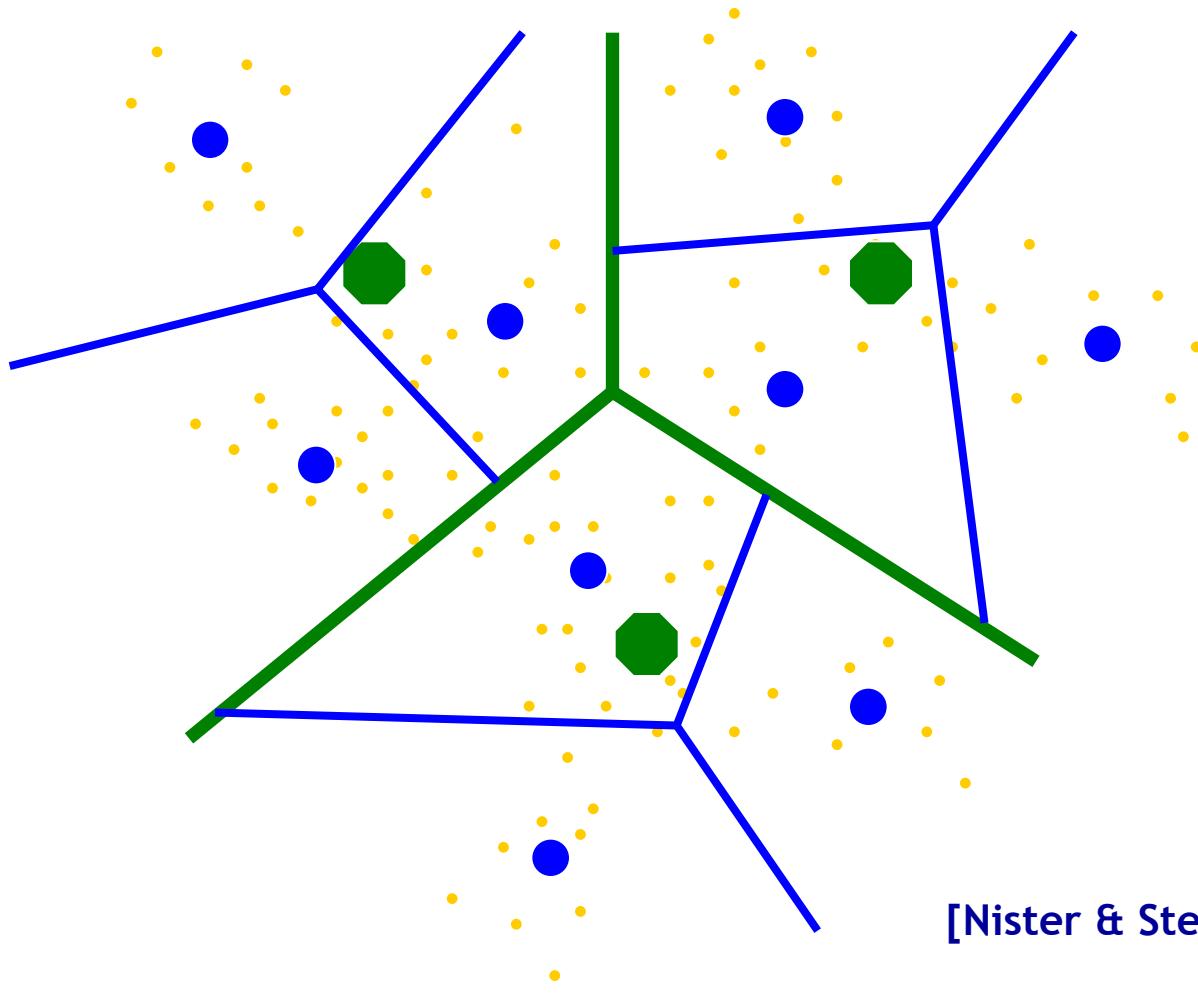
frame #10

Word number	List of image numbers
1	→ 5, 10, ...
2	→ 10, ...
...	...

When will this give us a significant gain in efficiency?

Example: Recognition with Vocabulary Tree

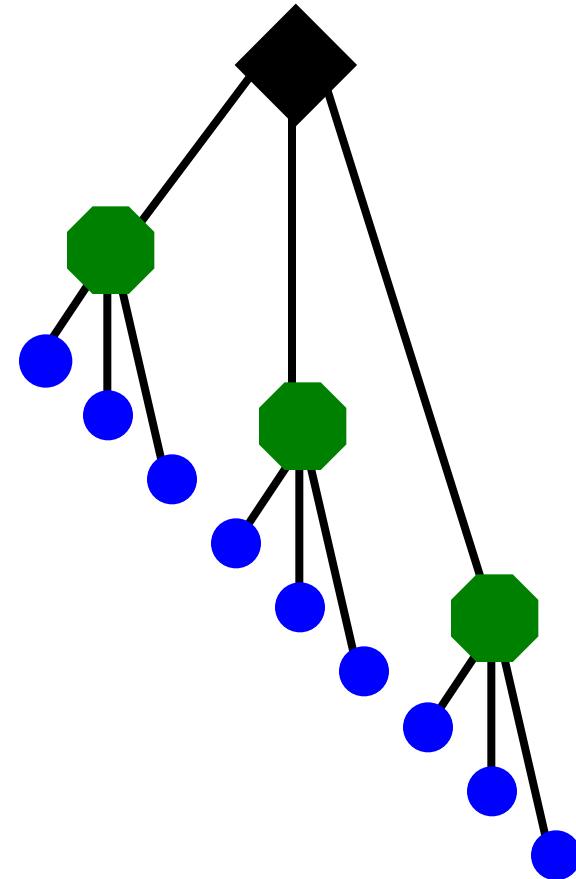
- Tree construction:



[Nister & Stewenius, CVPR'06]

Vocabulary Tree

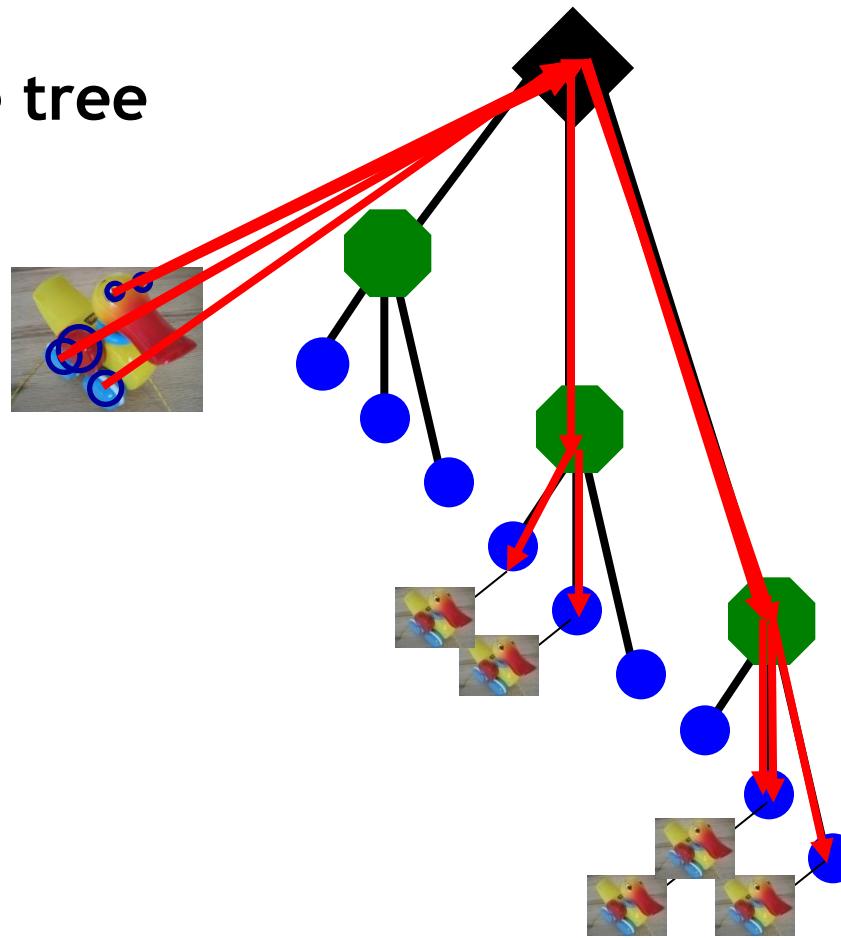
- Training: Filling the tree



[Nister & Stewenius, CVPR'06]

Vocabulary Tree

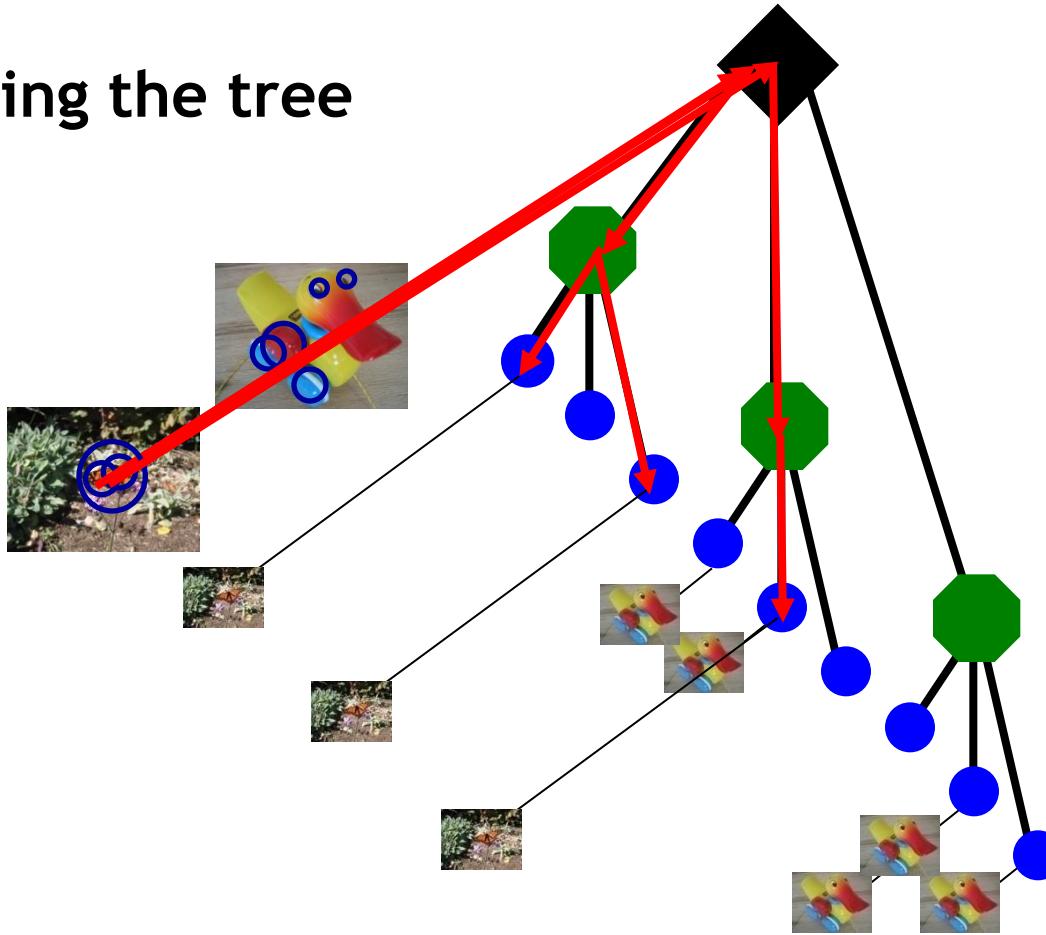
- Training: Filling the tree



[Nister & Stewenius, CVPR'06]

Vocabulary Tree

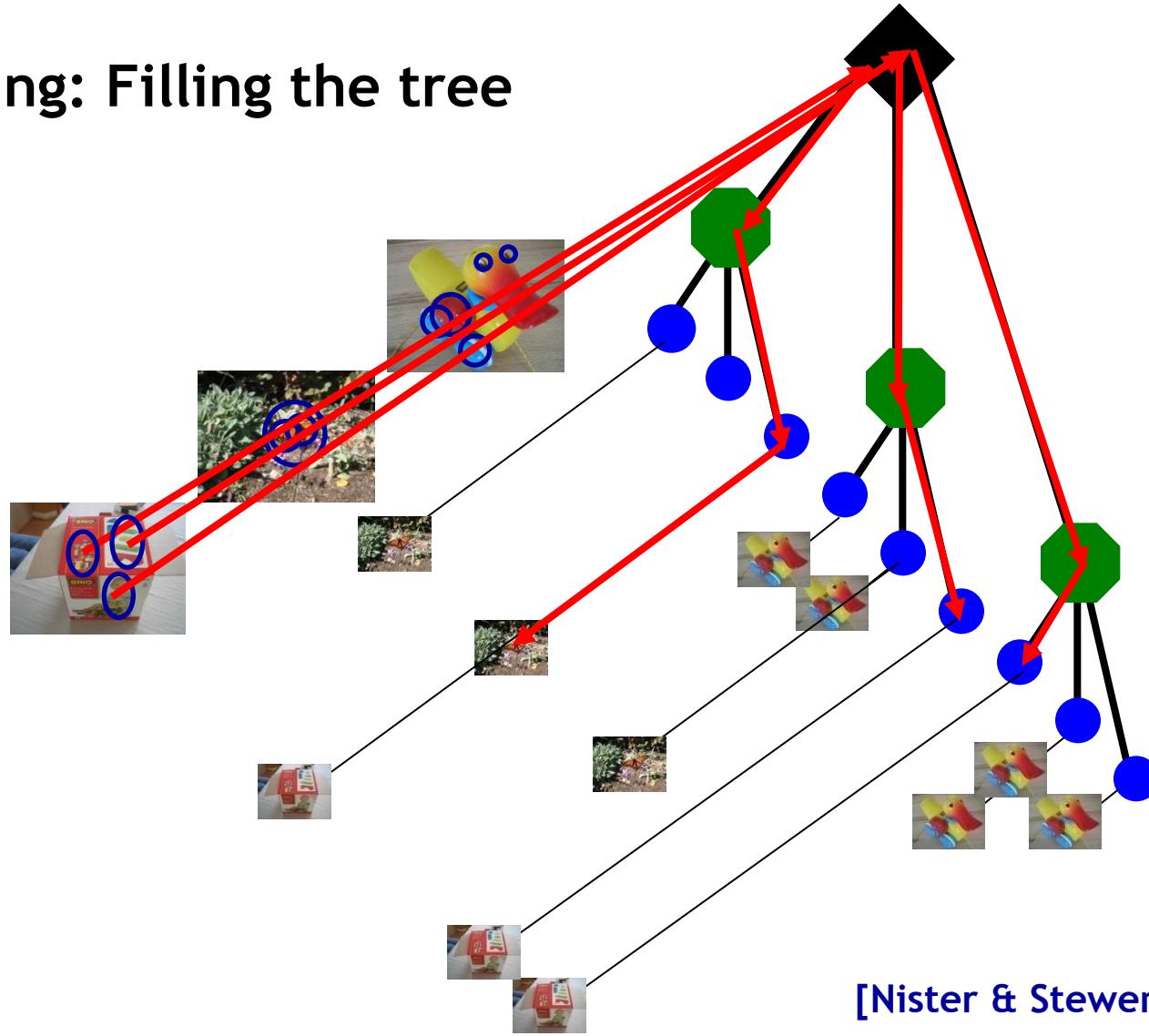
- Training: Filling the tree



[Nister & Stewenius, CVPR'06]

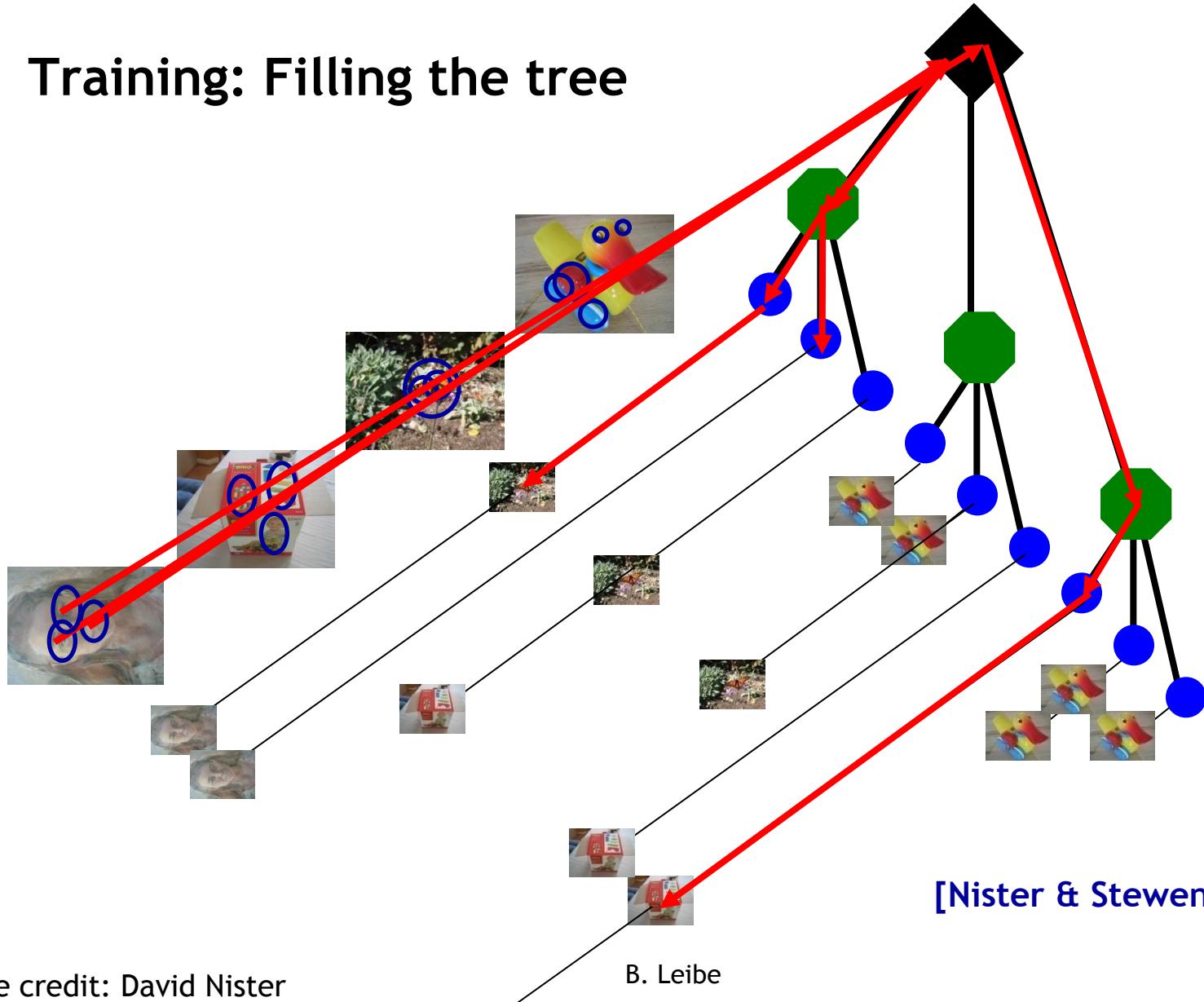
Vocabulary Tree

- Training: Filling the tree



Vocabulary Tree

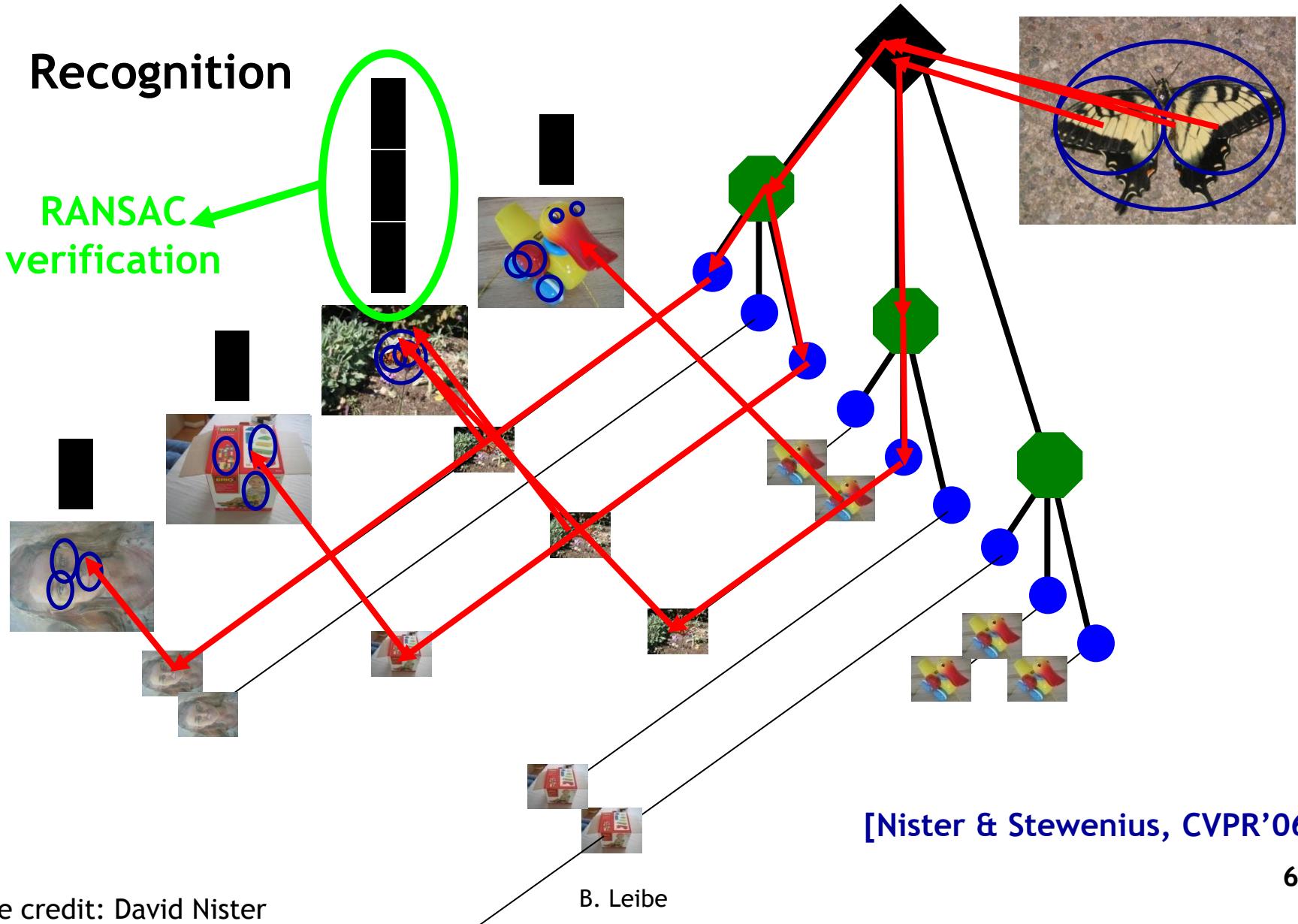
- Training: Filling the tree



Vocabulary Tree

- Recognition

RANSAC
verification



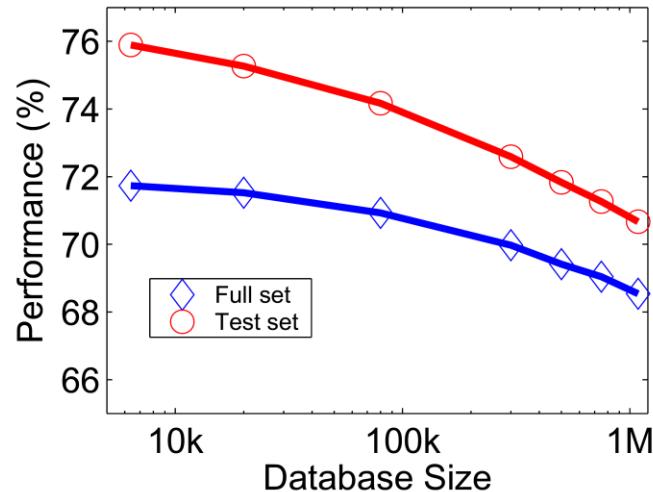
Quiz Questions

- **What is the computational advantage of the hierarchical representation vs. a flat vocabulary?**
- **What dangers does such a representation carry?**

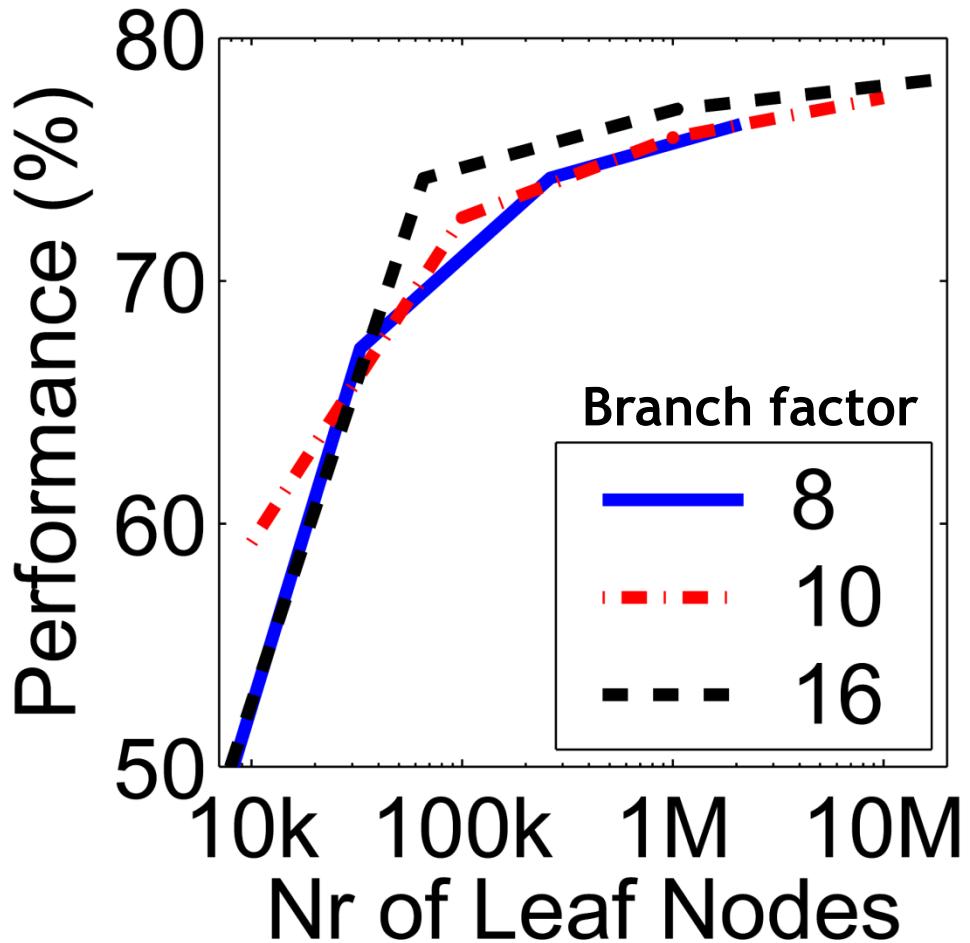
Vocabulary Tree: Performance

- Evaluated on large databases
 - Indexing with up to 1M images
- Online recognition for database of 50,000 CD covers
 - Retrieval in ~1s (in 2006)
- Experimental finding that large vocabularies can be beneficial for recognition

[Nister & Stewenius, CVPR'06]



Vocabulary Size



- Larger vocabularies can be advantageous...
- But what happens when the vocabulary gets too large?
 - Efficiency?
 - Robustness?

tf-idf Weighting

- Term frequency - inverse document frequency
- Describe frame by frequency of each word within it, downweight words that appear often in the database
- (Standard weighting for text retrieval)

$$t_i = \frac{n_{id}}{n_d} \log \frac{N}{n_i}$$

Number of occurrences of word i in document d

Number of words in document d

Total number of documents in database

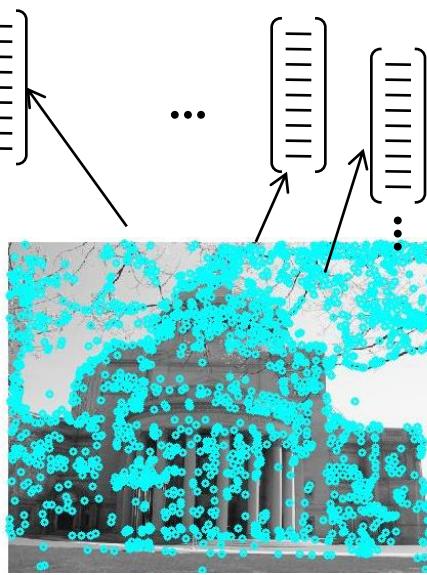
Number of occurrences of word i in whole database

Summary: Indexing features



Detect or sample features

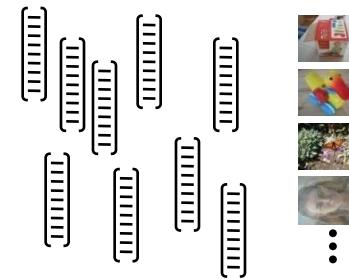
List of positions,
scales,
orientations



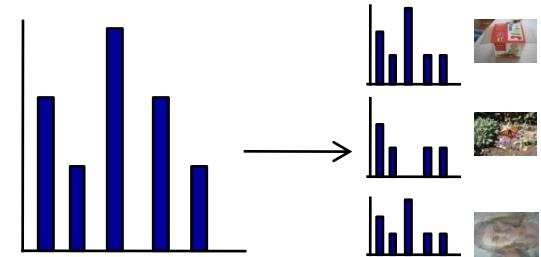
Describe features

Associated list of d-dimensional descriptors

or



Index each one into pool of descriptors from previously seen images



Quantize to form “bag of words” vector for the image

Application for Content Based Img Retrieval

- What if query of interest is a portion of a frame?

Visually defined query

“Find this
clock”



“Groundhog Day” [Rammis, 1993]



“Find this
place”



Video Google System

1. Collect all words within query region
2. Inverted file index to find relevant frames
3. Compare word counts
4. Spatial verification

Sivic & Zisserman, ICCV 2003

- Demo online at :
<http://www.robots.ox.ac.uk/~vgg/research/VideoGoogle/>



Query
region



Retrieved frames

Collecting Words Within a Query Region

- Example: Friends



Query region:
pull out only the SIFT
descriptors whose
positions are within the
polygon

Example Results



Query

raw nn 1sim=0.56697



raw nn 2sim=0.56163



raw nn 5sim=0.54917



B. Leibe

More Results



Query



Retrieved shots

Applications: Specific Object Recognition

- Commercial services coming out:

kooaba

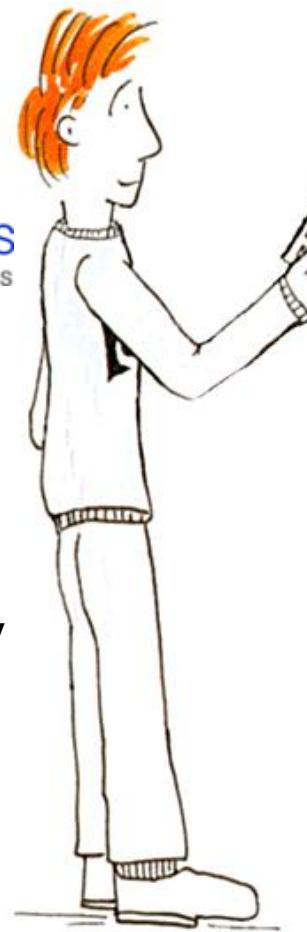
Google goggles
labs



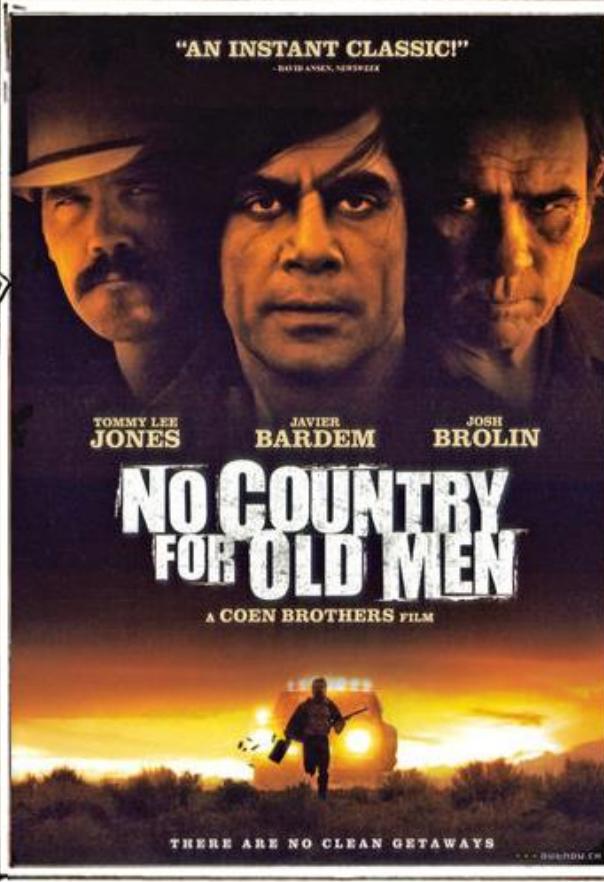
Works well for mostly planar objects:

- Movie posters,
- Book covers,
- CD/DVD covers,
- Video games,
- ...

MOBILE IMAGE RECOGNITION?
TRY IT OUT NOW!!!



kooaba



Show another poster

Movie data provided by:



(~20M images indexed)

1. POINT
YOUR MOBILE
PHONE CAMERA TO
THE MOVIE
POSTER.

2. SNAP A
PICTURE AND SEND
IT:

IN SWITZERLAND:
MMS TO 5555 (OR
079 394 57 00
FOR ORANGE
CUSTOMERS)

IN GERMANY:
MMS TO 84000

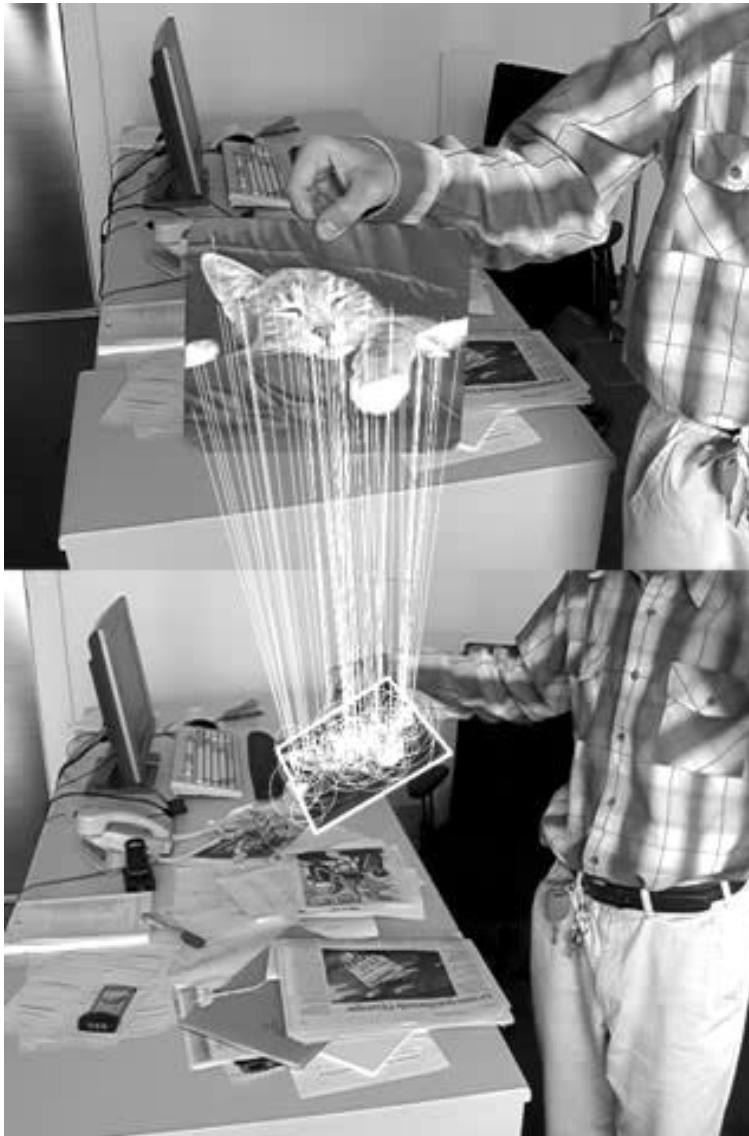
EVERYWHERE:
EMAIL TO
M@KOOABA.COM

3. FIND ALL
RELEVANT INFOR-
MATION ABOUT THE
MOVIE ON YOUR
MOBILE PHONE

Applications: Aachen Tourist Guide



Applications: Fast Image Registration



B. Leibe

Applications: Mobile Augmented Reality

Mobile Phone
Augmented Reality

at
30 Frames per Second
using
Natural Feature Tracking

(all processing and rendering done in software)

D. Wagner, G. Reitmayr, A. Mulloni, T. Drummond, D. Schmalstieg,
Pose Tracking from Natural Features on Mobile Phones. In *ISMAR 2008*.

References and Further Reading

- More details on RANSAC can be found in Chapter 4.7 of
 - R. Hartley, A. Zisserman
Multiple View Geometry in Computer Vision
2nd Ed., Cambridge Univ. Press, 2004
- Details about the Hough transform for object recognition can be found in
 - D. Lowe, Distinctive image features from scale-invariant keypoints,
IJCV 60(2), pp. 91-110, 2004
- Details about the Video Google system can be found in
 - J. Sivic, A. Zisserman,
Video Google: A Text Retrieval Approach to Object Matching in Videos, ICCV'03, 2003.

