

Computer Vision - Lecture 2

Binary Image Analysis

16.10.2014

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Announcements

- Course webpage
 - http://www.vision.rwth-aachen.de/teaching/
 - Slides will be made available on the webpage
- L2P electronic repository
 - Exercises and supplementary materials will be posted on the L2P

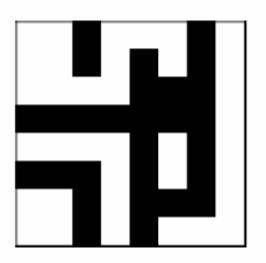
- Please subscribe to the lecture on the Campus system!
 - Important to get email announcements and L2P access!
 - Bachelor students please also subscribe



Binary Images

- Just two pixel values
- Foreground and background
- Regions of interest

1	1	0	1	1	1	0	1
1	1	0	1	0	1	0	1
1	1	1	1	0	0	0	1
0	0	0	0	0	0	0	1
1	1	1	1	0	1	0	1
0	0	0	1	0	1	0	1
1	1	0	1	0	0	0	1
1	1	0	1	0	1	1	1





Uses: Industrial Inspection

Fig. 3 Schematic diagram of marking inspection setup at Texas Instruments

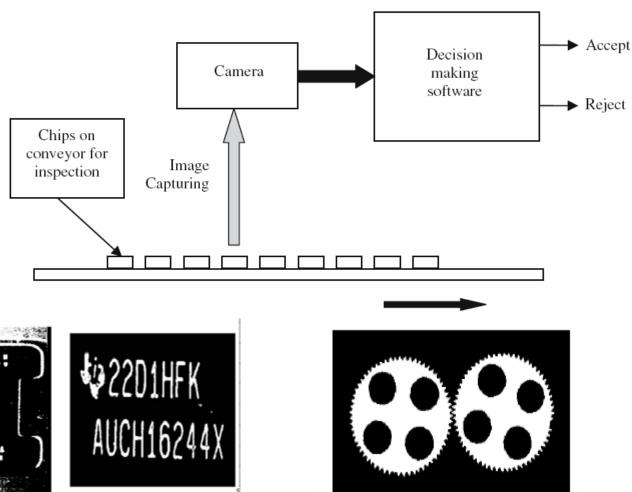




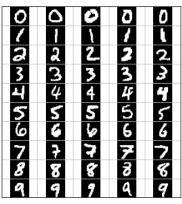




Fig. 7 Binarized image

Fig. 9 Row sum for separating a row

Uses: Document Analysis, Text Recognition



Handwritten digits

Final Andrews

The State State

Scanned documents







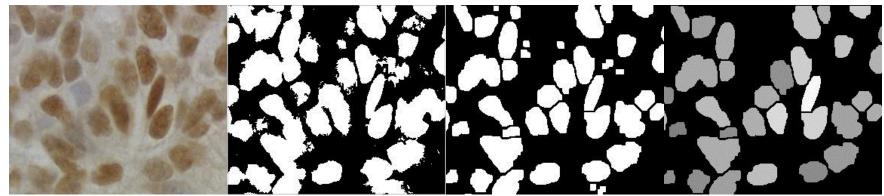




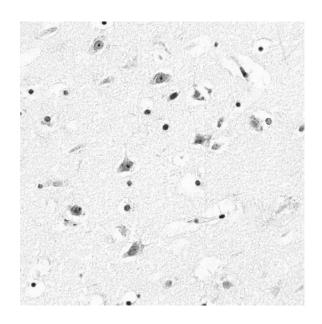
Source: Till Quack, Martin Renold

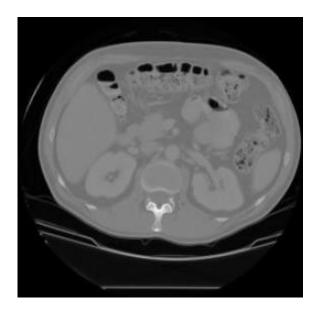


Uses: Medical/Bio Data



Source: D. Kim et al., Cytometry 35(1), 1999

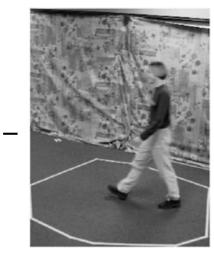




Uses: Blob Tracking & Motion Analysis

Frame Differencing







Source: Kristen Grauman

Background Subtraction





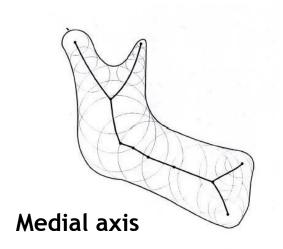


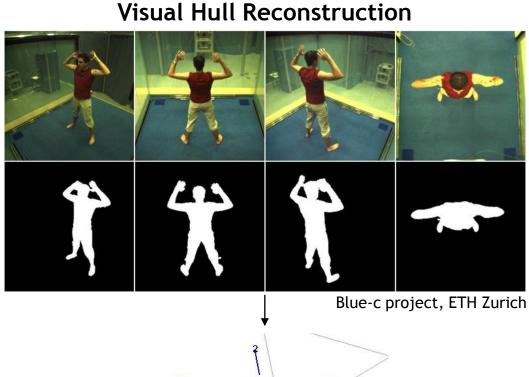
Source: Tobias Jäggli

Uses: Shape Analysis, Free-Viewpoint Video



Silhouette





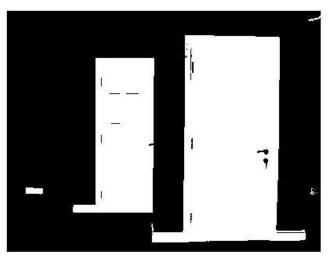
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Uses: Intensity Based Detection

Looking for dark pixels...





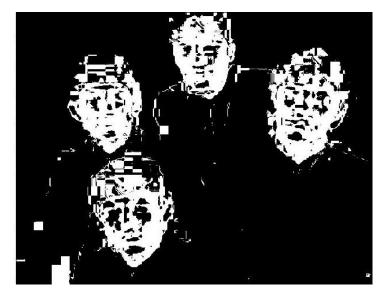
fg pix = find(im < 65);



Uses: Color Based Detection

Looking for pixels within a certain color range...



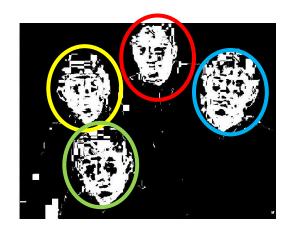


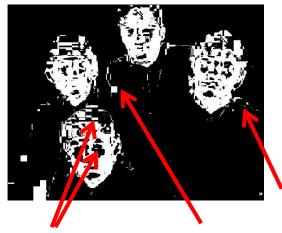
 $fg_pix = find(hue > t1 & hue < t2);$



Issues

- How to demarcate multiple regions of interest?
 - Count objects
 - Compute further features per object
- What to do with "noisy" binary outputs?
 - Holes
 - Extra small fragments

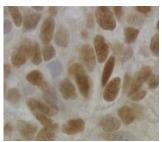


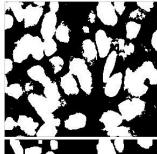


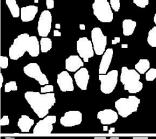


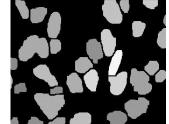
Outline of Today's Lecture

- Convert the image into binary form
 - > Thresholding
- Clean up the thresholded image
 - Morphological operators
- Extract individual objects
 - Connected Components Labeling
- Describe the objects
 - Region properties









Thresholding

- Grayscale image ⇒ Binary mask
- Different variants
 - One-sided

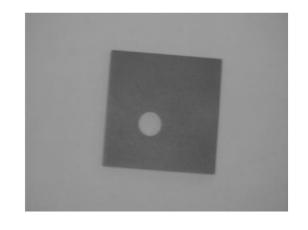
$$F_T[i,j] = \begin{cases} 1, & \text{if } F[i,j] \ge T \\ 0, & \text{otherwise} \end{cases}$$

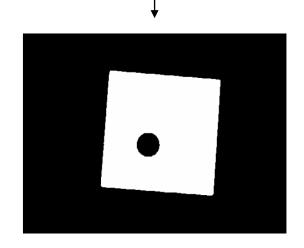
> Two-sided

$$F_T[i,j] = \begin{cases} 1, & \text{if } T_1 \le F[i,j] \le T_2 \\ 0, & \text{otherwise} \end{cases}$$

Set membership

$$F_T[i,j] = \begin{cases} 1, & \text{if } F[i,j] \in \mathbb{Z} \\ 0, & \text{otherwise} \end{cases}$$

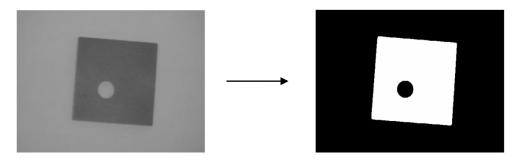






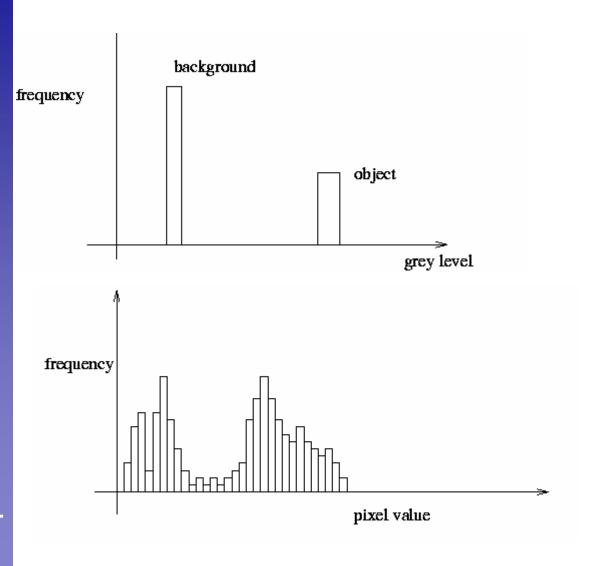
Selecting Thresholds

- Typical scenario
 - Separate an object from a distinct background



- Try to separate the different grayvalue distributions
 - Partition a bimodal histogram
 - Fit a parametric distribution (e.g. Mixture of Gaussians)
 - Dynamic or local thresholds
- In the following, I will present some simple methods.
 - We will then see some more general methods in Lecture 6...

A Nice Case: Bimodal Intensity Histograms



Ideal histogram, light object on dark background

Actual observed histogram with noise

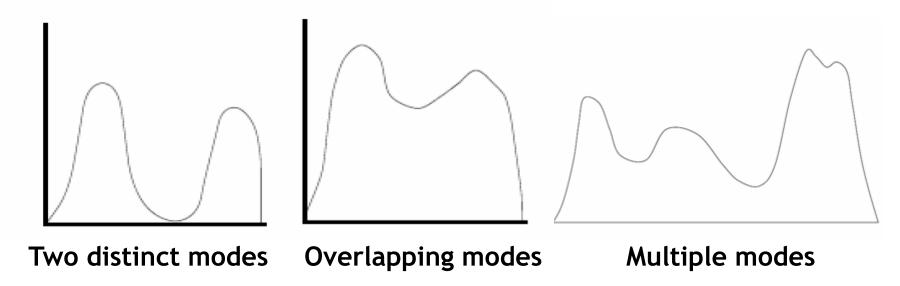
Source: Robyn Owens

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Not so Nice Cases...

How to separate those?



- Threshold selection is difficult in the general case
 - Domain knowledge often helps
 - \rightarrow E.g. Fraction of text on a document page (\Rightarrow histogram quantile)
 - E.g. Size of objects/structure elements



Global Binarization [Otsu'79]

• Search for the threshold T that minimizes the withinclass variance σ_{within} of the two classes separated by T

$$\sigma_{within}^{2}(T) = n_1(T)\sigma_1^2 + n_2(T)\sigma_2^2(T)$$

where

$$n_1(T) = |\{I_{(x,y)} < T\}|, \quad n_2(T) = |\{I_{(x,y)} \ge T\}|$$

• This is the same as maximizing the between-class variance $\sigma_{hetween}$

$$\sigma_{between}^2(T) = \sigma^2 - \sigma_{within}^2(T)$$
$$= n_1(T)n_2(T) \left[\mu_1(T) - \mu_2(T)\right]^2$$

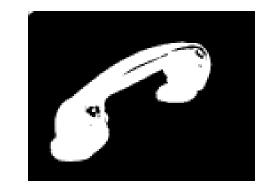


Algorithm

- 1. Precompute a cumulative grayvalue histogram h.
- **2.** For each potential threshold T
 - a) Separate the pixels into two clusters according to T
 - b) Look up n_1 , n_2 in h and compute both cluster means
 - c) Compute $\sigma_{between}^2(T) = n_1(T) n_2(T) \left[\mu_1(T) \mu_2(T) \right]^2$
- 3. Choose

$$T^* = \arg\max_{T} \left[\sigma_{between}^2(T) \right]$$





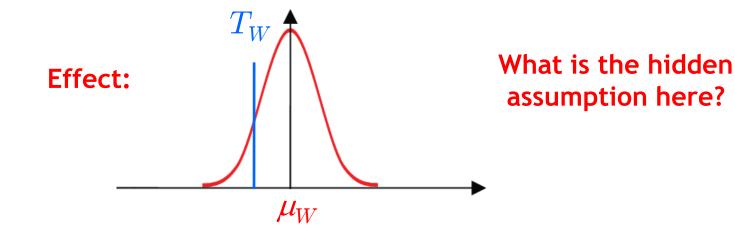


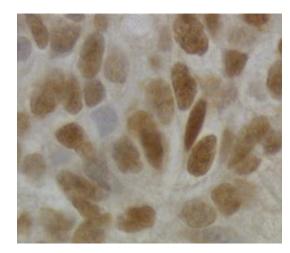
Local Binarization [Niblack'86]

• Estimate a local threshold within a small neighborhood window ${\cal W}$

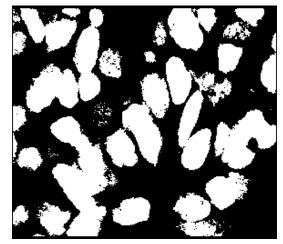
$$T_W = \mu_W + k \cdot \sigma_W$$

where $k \in [-1,0]$ is a user-defined parameter.

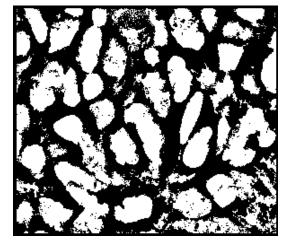




Original image



Global threshold selection (Otsu)

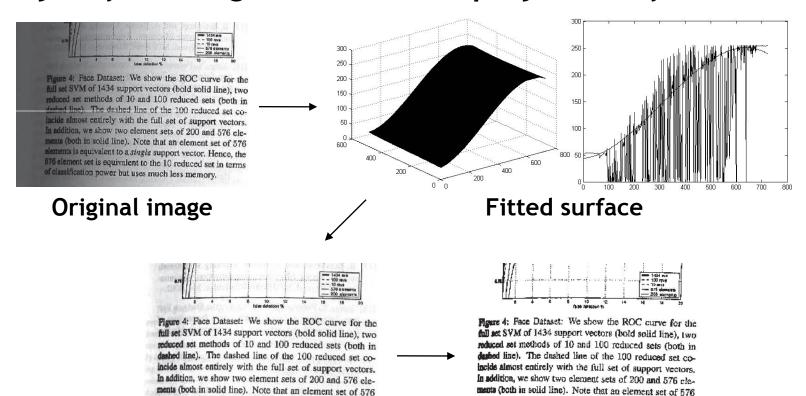


Local threshold selection (Niblack)



Additional Improvements

- Document images often contain a smooth gradient
- ⇒Try to fit that gradient with a polynomial function



Shading compensation

of classification power but uses much less memory.

elements is equivalent to a single support vector. Hence, the

576 element set is equivalent to the 10 reduced set in terms

Binarized result

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576 element set is equivalent to the 10 reduced set in terms

of classification power but uses much less memory.



Polynomial Surface Fitting

Polynomial surface of degree d

$$f(x,y) = \sum_{i+j=0}^{a} b_{i,j} x^{i} y^{j}$$

• For an image pixel (x_0,y_0) with intensity I_0 , this means

$$b_{0,0} + b_{1,0}x_0 + b_{0,1}y_0 + b_{2,0}x_0^2 + b_{1,1,1}x_0y_0 + \dots + b_{0,3}y_0^3 = I_0$$

• Least-squares estimation, e.g. for d=3

$$b = (A^T A)^{-1} A^T I$$

$$b = I \setminus A$$



Surface Fitting

- Iterative Algorithm
 - 1.) Fit parametric surface to all points in region.
 - 2.) Subtract estimated surface.
 - 3.) Apply global threshold (e.g. with Otsu method)

Initial guess

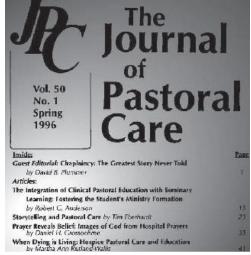
- 4.) Fit surface to all background pixels in original region.
- 5.) Subtract estimated surface.
- 6.) Apply global threshold (Otsu)

Refined guess

- 7.) Iterate further if needed...
- · The first pass also takes foreground pixels into account.
 - This is corrected in the following passes.
 - Basic assumption here: most pixels belong to the background.

Result Comparison

Original image



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No. 1
Spring
1996

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Global (Otsu)

Local (Niblack)



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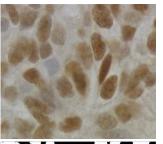
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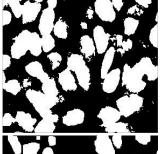
Polynomial + Global

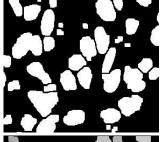


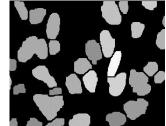
Outline of Today's Lecture

- Convert the image into binary form
 - > Thresholding
- Clean up the thresholded image
 - Morphological operators
- Extract individual objects
 - Connected Components Labeling
- Describe the objects
 - Region properties





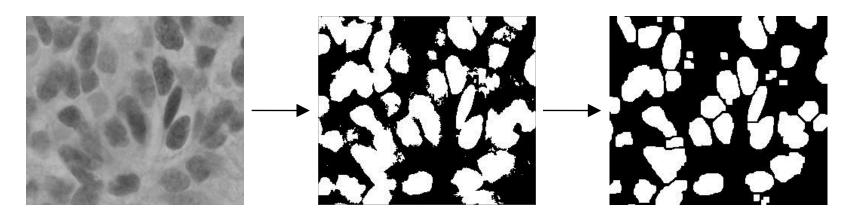






Cleaning the Binarized Results

Results of thresholding often still contain noise

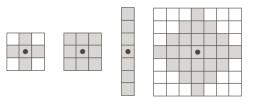


- Necessary cleaning operations
 - Remove isolated points and small structures
 - Fill holes
- ⇒ Morphological Operators



Morphological Operators

- Basic idea
 - Scan the image with a structuring element
 - Perform set operations (intersection, union) of image content with structuring element



Matlab:

>> help strel

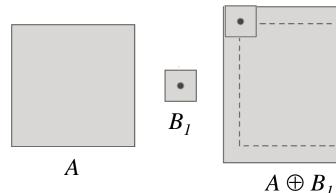
- Two basic operations
 - > Dilation (Matlab: imdilate)
 - > Erosion (Matlab: imerode)
- Several important combinations
 - > Opening (Matlab: imopen)
 - > Closing (Matlab: imclose)
 - Boundary extraction

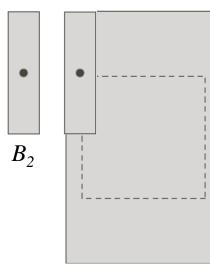
Dilation

Definition

- "The dilation of A by B is the set of all displacements z, such that $(\hat{B})_z$ and A overlap by at least one element".
- $((\hat{B})_z)$ is the mirrored version of B, shifted by z)

- If current pixel z is foreground, set all pixels under $(B)_z$ to foreground.
- ⇒ Expand connected components
- ⇒ Grow features
- ⇒ Fill holes





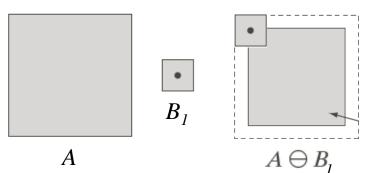
 $A \oplus B_2$



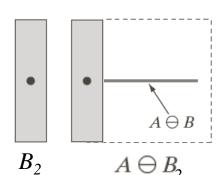
Erosion

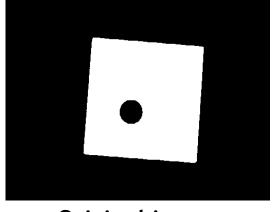
Definition

"The erosion of A by B is the set of all displacements z, such that $(B)_z$ is entirely contained in A".

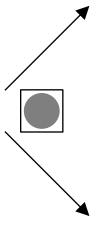


- > If not every pixel under $(B)_z$ is foreground, set the current pixel z to background.
- ⇒ Erode connected components
- ⇒ Shrink features
- ⇒ Remove bridges, branches, noise

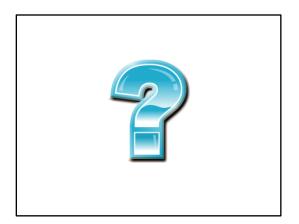




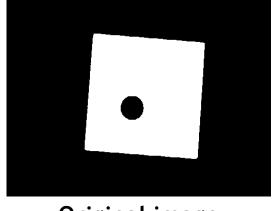
Original image



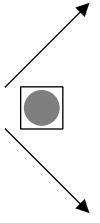
Dilation with circular structuring element



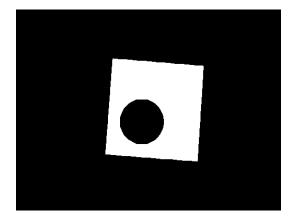
Erosion with circular structuring element



Original image



Dilation with circular structuring element



Erosion with circular structuring element

Opening

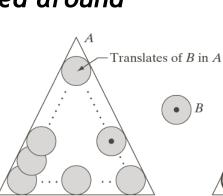
- Definition
 - Sequence of Erosion and Dilation

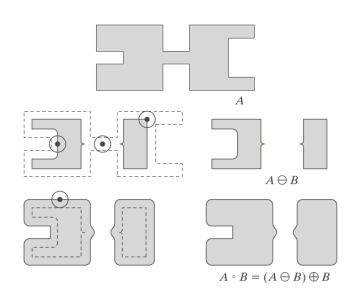
$$A \circ B = (A \ominus B) \oplus B$$

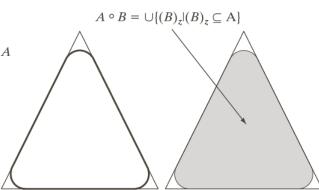


 $A \circ B$ is defined by the points that are reached if B is rolled around inside A.

⇒ Remove small objects, keep original shape.



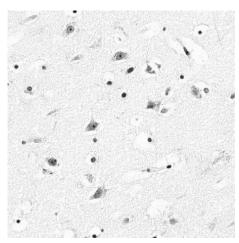




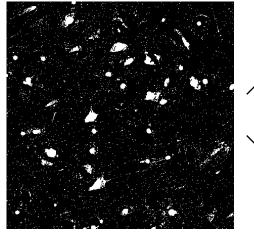


Effect of Opening

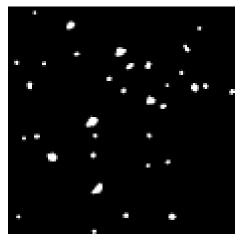
Feature selection through size of structuring element



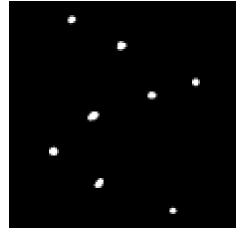
Original image



Thresholded



Opening with small structuring element

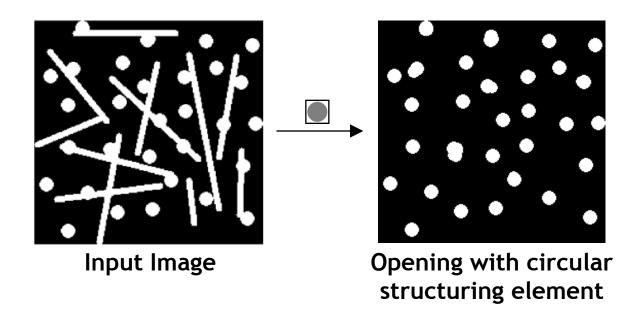


Opening with larger structuring element



Effect of Opening

Feature selection through shape of structuring element



• How could we have extracted the lines?

 $A \oplus B$

 $A \cdot B = (A \oplus B) \ominus B$

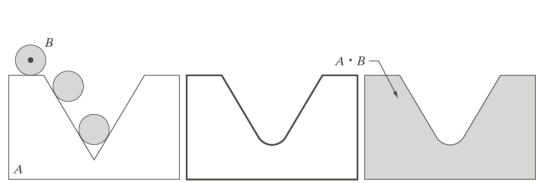
Closing

- Definition
 - Sequence of Dilation and Erosion

$$A \cdot B = (A \oplus B) \ominus B$$



- $A \cdot B$ is defined by the points that are reached if B is rolled around on the outside of A.
- ⇒ Fill holes, keep original shape.





Effect of Closing

 Fill holes in thresholded image (e.g. due to specularities)

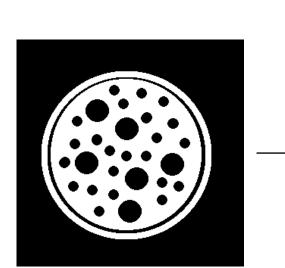


Original image

Size of structuring element determines which structures are selectively filled.

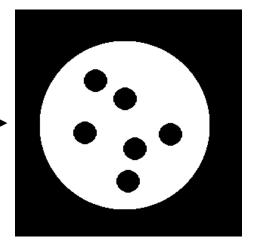


Thresholded





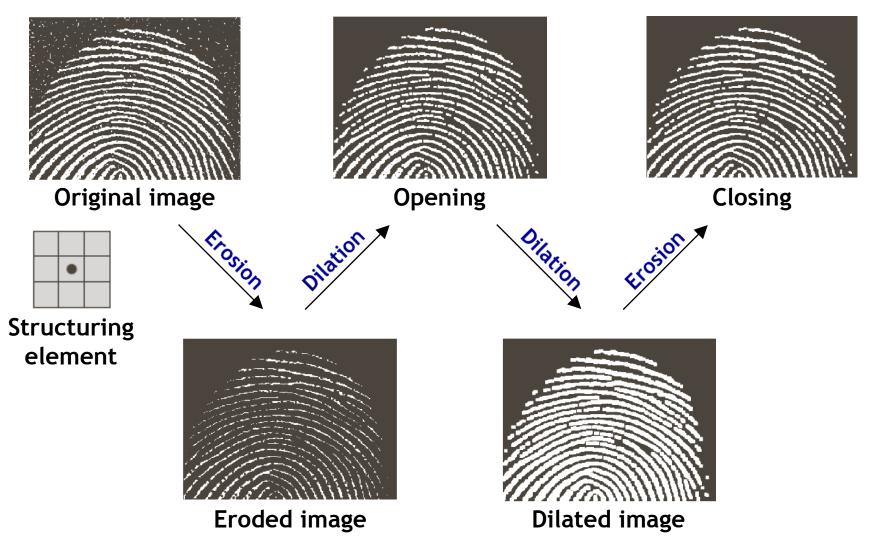
Closing with circular structuring element



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Example Application: Opening + Closing

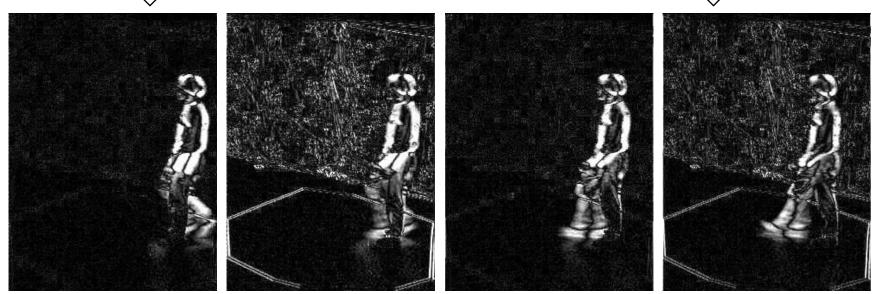




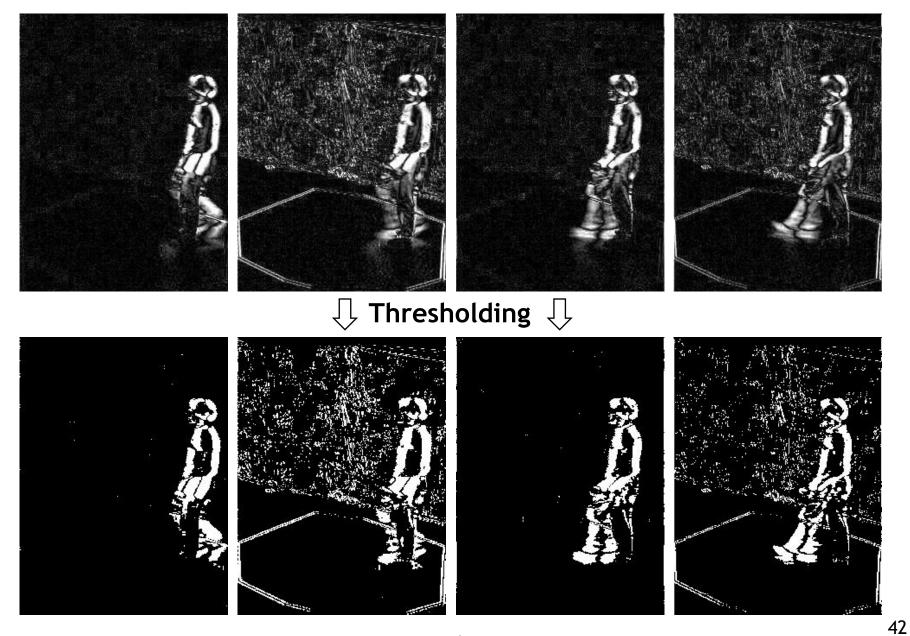
Application: Blob Tracking



 $igcup_{}$ Absolute differences from frame to frame $igcup_{}$

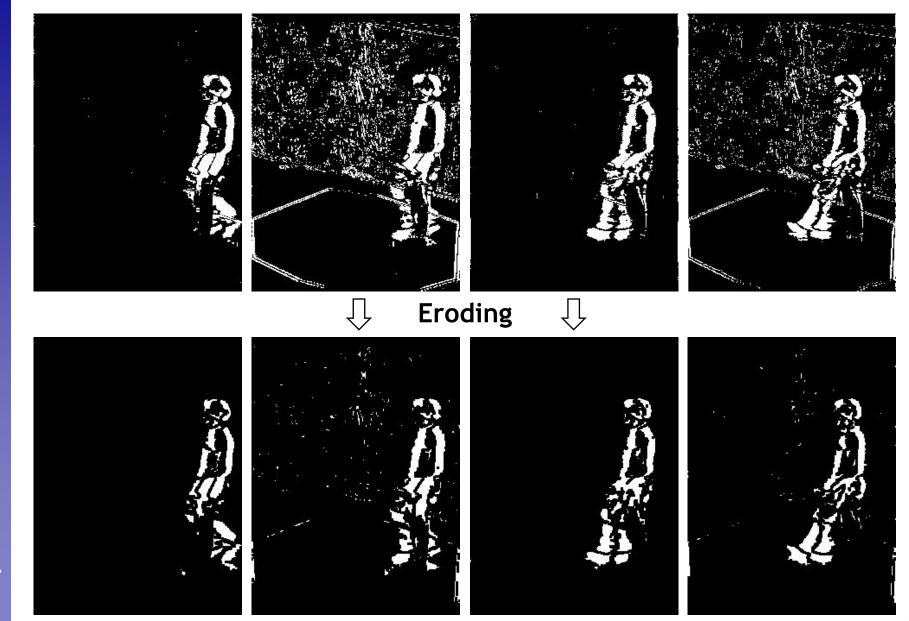


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B. Leibe

Slide credit: K. Grauman



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Morphological Boundary Extraction

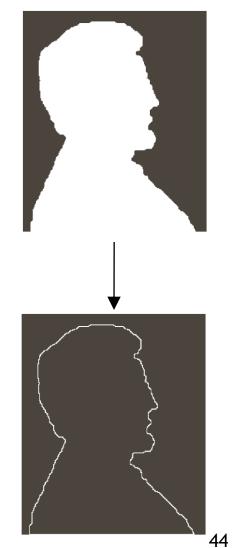
Definition

First erode A by B, then subtract the result from the original A.

$$\beta(A) = A - (A \ominus B)$$

Effects

If a 3×3 structuring element is used, this results in a boundary that is exactly 1 pixel thick.



Morphology Operators on Grayscale Images

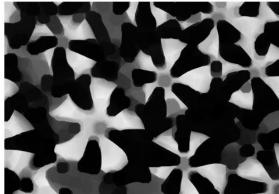
- Dilation and erosion are typically performed on binary images.
- If image is grayscale: for dilation take the neighborhood max, for erosion take the min.



Original



Dilated

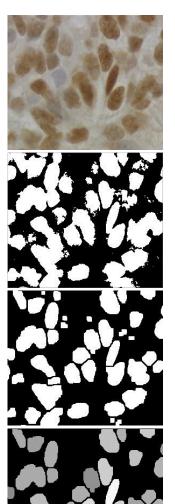


Eroded



Outline of Today's Lecture

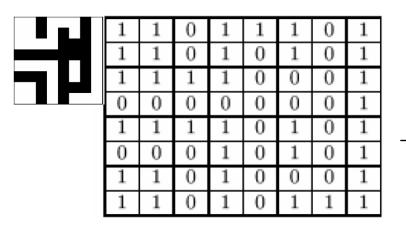
- Convert the image into binary form
 - > Thresholding
- Clean up the thresholded image
 - > Morphological operators
- Extract individual objects
 - Connected Components Labeling
- Describe the objects
 - Region properties

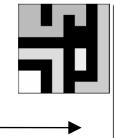




Connected Components Labeling

Goal: Identify distinct regions

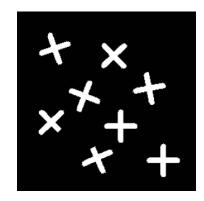




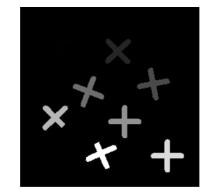
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I	1	1	0	1	1	1	0	2
ı	1	1	0	1	0	1	0	2
ı	1	1	1	1	0	0	0	2
l	0	0	0	0	0	0	0	2
	3	3	3	3	0	4	0	2
	0	0	0	3	0	4	0	2
	5	5	0	3	0	0	0	2
	5	5	0	3	0	2	2	2

Binary image

Connected components labeling

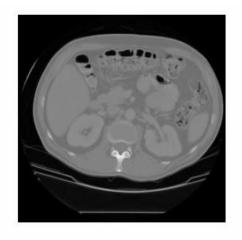


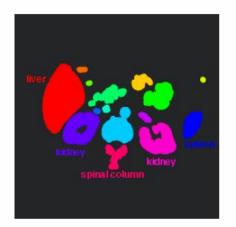






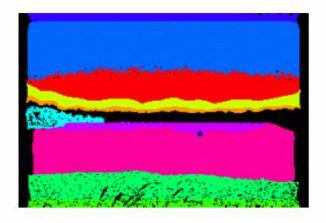
Connected Components Examples





connected components of 1's from thresholded image





connected components of cluster labels

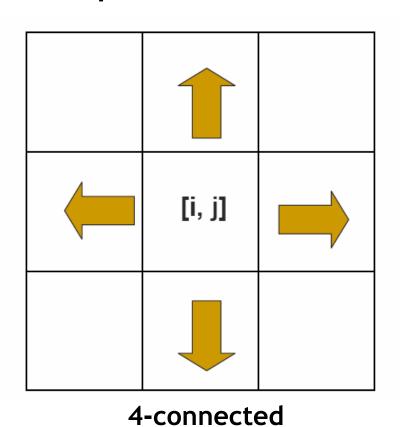
Source: Pinar Duygulu

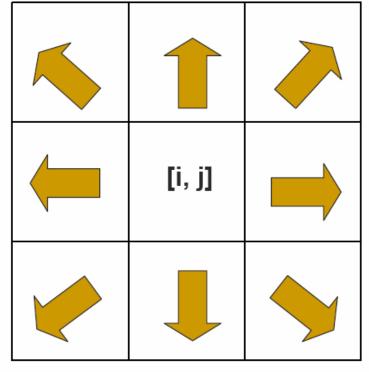
B. Leibe



Connectedness

Which pixels are considered neighbors?



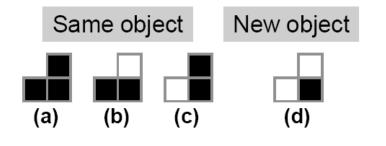


8-connected

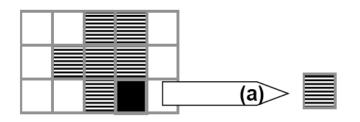


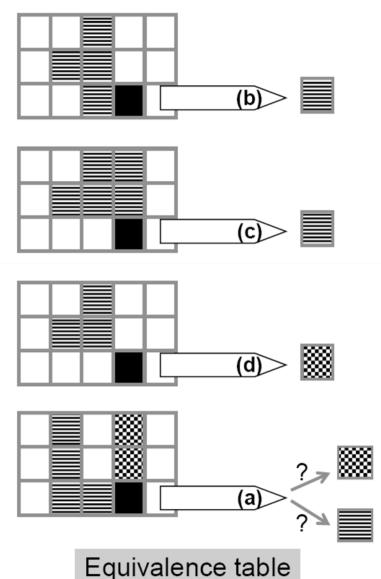
Sequential Connected Components

- Labeling a pixel only requires to consider its prior and superior neighbors.
- It depends on the type of connectivity used for foreground (4-connectivity here).



What happens in these cases?





B. Leibe

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Sequential Connected Components (2)

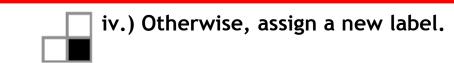
- Process the image from left to right, top to bottom:
 - 1.) If the next pixel to process is 1

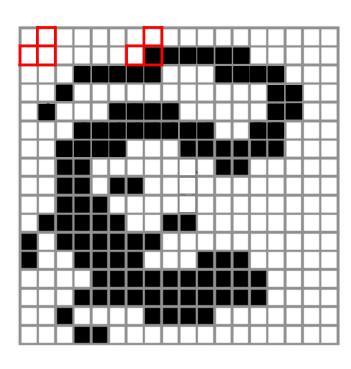


- i.) If only one of its neighbors (top or left) is 1, copy its label.
- ii.) If both are 1 and have the same label, copy it.



- iii.) If they have different labels
 - Copy the label from the left.
 - Update the equivalence table.





Equivalence table

{1}

51



Sequential Connected Components (2)

- Process the image from left to right, top to bottom:
 - 1.) If the next pixel to process is 1



i.) If only one of its neighbors (top or left) is 1, copy its label.



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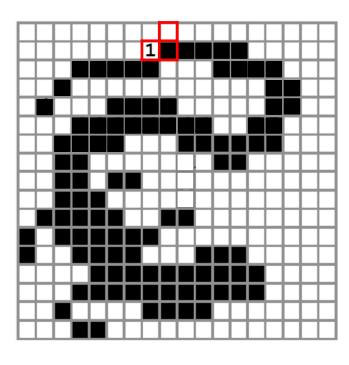


iii.) If they have different labels

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- Update the equivalence table.



iv.) Otherwise, assign a new label.



Equivalence table

{1}

Sequential Connected Components (2)

- Process the image from left to right, top to bottom:
 - 1.) If the next pixel to process is 1

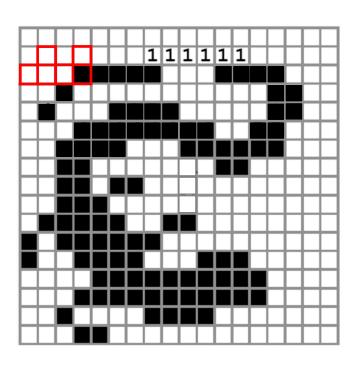


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Equivalence table

{1}

{2}

Sequential Connected Components (2)

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- i.) If only one of its neighbors(top or left) is 1, copy its label.
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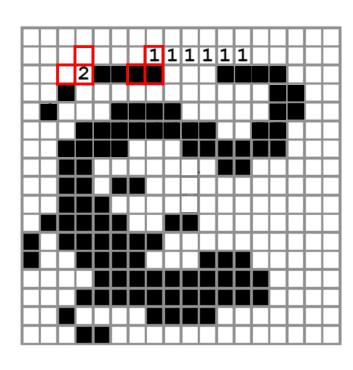


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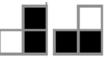
Equivalence table

{1} 2}

{2}

Sequential Connected Components (2)

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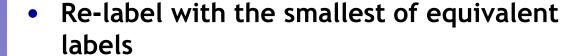


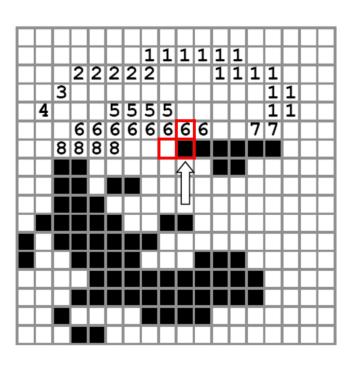
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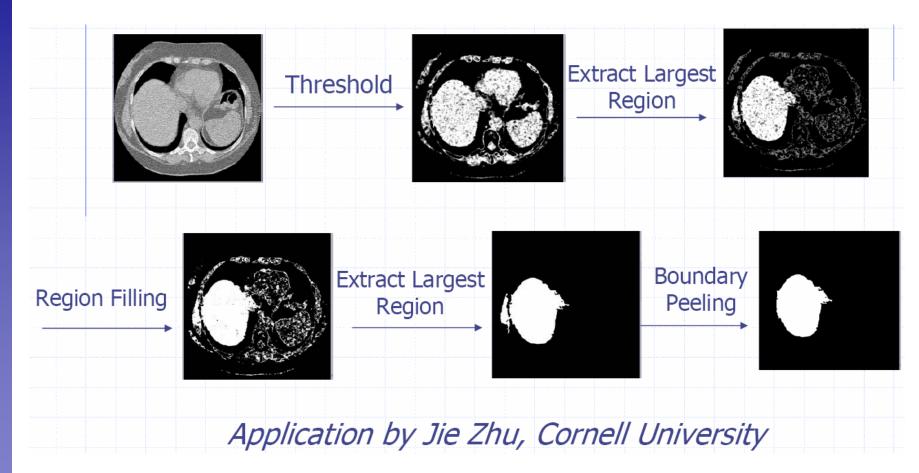




Equivalence table



Application: Segmentation of a Liver

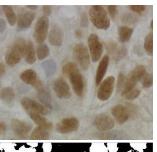


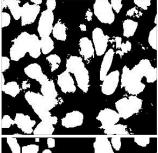
56

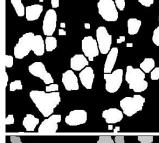


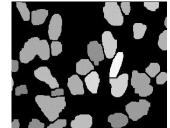
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Region Properties

- From the previous steps, we can obtain separated objects.
- Some useful features can be extracted once we have connected components, including
 - Area
 - Centroid
 - Extremal points, bounding box
 - Circularity
 - Spatial moments





Area and Centroid

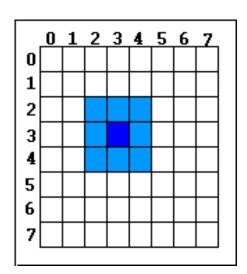
- We denote the set of pixels in a region by R
- Assuming square pixels, we obtain
 - > Area:

$$A = \sum_{(x,y)\in R} 1$$

Centroid:

$$\overline{x} = \frac{1}{A} \sum_{(x,y) \in R} x$$

$$\overline{y} = \frac{1}{A} \sum_{(x,y) \in R} y$$





Circularity

Measure the deviation from a perfect circle

> Circularity:
$$C = \frac{\mu_R}{\sigma_R}$$

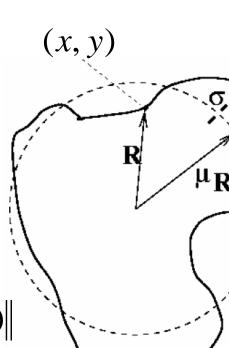
where μ_R and σ_R^2 are the mean and variance of the distance from the centroid of the shape to the boundary pixels (x_k, y_k) .



$$\mu_{R} = \frac{1}{K} \sum_{k=0}^{K-1} ||(x_{k}, y_{k}) - (\bar{x}, \bar{y})||$$



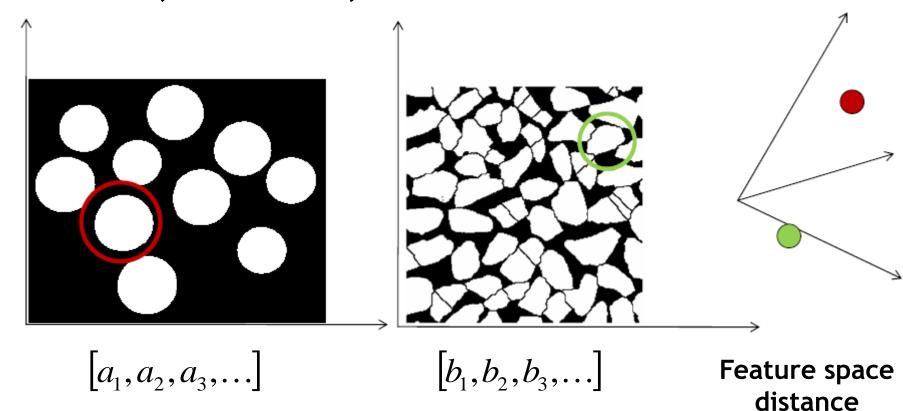
$$\sigma_R^2 = \frac{1}{K} \sum_{k=0}^{K-1} \left[\| (x_k, y_k) - (\bar{x}, \bar{y}) \| - \mu_R \right]^2$$





Invariant Descriptors

 Often, we want features independent of location, orientation, scale.





Central Moments

- S is a subset of pixels (region).
- Central (j,k)th moment defined as:

$$\mu_{jk} = \sum_{(x,y)\in S} (x - \overline{x})^j (y - \overline{y})^k$$

• Invariant to translation of S.

Interpretation:

- > 0th central moment: area
- > 2nd central moment: *variance*
- > 3rd central moment: *skewness*
- > 4th central moment: *kurtosis*



Moment Invariants ("Hu Moments")

Normalized central moments

$$\eta_{pq} = \frac{\mu_{pq}}{\mu_{00}^{\gamma}}, \qquad \gamma = \frac{p+q}{2} + 1$$

• From those, a set of *invariant moments* can be defined for object description.

$$\phi_1 = \eta_{20} + \eta_{02}$$

$$\phi_2 = (\eta_{20} - \eta_{02})^2 + 4\eta_{11}^2$$

$$\phi_3 = (\eta_{30} - 3\eta_{12})^2 + (3\eta_{21} - \eta_{03})^2$$

$$\phi_4 = (\eta_{30} + \eta_{12})^2 + (\eta_{21} + \eta_{03})^2$$

 Robust to translation, rotation & scaling, but don't expect wonders (still summary statistics).



Moment Invariants

$$\phi_5 = (\eta_{30} - 3\eta_{12})(\eta_{30} + \eta_{12}) \left[(\eta_{30} + \eta_{12})^2 - 3(\eta_{21} + \eta_{03})^2 \right]$$

$$+ (3\eta_{21} - \eta_{03})(\eta_{21} + \eta_{03}) \left[3(\eta_{30} + \eta_{12})^2 - (\eta_{21} + \eta_{03})^2 \right]$$

$$\phi_6 = (\eta_{20} - \eta_{02}) [(\eta_{30} + \eta_{12})^2 - (\eta_{21} + \eta_{03})^2] + 4\eta_{11}(\eta_{30} + \eta_{12})(\eta_{21} + \eta_{03})$$

$$\phi_7 = (3\eta_{21} - \eta_{03})(\eta_{30} + \eta_{12}) \left[(\eta_{30} + \eta_{12})^2 - 3(\eta_{21} + \eta_{03})^2 \right]$$

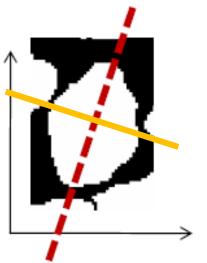
$$+ (3\eta_{12} - \eta_{30})(\eta_{21} + \eta_{03}) \left[3(\eta_{30} + \eta_{12})^2 - (\eta_{21} + \eta_{03})^2 \right]$$

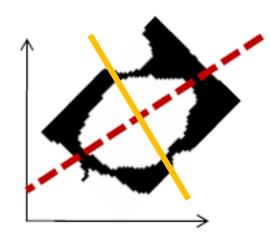
Often better to use $\log_{10}(\phi_i)$ instead of ϕ_i directly...



Axis of Least Second Moment

- Invariance to orientation?
 - Need a common alignment





Axis for which the squared distance to 2D object points is minimized (maximized).

Compute Eigenvectors of 2nd moment matrix (Matlab: eig(A))

$$\begin{bmatrix} \mu_{20} & \mu_{11} \\ \mu_{11} & \mu_{02} \end{bmatrix} = VDV^{T} = \begin{bmatrix} v_{11} & v_{12} \\ v_{22} & v_{22} \end{bmatrix} \begin{bmatrix} \lambda_{1} & 0 \\ 0 & \lambda_{2} \end{bmatrix} \begin{bmatrix} v_{11} & v_{12} \\ v_{21} & v_{22} \end{bmatrix}^{T}$$



Summary: Binary Image Processing

Pros

- Fast to compute, easy to store
- Simple processing techniques
- Can be very useful for constrained scenarios

Cons

- Hard to get "clean" silhouettes
- Noise is common in realistic scenarios
- Can be too coarse a representation
- Cannot deal with 3D changes



References and Further Reading

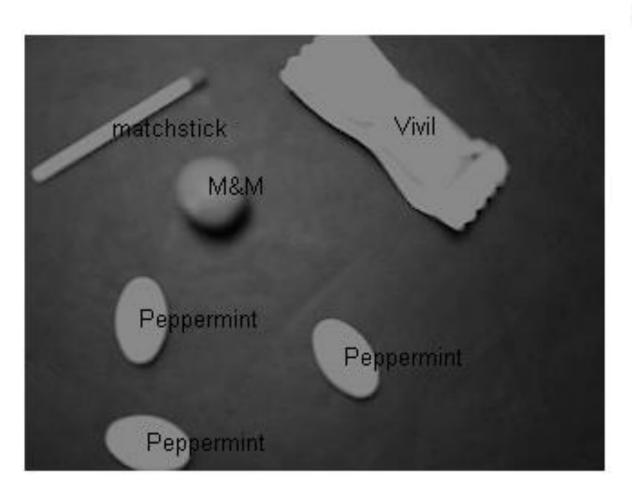
- More on morphological operators can be found in
 - R.C. Gonzales, R.E. Woods,
 Digital Image Processing.
 Prentice Hall, 2001
- Online tutorial and Java demos available on
 - http://homepages.inf.ed.ac.uk/rbf/HIPR2/



Questions?



Demo "Haribo Classification"





You Can Do It At Home...

Accessing a webcam in Matlab:

img=getsnapshot(cam);

```
function out = webcam
% uses "Image Acquisition Toolbox,"
adaptorName = 'winvideo';
vidFormat = 'I420 320x240';
vidObj1= videoinput(adaptorName, 1, vidFormat);
set(vidObj1, 'ReturnedColorSpace', 'rgb');
set(vidObj1, 'FramesPerTrigger', 1);
out = vidObj1 ;
cam = webcam();
```





Questions?